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# Meson-pair production processes from two-photon collisions at Belle

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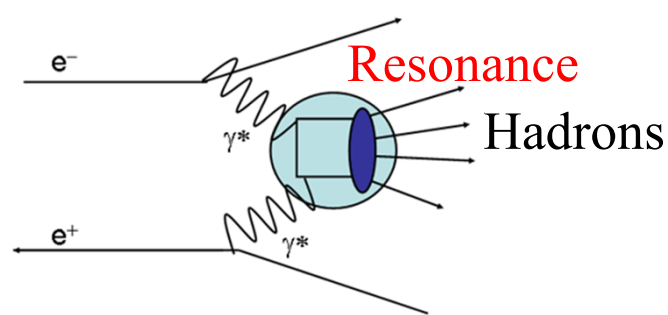
Sadaharu Uehara (KEK)  
Belle Collaboration



*Workshop on hadron tomography at J-PARC and KEKB  
Jan. 6, 2017*

# Resonance production and quantum numbers

## Resonance formation from two photon collisions



$Q = 0$ ,  $C = +$ ,

for **real-photon** collisions

$J^P = 0^+, 0^-, 2^+, 2^-, 3^+, 4^+, 4^-, 5^+ \dots$  **(even) $^\pm$ , (odd  $\neq 1$ ) $^+$**

**Pseudoscalar-meson pair production:**  $J^P = (\text{even})^+$  only

Strict constraints for quantum numbers  $\rightarrow$  **Determination of  $J^P$  by PWA**

$\Gamma_{\gamma\gamma}$ : The cross section is proportional to the two-photon partial decay width of the resonance, useful information to explore **meson's internal structure**

**Decay properties** of the resonance

Searches/Discoveries of **new resonances**

Isospin mixing, **Form factors**, **Test of QCD**



# KEKB Accelerator and Belle Detector

- Asymmetric  $e^- e^+$  collider  
8 GeV  $e^-$  (HER) x 3.5 GeV  $e^+$  (LER)

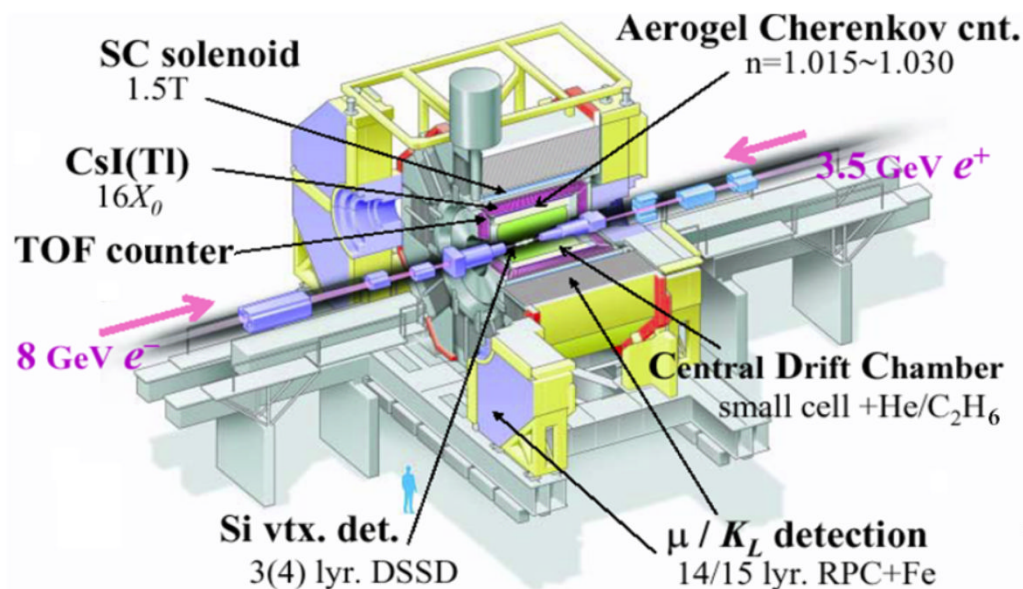
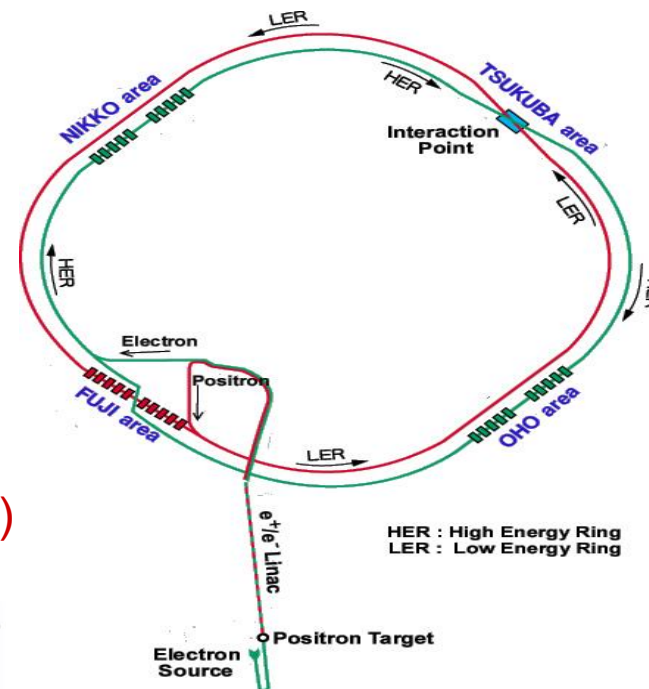
$\sqrt{s}$  = around 10.58 GeV  $\Leftrightarrow \Upsilon(4S)$

