Introduction	Echo effect	Examples and issues	Applications	EEHG at SLAC	Conclusion

Echo-Enabled Harmonic Generation for seeded FELs - theory and experiment

Gennady Stupakov SLAC NAL, Stanford, CA 94309

KEK Nov. 5, 2010

Introduction	Echo effect	Examples and issues	Applications	EEHG at SLAC	Conclusion
0000	000000000		0000	000000000	00
Outline o	f the talk				

- Introduction and motivation, HGHG seeding
- Echo effect in physics
- Echo-Enabled Harmonic Generation (EEHG)
- Some practical issues: ISR, CSR, leaking R_{51}
- EEHG for FELs
 - VUV-Soft X-ray FEL at LBNL
 - Attosecond pulse generation using EEHG
 - EEHG in LCLS-II
- EEHG experiment at SLAC
- Conclusion

 Introduction
 Echo effect
 Examples and issues
 Applications
 EEHG at SLAC
 Conclusion

 •ooo
 Conclusion
 oooo
 SLAC
 Conclusion
 oo
 <t



Introduction	Echo effect	Examples and issues	Applications	EEHG at SLAC	Conclusion
0●00	000000000		0000	000000000	00
Motivatio	on				

The SASE radiation starts from initial shot noise in the beam, with the resulting radiation having an excellent spatial coherence, but a rather poor temporal one.



There are several approaches to generation of longitudinally coherent FEL radiation based on seeding techniques

- High Harmonic Generation (HHG)
- High-Gain Harmonic Generation (HGHG)
- Echo-Enabled Harmonic Generation (EEHG)
- Self seeding

Introduction 00●0	Echo effect 000000000	Examples and issues	Applications	EEHG at SLAC	Conclusion 00
HGHG se	eding med	chanism			

HGHG modulates the FEL bunch current at a harmonic of the laser frequency.



The laser-beam interaction in the undulator, through the IFEL mechanism, generates energy modulation in the beam at the laser wavelength with some amplitude ΔE_{mod} . The laser power is proportional to ΔE_{mod}^2 .

	and high h	armonice			
0000	000000000	0000	0000	000000000	00
Introduction	Echo effect	Examples and issues	Applications	EEHG at SLAC	Conclusion

HGHG and high harmonics

HGHG phase space and current modulation for $A=\Delta E_{\rm mod}/\sigma_E=3$





In the limit of large k, the optimized bunching factor,

$$|\mathbf{b}_{k}| \approx \frac{0.68}{k^{1/3}} e^{-\frac{k^{2}}{2A^{2}}}$$

Large A deteriorates beam properties as a lasing medium, and requires a large laser energy. Several stages are necessary to get to x-ray wavelengths.

Introduction 0000	Echo effect ●00000000	Examples and issues	Applications 0000	EEHG at SLAC	Conclusion
Echo effe	ect - shad	low echo			

Echo effect can be observed in various media: photon echo, plasma echo, spin echo, etc. A simple illustration of the echo mechanism from the book by B.

Kadomtsev, "Collective phenomena in plasma".



We expect that echo develops in time, but in this example the role of time is played by the distance x.



Mask is illuminated by light source

A thin mask with periodic slits of period p = a + d is uniformly illuminated by light with angular spread σ_{θ} . Neglect diffraction and interference (small wavelength $\lambda \to 0$). The image is observed at the screen S.



Mask is illuminated by a light source



Rays begin to overlap at distance $z\sim d/\sigma_{\theta}$

If the distance $z\gg d/\sigma_{\theta},$ one sees a uniform illumination of the screen (Landau damping).

Chadau	acha				
	00000000				
Introduction	Echo effect	Examples and issues	Applications	EEHG at SLAC	Conclusion

Shadow echo

Add another screen with period p_2 at distance l from the first one $(l, z \gg d/\sigma_{\theta})$. Notation: $k_1 = 1/p_1$, $k_2 = 1/p_2$.



