Limits on Extra Dimensions and New Particle Production in the Exclusive Photon and Missing Energy Signature in $p\bar{p}$ Collisions at $\sqrt{s} = 1.8$ TeV

The exclusive $\gamma E_T$ signal has a small standard model cross section and is thus a channel sensitive to new physics. This signature is predicted by models with a superlight gravitino or with large extra spatial dimensions. We search for such signals at the Collider Detector at Fermilab, using $87\text{ pb}^{-1}$ of data at $\sqrt{s} = 1.8\text{ TeV}$, and extract $95\%$ C.L. limits on these processes. A limit of $221\text{ GeV}$ is set on the scale $|F|^{1/2}$ in supersymmetric models. For $4, 6,$ and $8$ extra dimensions, model-dependent limits on the fundamental mass scale $M_D$ of $0.55, 0.58,$ and $0.60\text{ TeV}$, respectively, are found. We also specify a “pseudo-model-independent” method of comparing the results to theoretical predictions.

Many extensions to the standard model predict the existence of minimally interacting particles, such as the gravitino in supersymmetric models and Kaluza-Klein (KK) modes of the graviton in models with large compact spatial dimensions [1]. Such particles cannot be directly observed in a detector, but their production can be inferred from missing transverse energy ($E_T$ [2]) among the visible particles in a high-energy collision. Photons can be emitted in such hard-scattering processes due to the presence of charged quarks in the $p\bar{p}$ initial state; many models also predict the production of photons during data taking. Level 1 requires a central tower with $E_T^{\text{EM}} > 8\text{ GeV}$ [6]. The Level 2 system forms clusters of towers and then requires the event to pass a logical OR of several triggers, including (a) a loose trigger requiring only an electromagnetic cluster [8] with $E_T^{\text{EM}} > 50\text{ GeV}$ and (b) a trigger requiring $E_T > 35\text{ GeV}$. Level 3 requires that the photon candidate satisfy $E_T > 50\text{ GeV}$ and have a CES cluster within the fiducial region [9].

The CDF three-level trigger system [7] selects events with high-$p_T$ photons during data taking. Level 1 requires a central tower with $E_T^{\text{EM}} > 8\text{ GeV}$ [6]. The Level 2 system forms clusters of towers and then requires the event to pass a logical OR of several triggers, including (a) a loose trigger requiring only an electromagnetic cluster [8] with $E_T^{\text{EM}} > 50\text{ GeV}$ and (b) a trigger requiring $E_T > 35\text{ GeV}$. Level 3 requires that the photon candidate satisfy $E_T > 50\text{ GeV}$ and have a CES cluster within the fiducial region [9].

The off-line photon candidate identification (“photon ID”) criteria [9–11] are (a) an electromagnetic cluster in the CEM with $|\eta| < 1$ [12], a ratio $E^{\text{HAD}}/E^{\text{EM}}$ less than $0.055 + 0.00045 \times E_{\text{ESUM}}$, a centroid within the fiducial region of the CES, and shower evolution measured by the CES consistent with expectation; (b) no second energetic object in the same CES wire chamber as the cluster; (c) at most one CTC track, and none with $p_T > 1\text{ GeV}$ [13], pointing at the cluster; (d) within a radius of 0.4 in $\eta-\phi$ space around the cluster centroid, $E_T$ (summed over towers excluding those in the photon cluster) <2 GeV and a sum of track $p_T < 5\text{ GeV}$; (e) $E_T^\gamma > 55\text{ GeV}$ [14]; and (f) an event vertex within 60 cm of the center of the detector along the beam line.
We require $E_T > 45$ GeV. This threshold is lower than the $E_T^\gamma$ threshold to give full efficiency for signal processes, taking into consideration the $E_T$ resolution and the intrinsic parton $p_T$ in the $p$ and $\bar{p}$ initial states.

Backgrounds to the $\gamma E_T$ signal include: (a) $q\bar{q} \rightarrow Z \gamma \rightarrow \nu \bar{\nu} \gamma$; (b) cosmic ray muons that undergo bremsstrahlung in the CEM but for which no track is found; (c) $W \rightarrow e\nu$ with the electron misidentified as a photon; (d) $W\gamma$ production where the charged lepton in a leptonic $W$ decay is lost; (e) prompt $\gamma\gamma$ production where a photon is lost; and (f) dijet and photon + jet production. The expected number of events from each background source is shown in Table I.