Beam crossing angle: 22mrad

- World-highest Luminosity

$$L_{\max} = 2.1 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$$

$$\int L dt \sim 1040 \text{ fb}^{-1} \text{ (Completed in Jun. 2010)}$$



High momentum/energy resolutions

CDC+Solenoid, CsI

Vertex measurement – Si strips


Particle identification

TOF, Aerogel, CDC-dE/dx,

RPC for  $K_L$ /muon

# “ $\gamma\gamma \rightarrow$ Pseudoscalar-meson pair” from Belle

10 papers for 6 processes

Process	Reference		Int.Lum. (fb <sup>-1</sup> )	$\gamma\gamma$ c.m. Energy (GeV)	Light Mesons	QCD	Char- monia
$\pi^+\pi^-$	PLB 615, 39 (2005) PRD 75, 051101(R) (2007) J. Phys. Soc. Jpn. 76, 074102 (2007)		87.7 85.9 85.9	2.4 - 4.1 0.8 - 1.5 0.8 - 1.5	$\checkmark$ $\checkmark$	$\checkmark$	$\checkmark$
$K^+K^-$	EPJC 32, 323 (2003) PLB 615, 39 (2005)		67 87.7	1.4 - 2.4 2.4 - 4.1	$\checkmark$	$\checkmark$	$\checkmark$
$\pi^0\pi^0$	PRD 78, 052004 (2008) PRD 79, 052009 (2009)		95 223	0.6 - 4.0 0.6 - 4.0	$\checkmark$ $\checkmark$	$\checkmark$	$\checkmark$
$K_S^0 K_S^0$	PLB 651, 15 (2007) PTEP 2013, 123C01 (2013)		397.1 972	2.4 - 4.0 1.05 - 4.0	$\checkmark$	$\checkmark$ $\checkmark$	$\checkmark$ $\checkmark$
$\eta\pi^0$	PRD 80, 032001 (2009)		223	0.84 - 4.0	$\checkmark$	$\checkmark$	
$\eta\eta$	PRD 82, 114031 (2010)		393	1.1 - 3.8	$\checkmark$	$\checkmark$	$\checkmark$