If the screen is at the right position, one can observe a pattern on the screen— *shadow echo*:

$$z = \frac{nk_1}{mk_2 - nk_1}l$$

 $k = |nk_1 - mk_2|$

where m and n are integers. The patten has period p (k = 1/p)

The animation shows the case $p_2 = \frac{1}{3}p_1$. For m, n = 1, echo should be observed at $z = \frac{1}{2}l$ with the period $p = \frac{1}{2}p_1$.

Introduction 0000	Echo effect 000●00000	Examples and issues	Applications 0000	EEHG at SLAC	Conclusion 00
Shadow	echo				

(Loading shadow echo movie)



EEHG (Stupakov, PRL, 2009): use a strong dispersion element in the first modulator and add one more modulator-chicane:



4 parameters: dimensionless energy modulations $A_1 = \Delta E_1 / \sigma_E$, $A_2 = \Delta E_2 / \sigma_E$, and dimensionless strengths of chicanes $B_1 = R_{56}^{(1)} \kappa_L \sigma_E / E_0$, and $B_2 = R_{56}^{(1)} \kappa_L \sigma_E / E_0$.

 Introduction
 Echo effect
 Examples and issues
 Applications
 EEHG at SLAC
 Conclusion

 0000
 0000
 0000
 0000
 0000
 0000
 0000
 0000

 Echo phase space evolution through the system
 0000
 0000
 0000
 0000
 0000

(Loading beam echo movie)

Introduction 0000	Echo effect 000000€00	Examples and issues	Applications 0000	EEHG at SLAC	Conclusion 00
1D echo	bunching	theory			

Echo generates the frequency $\omega=n\omega_1+m\omega_2$ (recall shadow echo).

A general expression for the bunching factor b_k (Xiang, Stupakov. PRST-AB, 2009). Practically, the case $\omega_1 = \omega_2 = \omega$ can be realized with a single laser beam.

$$I(z)/I_{0} = 1 + \sum_{k=1}^{\infty} 2b_{k} \cos(k\kappa_{L}z + \psi_{k})$$
$$b_{k} = \left| \sum_{m=-\infty}^{\infty} e^{im\phi} J_{-m-k} \left(A_{1}((m+k)B_{1} + kB_{2}) \right) \right.$$
$$\times J_{m} \left(kA_{2}B_{2} \right) e^{-\frac{1}{2}((m+k)B_{1} + kB_{2})^{2}} \right|$$

where ϕ is the phase between the laser beams 1 and 2. The maximized value of $|b_k|$ does not depend on ϕ (for $\omega_1 = \omega_2$)!





Echo excites a relatively narrow spectrum around the optimized harmonic.



What is the maximal echo modulation one can get for given amplitudes A_1 , A_2 and optimized dispersions?



In contrast to HG, there is no exponential suppression factor for large k! The amplitude A_1 may not be large, but the optimized strength $B_1 \propto k$.



Beam parameters for the FERMI@ELETTRA project: the beam energy $E_0=1.2$ GeV, the beam energy spread $\sigma_E=150$ keV and the laser wavelength is 0.24 micron.

Numerical examples

k	λ_r , nm	A ₁	A ₂	$R_{56}^{(1)}$, mm	$R^{(2)}_{56}$, mm	$ b_k $
24	10	3	1	8.2	0.35	0.11
48	5	3	2	8.1	0.16	0.09
24	10	3	3	2.5	0.12	0.11

Introduction	Echo effect	Examples and issues	Applications	EEHG at SLAC	Conclusion
0000	000000000	0●00	0000		00
Physics is	sues with	EEHG			

- Energy diffusion due to incoherent synchrotron radiation in chicanes
- CSR and associated microbunching instability
- Lattice nonlinearities and emittance effects—simulations with elegant
- \bullet Tolerances on magnetic field (leaking $R_{51})$ $\Delta B/B\approx 10^{-3}$
- \bullet Finite laser beam size: $\sigma_{L\perp} > 4 \sigma_{B\perp}$
- Energy chirp in the beam

These issued are addressed in: D. Xiang and G. Stupakov, PRST-AB, 030702 (2009); Z. Huang, D. Ratner, G. Stupakov, D. Xiang, SLAC-PUB-13547 (2009); D. Xiang and G. Stupakov, SLAC-PUB-13644, (2009); PAC09, FEL09, IPAC10.