To reject cosmic ray muons, we require a timing signal in the hadronic calorimeter which is in-time with the collision within a window 55 ns wide for at least one tower in the cluster, and no evidence of a muon in the central muon systems within 30$^\circ$ in $\phi$ of the photon. The efficiency of requiring timing information rises with $E_T^\gamma$ from 78% at 55 GeV to over 98% above 100 GeV; the timing resolution for photons is on the order of 4 ns. The efficiency of requiring timing information rises with $E_T^\gamma$. To reject cosmic ray muons, we require a timing signal in the hadronic calorimeter which is in-time with the collision within a window 55 ns wide for at least one tower in the cluster, and no evidence of a muon in the central muon systems within 30$^\circ$ in $\phi$ of the photon. The efficiency of requiring timing information rises with $E_T^\gamma$ from 78% at 55 GeV to over 98% above 100 GeV; the timing resolution for photons is on the order of 4 ns. The efficiency of requiring timing information rises with $E_T^\gamma$. To reject cosmic ray muons, we require a timing signal in the hadronic calorimeter which is in-time with the collision within a window 55 ns wide for at least one tower in the cluster, and no evidence of a muon in the central muon systems within 30$^\circ$ in $\phi$ of the photon. The efficiency of requiring timing information rises with $E_T^\gamma$ from 78% at 55 GeV to over 98% above 100 GeV; the timing resolution for photons is on the order of 4 ns. The efficiency of requiring timing information rises with $E_T^\gamma$. To reject cosmic ray muons, we require a timing signal in the hadronic calorimeter which is in-time with the collision within a window 55 ns wide for at least one tower in the cluster, and no evidence of a muon in the central muon systems within 30$^\circ$ in $\phi$ of the photon. The efficiency of requiring timing information rises with $E_T^\gamma$ from 78% at 55 GeV to over 98% above 100 GeV; the timing resolution for photons is on the order of 4 ns. The efficiency of requiring timing information rises with $E_T^\gamma$. To reject cosmic ray muons, we require a timing signal in the hadronic calorimeter which is in-time with the collision within a window 55 ns wide for at least one tower in the cluster, and no evidence of a muon in the central muon systems within 30$^\circ$ in $\phi$ of the photon. The efficiency of requiring timing information rises with $E_T^\gamma$ from 78% at 55 GeV to over 98% above 100 GeV; the timing resolution for photons is on the order of 4 ns. The efficiency of requiring timing information rises with $E_T^\gamma$.

To remove the $W\gamma$ background as well as events in which mismeasurement of jet energy produces fake $E_T$, we require no jets [8] with $E_T > 15$ GeV, no jets with $E_T > 8$ GeV within 0.5 rad in $\phi$ of the photon, and no tracks in the event with $p_T > 5$ GeV.

Trigger and background considerations drive the choice of the $E_T^\gamma$ threshold. The Level 3 trigger becomes fully efficient (> 99%) at 55 GeV. In addition, below 45 GeV the background from $W \rightarrow e\nu$ with a misidentified electron is very large; as the $E_T^\gamma$ threshold is increased beyond the kinematic limit for electrons from $W$ decay at rest, the $W$ must recoil against another object, and the event is then rejected by the jet and track vetoes.

For an exclusive photon and invisible particle process, the overall efficiency for all cuts is found to vary from 0.45 at $E_T^\gamma = 55$ GeV to 0.56 for $E_T^\gamma > 100$ GeV, with a ±10% uncertainty. The cumulative effect of each cut is shown in Fig. 1. The number of events surviving the photon ID, $E_T$, cosmic ray rejection, and jet and track cuts are 15 046, 1475, 94, and 11, respectively. The largest measured difference between $E_T^\gamma$ and $E_T$ in the 11 events is 8.2 GeV and the mean value of $|E_T^\gamma - E_T|$ is 3.2 GeV, reflecting the detector’s good resolution for unclustered energy.

To estimate the number of cosmic ray events in the signal sample, we use the events which have a timing signal outside the in-time window but which pass all other cuts. We then extrapolate into the signal region, assuming a flat distribution in-time [15].

The Monte Carlo simulations of both signal processes and the $Z\gamma$, $W\gamma$, and prompt $\gamma\gamma$ backgrounds use the PYTHIA event generator [16] with the CTEQ5L parton distribution functions (PDFs) [17], followed by a parameterized simulation of the CDF detector. The simulations are then corrected for deficiencies in the detector model and the ±10% efficiency uncertainty applied. We turn off initial state radiation (ISR) to obtain leading-order (LO) cross sections and efficiencies. For the background processes, the resulting cross sections are corrected by the ratio of the LO cross section to the next-to-leading-order “zero-jet” cross section, obtained from theoretical calculations and Monte Carlo estimates. This allows the correct estimation of the acceptance $\times$ efficiency $\times$ cross section $(A\varepsilon\sigma)$ for the exclusive process. We obtain correction factors of 0.95 ± 0.3 for $Z\gamma$ [18], 0.9 ± 0.2 for $W\gamma$ [19], and 1.0 ± 0.3 for prompt $\gamma\gamma$ [20]; the systematic uncertainties considered are $Q^2$ choice and acceptance variations due to modeling of ISR in the Monte Carlo simulations. These uncertainties are added in quadrature with the efficiency uncertainty.