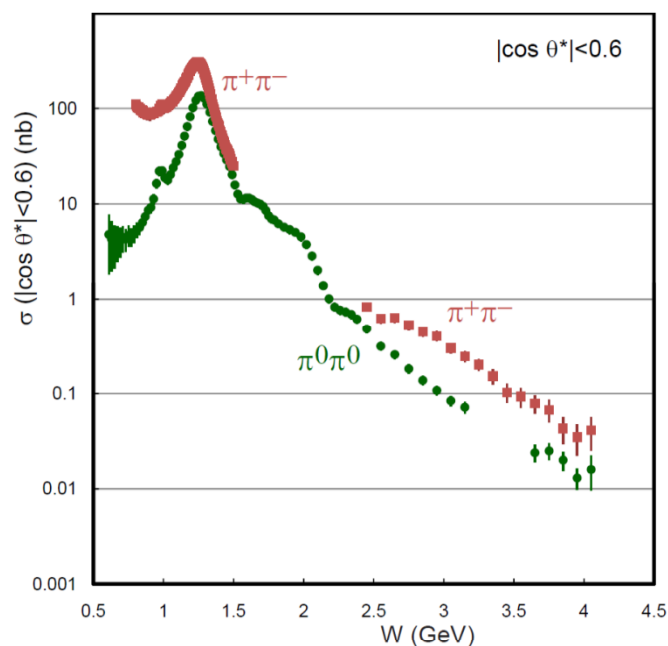
Differential cross section  $d\sigma/d|\cos\theta^*|$  for these processes are measured.





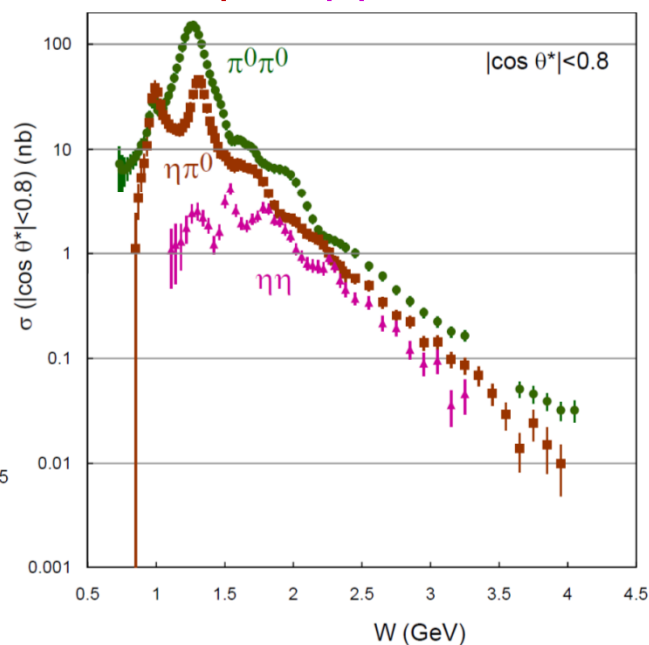
# The six processes; in total ~20 peaks

## Charged vs Neutral $\pi\pi$

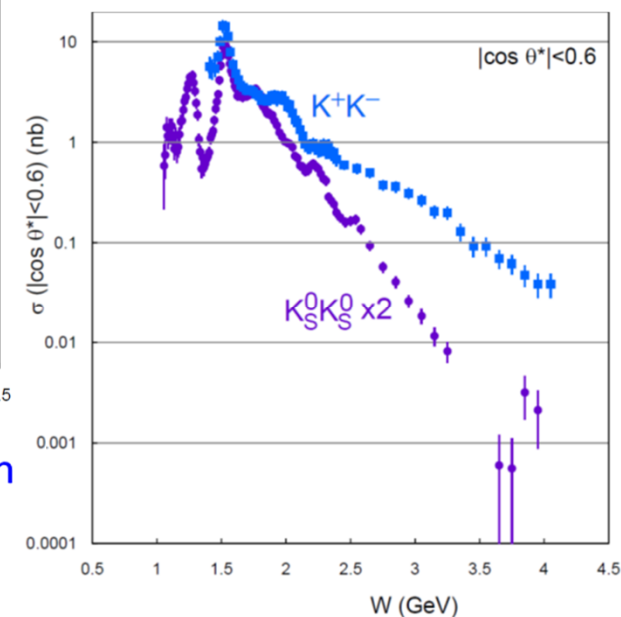


## Three neutral-pair processes

$\pi^0\pi^0$ ,  $\eta\pi^0$ ,  $\eta\eta$



## Charged vs Neutral $K\bar{K}$



Horizontal axis:

$W$  --  $\gamma\gamma$  c.m. energy = invariant mass of the two-meson system

$W < \sim 2.5$  GeV: Dominated by resonances

$W > \sim 2.5$  GeV: (Netnegative) Power law works + ( $\chi_c$  charmonia)