Large value of $R_{56}^{(1)}$ generates a fine structure over the energy. For $\lambda_r=10$ nm case the width of the modulation is $\sim 0.2\sigma_E\sim 30$ KeV. The scaling is $\Delta E\sim \sigma_E/k.$



The incoherent energy spread after passing a dipole

$$\Delta \sigma_{E} = 6.4~{\rm KeV} \times \sqrt{\frac{L\left({\rm m}\right)}{\left[\rho\left({\rm m}\right)\right]^{3}}} \left[E\left({\rm GeV}\right)\right]^{7/2}$$

can be a fraction of keV. Choosing larger bending radius in the chicane would decrease $\Delta\sigma_{E}.$



As the beam travels through the chicanes, it senses variable $R_{56}.$ In combination with the energy modulation, in 1D, this will generate undesirable microbunching inside the dipoles of the dispersion sections. The microbunching would result in CSR and uncontrolled energy modulation of the beam. Fortunately, this modulation is suppressed due to R_{51} and $R_{52}.$

The suppression factor due to R_{51} :

$$\sim \exp\left(-k_{
m mod}^2R_{51}^2\sigma_x^2/2
ight)$$



 R_{51} in the second chicane. For $\sigma_x=40~\mu m$ and $R_{51}\sim 0.01$, microbunching with $\lambda_{mod}<1~\mu m$ will be smeared out.

Echo effect Examples and issues Applications EEHG at SLAC 0000

LBNL soft x-ray FEL with EEHG

Main parameters: Beam energy 2.4 GeV Energy spread: 100 keV Emittance: 0.7 mm mrad Peak current: 1 kA



The beam distribution is obtained from IMPACT-Z simulation by J. Qiang.





Radiation at 3.8 nm (50th harmonic of 190 nm laser). The spectrum is close to the Fourier limit.



Simulations were carried out with GENESIS.



Adding a chirp element to the system results in additional compression of the microbunching (Xiang, Huang, Stupakov. PRST-AB, 2009). The chirp is provided by a short long-wavelength (800 nm) laser pulse. The echo generates 20th harmonic which is further compressed by a factor of 10.



Zholents and Penn (NIM, 2009) proposed to use echo to generate two attosecond pulses, 2.27 nm and 3.03 nm, from the laser wavelength 200 nm and 800 nm.

Introduction 0000	Echo effect 000000000	Examples and issues	Applications	EEHG at SLAC 000000000	Conclusion
FFGH fo	or I CLS-I				

Electron beam energy	4.3 GeV
Peak current	800 A
Normalized emittance	0.6 µm
Slice energy spread	700 keV
Seed laser wavelength	202 nm
Seed laser power	300 MW
$N_p \times \lambda_u$	$8 \times 35 \text{cm}$
R_{56} for C1	4.4 mm
R ₅₆ for C2	109 µm

EEHG FEL power is about 8 GW after 18 m of the undulator.





A proof-of-principe experiment to demonstrate EEHG has been carried out at SLAC at the NLCTA facility (PRL, **105**, 114801 (2010)). 3/2009 - first planning, 7/2010 - first echo signal. NLCTA is equipped with an S-band injector (to ~ 100 pC), an X-band linac (60 - 200 MeV) and Ti:Sapphire laser systems.



Layout of the ECHO-7 at the NLCTA.