The background from $W \rightarrow e\nu$ arises either from hard bremsstrahlung by the electron before it enters the tracking chamber or inefficiency in the track reconstruction.

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**TABLE I.** Background sources. The uncertainty in the QCD background is unknown, and this background is not considered when setting limits. The numbers do not total due to rounding.

<table>
<thead>
<tr>
<th>Background Source</th>
<th>Events / 5 GeV</th>
<th>Uncertainty</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cosmic rays</td>
<td>6.3 ± 2.0</td>
<td></td>
</tr>
<tr>
<td>$Z\gamma \rightarrow \nu\bar{\nu}\gamma$</td>
<td>3.2 ± 1.0</td>
<td></td>
</tr>
<tr>
<td>$W \rightarrow e\nu$</td>
<td>0.9 ± 0.1</td>
<td></td>
</tr>
<tr>
<td>Prompt $\gamma\gamma$</td>
<td>0.4 ± 0.1</td>
<td></td>
</tr>
<tr>
<td>$W\gamma$</td>
<td>0.3 ± 0.1</td>
<td></td>
</tr>
<tr>
<td>Total non-QCD background</td>
<td>11.0 ± 2.2</td>
<td></td>
</tr>
<tr>
<td>QCD background</td>
<td>~1</td>
<td></td>
</tr>
<tr>
<td>Total observed</td>
<td>11</td>
<td></td>
</tr>
</tbody>
</table>

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**FIG. 1.** Photon $E_T$ spectrum after each stage of cuts.
As a radiated photon tends to be collinear with the electron, the \( E_T \) of the identified electromagnetic object will be close to the initial energy of the electron. We estimate the ratio \( P \) between the number of electrons faking photons and the number of electrons passing standard electron identification cuts [9] in the region \( |\eta^e| < 1 \), by assuming that “e\(\gamma\)” events with invariant masses within 10 GeV of the \( Z^0 \) mass are actually \( Z^0 \to ee \) events. We obtain \( P = (0.8 \pm 0.1)\% \). The background estimate is \( P \) times the number of \( W \to ev \) events that have \( |\eta^e| < 1, E_T^e > 55 \text{ GeV}, E_T^n > 45 \text{ GeV}, \) and pass the jet and track vetoes (discounting the electron track).

We have investigated QCD backgrounds which involve the mismeasurement of jet energy leading to apparent \( j_T, \) jet or misidentification of a jet as a photon. The most likely contributors to fakes are events with one high-energy object and many low-energy jets. With the \( E_T \), jet, and track requirements, these events are rare. To estimate these backgrounds one must use data; however, all control samples have small statistics and estimates range from 0.1 to 2 events. We take the conservative approach of not including this background source in the total background used in the limit calculations. This can only make the limits less stringent [21].

We study two hypothetical signal processes in detail. One is predicted by a supersymmetric model and the other by a model with large compact extra dimensions.

The first process (\( q\bar{q} \to G\bar{G}\gamma \)) is described in [22]. It presumes that the gravitino \( G \) is the lightest supersymmetric particle, with the other superpartners too heavy to produce at the Tevatron. Since the gravitino coupling is very small, being able to produce other supersymmetric particles increases the cross section; we therefore set an absolute lower limit on the gravitino mass \( m_{3/2} \) or, equivalently, the supersymmetry breaking scale \( |F|^{1/2} \) (the two are related by \( |F| = \sqrt{3} m_{3/2} M_p \), with \( M_p \) being the Planck mass). The cross section for this process scales as \( |F|^{-4} \); the kinematic distributions are independent of \( |F| \).

The second process (\( q\bar{q} \to \gamma G_{KK} \)) is described in [23]: \( n \) extra spatial dimensions are assumed to be compactified with radius \( R \). The fundamental mass scale \( M_D \) and \( R \) are related to \( n \) and Newton’s constant by \( G_N^{-1} = 8\pi R^n M_D^{1+n} \) [24]. The standard model fields propagate only on a \( 3 + 1 \) dimensional subspace, while gravitons propagate in the whole space. The graviton modes which propagate in the extra dimensions appear to four-dimensional observers as massive states of the graviton. A large value of \( R \) results in a large phase space for graviton production, canceling the weakness of the coupling to standard model fields. For a given \( n \), the cross section scales as \( 1/M_D^{4n+2} \); for fixed \( n \), the kinematic distributions are independent of \( M_D \).

Collisions at the Tevatron occur at sufficiently high values of the parton center-of-mass energies (\( \sqrt{s} \)) that we must consider the behavior of the differential cross section for collisions with \( \sqrt{s} \geq M_D \). We assume that the effective theory is valid for \( \sqrt{s} \ll 2M_D \). Our limits are sensitive to this choice as explained below.