# Formalism of PWA for P-meson pair final-state processes

- We consider up to  $J=4$  (for  $W < 3$  GeV).

$$\frac{d\sigma}{d\Omega} = \left| S Y_0^0 + D_0 Y_2^0 + G_0 Y_4^0 \right|^2 + \left| D_2 Y_2^2 + G_2 Y_4^2 \right|^2$$

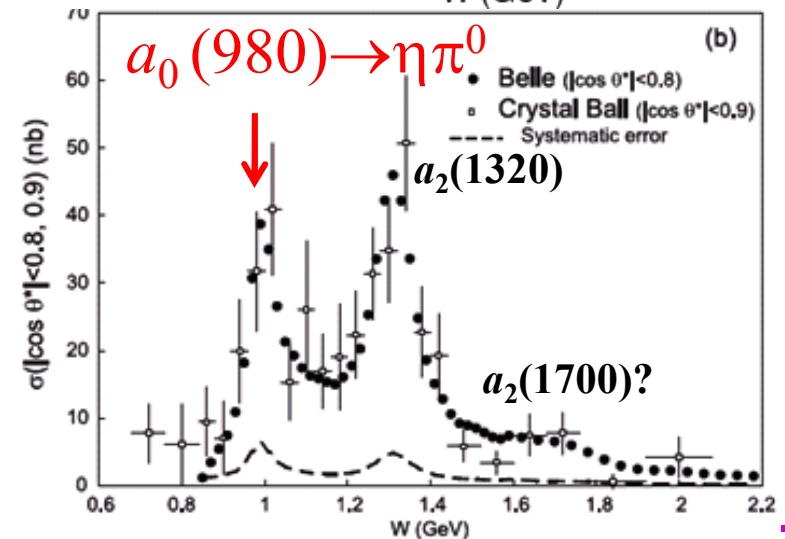
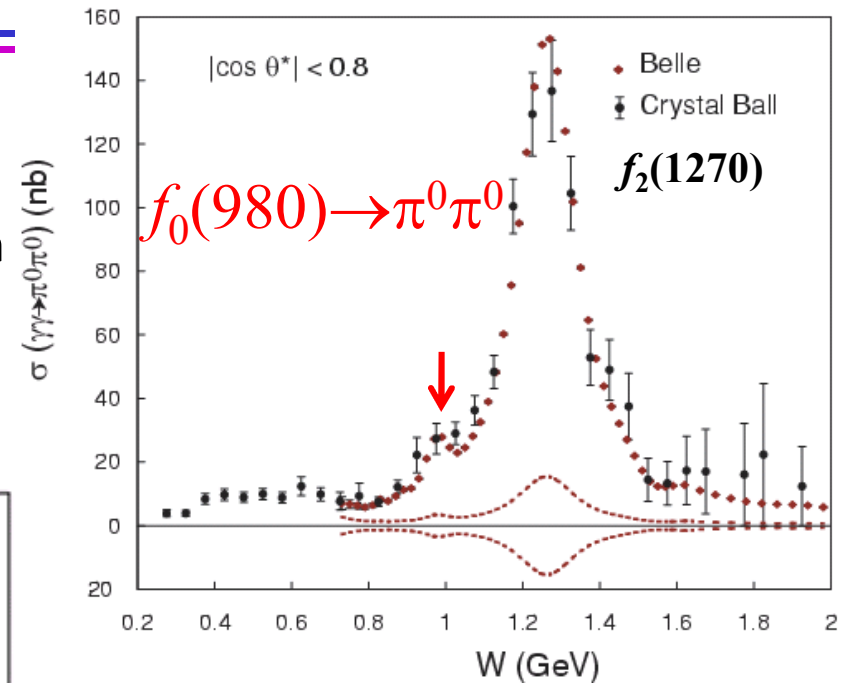
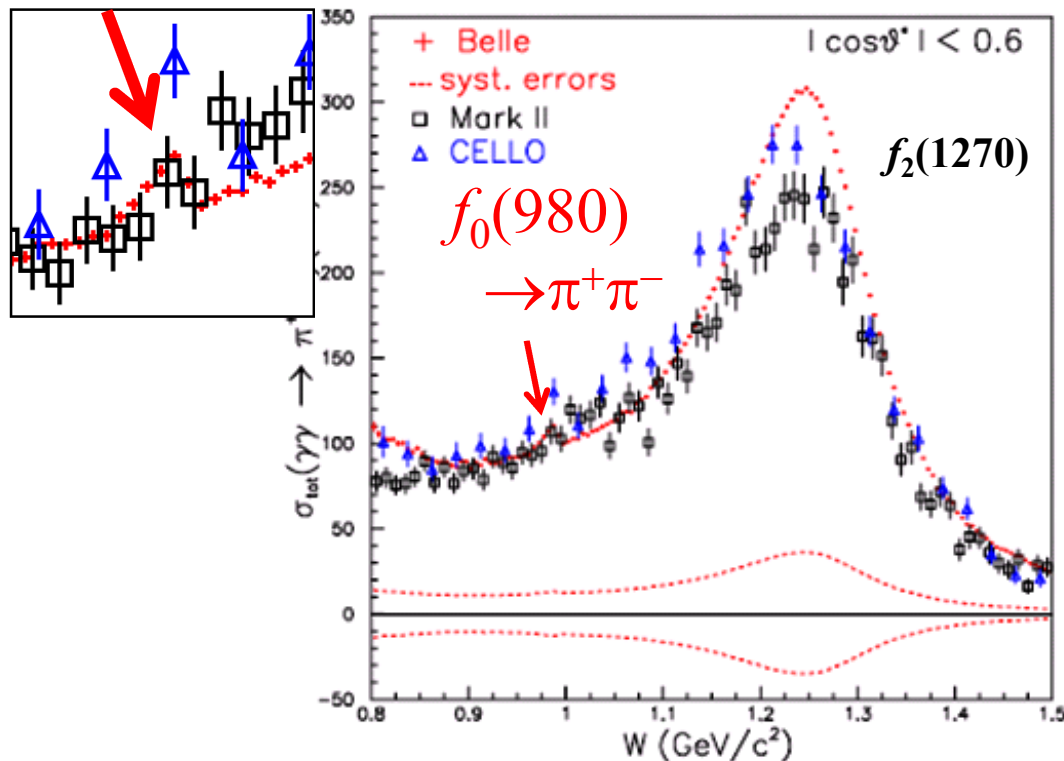
- $S, D_0, G_0, D_2, G_2$  Partial-wave amplitudes for each wave  $J_\lambda$   
 $J = L = 0, 2, 4$  (even only) with the helicity  $\lambda = 0$  or  $2$  (to the  $\gamma\gamma$  axis)
  - $Y_J^\lambda$  : spherical harmonics
  - $|Y_J^\lambda|$  are NOT mutually independent, as we have no information for the azimuthal-angle direction.
- We cannot determine the partial waves model independently;  
We need **parameterization based on a model** including the  $W$  dependence of resonances and continuum components.
- Ancillary model-independent way: **Hat amplitudes**;  $|Y_J^m|^2$  mutually independent