 Introduction
 Echo effect
 Examples and issues
 Applications
 EEHG at SLAC
 Conclusion

 0000
 0000
 0000
 0000
 0000
 0000
 0000

Echo experiment at NLCTA at SLAC

The parameters of the experiment:

Electron beam energy	120 MeV
Bunch length	0.5-2.5 ps
Bunch charge	20-40 pC
Normalized emittance	$\sim 8\mu m$
Slice energy spread	$\sim 1 \text{keV}$
First laser wavelength	795 nm
Second laser wavelength	1590 nm
$N_p imes \lambda_u$ for U1	$10{\times}3.3\text{cm}$
$N_p \times \lambda_u$ for U2	$10{ imes}5.5\text{cm}$
$N_p \times \lambda_u$ for U3	$10{ imes}2.0\text{cm}$
Peak energy modulation in U1 and U2	10-40 keV
R ₅₆ for C1 and C2	1-9 mm

Introd	
0000	

Echo effect 000000000 Examples and issues

Application

EEHG at SLAC

Conclusion 00

Upstream view



Introduction 0000 Echo effect 000000000 Examples and issues

Application

EEHG at SLAC

Conclusion

Chicanes and undulators in the NLCTA









27/34

Fynerime	ntal chal	lenges			
Introduction 0000	Echo effect 000000000	Examples and issues	Applications 0000	EEHG at SLAC	Conclusion 00

The main challenge in this experiment was that the beam energy spread was small (in contrast to a real FEL), and the amplitude of the energy modulation due to interaction with the laser was large (this was required in order to keep the chicane strength reasonable). In this situation, both HGHG and EEHG generate high harmonics. Different laser wavelengths help to partially separate HGHG from EEHG.

Introduction	Echo effect	Examples and issues	Applications	EEHG at SLAC	Conclusion
0000	000000000		0000	0000000000	00
First echo	o signal				

ECHO signals, no energy chirp: a) only 1590 nm laser is on, b) only 795 nm laser is on, c) both lasers are on.



ECHO signals when beam has energy chirp $\sim 33.4 \text{ m}^{-1}$.



To fully separate HGHG and EEHG, we introduced energy chirp h in the beam.

$$\omega = \frac{n\omega_1 + (1 + hR_{56}^{(1)})m\omega_2}{1 + h(R_{56}^{(1)} + R_{56}^{(2)})}$$

Compari	con with	cimulations			
Introduction	Echo effect	Examples and issues	Applications	EEHG at SLAC	Conclusion
0000	000000000		0000	000000000	00



	ogth vorcu	s oporov chirr	2		
0000	000000000	0000	0000	00000000	00
Introduction	Echo effect	Examples and issues	Applications	EEHG at SLAC	Conclusion





Introduction 0000	Echo effect 000000000	Examples and issues	Applications 0000	EEHG at SLAC	Conclusion ●○
EEHG pro	omise - I				

Echo Enabled Harmonic Generation (EEHG) seems promising for generation of harmonics up to 40-100. The harmonic amplitude scales as $\sim n^{-1/3}$. With the seed laser wavelength of about 200 nm, one can achieve seeding of soft x-ray FELs. Typical parameters

Electron beam energy	1-2 GeV
Energy spread	100-200 keV
Laser wavelength	200 nm
Harmonic number	20-100
FEL wavelength	a few nm

Several soft xray FEL projects in the world can benefit from the EEHG: FERMI@ELETTRA (Trieste, Italy), SwissFEL (PSI, Switzerland), SDUV-FEL (Shanghai, China), LBNL FEL (USA), LCLS-II

Introduction	Echo effect	Examples and issues	Applications	EEHG at SLAC	Conclusion
0000	000000000		0000	000000000	○●
EEHG pro	omise - II				

Further development of the echo idea:

• J. Wurtele: using echo oscillator (FEL 2010).



 D. Ratner and A. Chao: steady state microbunching in storage ring (PRL, 105, 154801, (2010)).



34/34