The two signal processes are simulated with modified versions of PYTHIA. The \( q\bar{q} \to \gamma G\gamma \) process is simulated with \( |F|^{1/2} = 100 \text{ GeV} \), and the \( q\bar{q} \to \gamma G_{KK} \) process is simulated with \( M_D = 1 \text{ TeV} \) for \( n = 4, 6, \) and 8 extra dimensions.

We obtain estimates of three sources of theoretical systematic uncertainty in the cross section and acceptance predictions by varying \( Q^2 \) by a factor of 4 up and down, by using the GRV98 LO PDFs [25], and by turning the modeling of ISR on and off. The uncertainty due to ISR includes order-\( \alpha \) effects and acceptance changes due to the jet and track vetoes. For \( q\bar{q} \to GG\gamma \), the dominant uncertainty is the \( Q^2 \) choice (+26\%26), followed by ISR (±14\%) and PDF choice (±10\%). For \( q\bar{q} \to \gamma G_{KK} \), the dominant uncertainty comes from ISR (±34\%), followed by \( Q^2 \) choice (+16\%) and PDF choice (±8\%). The overall uncertainty in Aeff\( \sigma \) for the \( q\bar{q} \to \gamma G\gamma \) process, which includes the ±10\% efficiency uncertainty, is ±33\%. For \( q\bar{q} \to \gamma G_{KK} \), the corresponding figure is ±40\%.

The method we use to set limits is outlined in [26]. We find the following limits at 95% C.L.: for the supersymmetric model, \( |F|^{1/2} \geq 221 \text{ GeV} \) (equivalently, \( m_{3/2} \geq 1.17 \times 10^{-5} \text{ eV} \)); for large extra dimensions, \( M_D \geq 0.55, 0.58, \) and 0.60 TeV for \( n = 4, 6, \) and 8 extra dimensions (equivalently, \( R \leq 24 \text{ pm}, 55 \text{ fm}, \) and 2.6 fm, respectively). Similar limits on \( |F|^2 \) have previously been set in Refs. [4,27–30]; limits on \( M_D \) in the real graviton emission channel have been set in Refs. [27–30].

The kinematic region in \( E_T^\gamma \) and \( \sqrt{s} \) explored here is very different from that probed at LEP and the limits on \( M_D \) are more dependent on the behavior of the cross section for \( \sqrt{s} \geq M_D \). For illustration, we have evaluated the limits using the prescription of suppressing the cross section by a factor of \( M_D^4/\sqrt{s}^2 \) above \( M_D \) [31]. These limits are set without including the 40\% theoretical uncertainty. The limits decrease by between 0.01 and 0.05 TeV [32].

The results of this analysis can be presented in a “pseudo-model-independent” manner. In both the above models, the uncertainties in the predicted numbers of signal events have been dominated by theoretical factors. It can be useful to derive a limit which considers only the uncertainties in the detector simulation of the processes and so can easily be compared across models [10] (keeping in mind that such a limit is not a substitute for the rigorous extraction of a limit noting theoretical uncertainties). To obtain this limit, we compute a 95% C.L. upper limit on the number of events from new physics that would be detected, using only the ±10\% uncertainty in efficiency as the uncertainty in the Aeff\( \sigma \) for the new process. This limit is 9.8 events, which for this integrated luminosity corresponds to a cross section of 112 fb.
The plots in Fig. 2 allow a comparison of models to the $Ae\sigma$ limit. These curves are obtained by studying the acceptance and efficiency curves for simulated events and correcting for deficiencies in the detector simulation. These plots are valid for both the $\bar{G}G\gamma$ and $\gamma G_{KK}$ processes studied above, and for any process producing an exclusive photon and invisible particle signature. One can estimate $Ae\sigma$ for such a process by convolving the theoretical photon $\eta$ and $E_T$ spectra with the acceptance and efficiency curves.

In conclusion, we have performed a search for new physics in the exclusive $\gamma E_T$ channel. We have found no departure from the expected standard model cross section and have set limits on two specific models of new physics, one a supersymmetric model in which the photon is produced in association with two gravitinos, the second a model with large extra dimensions in which the photon is produced in association with a KK mode of the graviton. We have also presented the limit in a “pseudo-model-independent” manner.

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Estimates of backgrounds with small central values but large uncertainties are necessarily highly asymmetric, as a background cannot be less than zero. During the limit-setting procedure, this would produce artificially high limits.

This is in the convention of Giudice et al.; other authors replace $8\pi$ by other values.

The results are $M_D \geq 0.54, 0.55$, and $0.55$ TeV for $n = 4, 6$, and $8$, respectively.