$$\frac{d\sigma}{d\Omega} = \hat{S}^2 |Y_0^0|^2 + \hat{D}_0^2 |Y_2^0|^2 + \hat{G}_0^2 |Y_4^0|^2 + \hat{D}_2^2 |Y_2^2|^2 + \hat{G}_2^2 |Y_4^2|^2$$



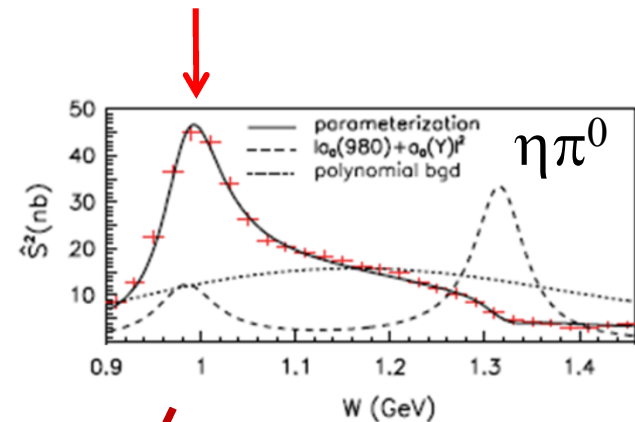
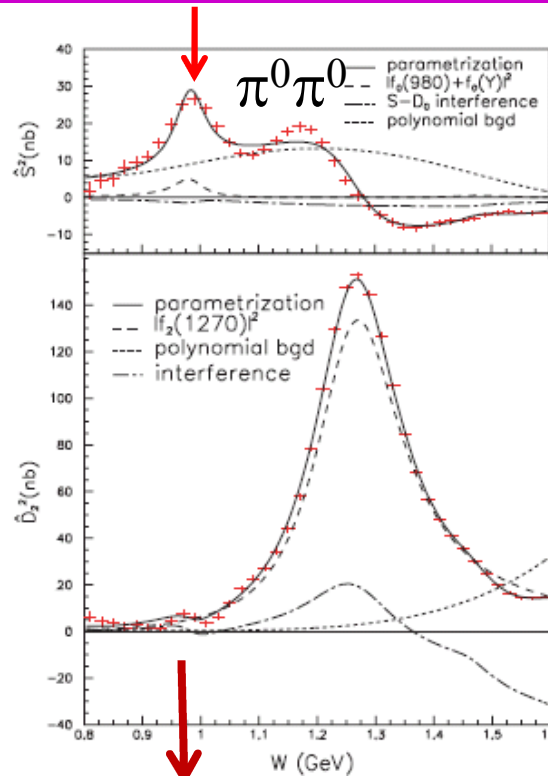
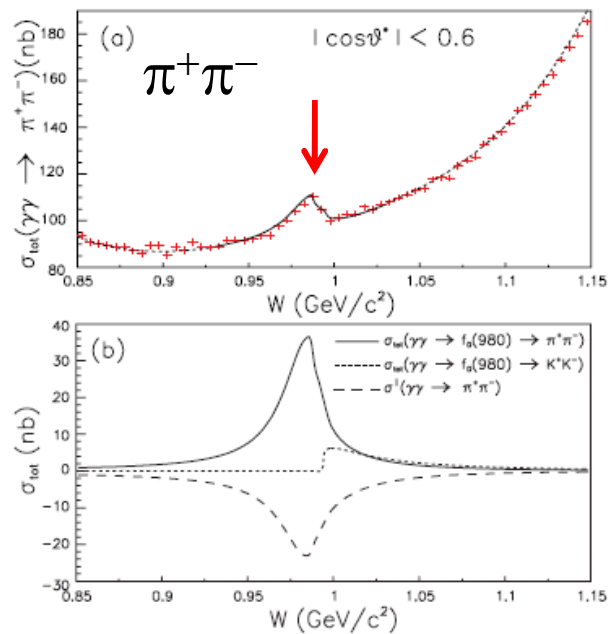
# Confirmations of $f_0(980)$ and $a_0(980)$ formations

$f_0(980)$  and  $a_0(980)$  :  
Observed as a peak very clearly in two-photon  
production, for the first time.



S. Uehara, KEK, Jan. 2011

# Two-photon decay width of $f_0(980)$ and $a_0(980)$



Predictions for  $f_0(980)$

Meson	$f_0(980)$	$f_0(980)$	$a_0(980)$
$M[\text{MeV}/c^2]$	$985.6^{+1.2+1.1}_{-1.5-1.6}$	$982.2 \pm 1.0^{+8.1}_{-8.0}$	$982.3^{+0.6+3.1}_{-0.7-4.7}$
$\Gamma_{\pi\pi/\text{tot}}[\text{MeV}]$	$51.3^{+20.9+13.2}_{-17.7-3.8}$	$66.9^{+13.9+8.8}_{-11.8-2.5}$	$75.6 \pm 1.6^{+17.4}_{-10.0}$
$\Gamma_{\gamma\gamma}[\text{eV}]$	$205^{+95+147}_{-83-117}$	$286 \pm 17^{+211}_{-70}$	$128^{+3+502}_{-2-43} / \mathcal{B}_{\pi^0\eta}$

Model	$\Gamma_{\gamma\gamma}[\text{eV}]$
$u\bar{u}, d\bar{d}$	1300 – 1800
$s\bar{s}$	300 – 500
<b><math>K\bar{K}</math> molecule</b>	200 – 600
<b>Four-quark</b>	270

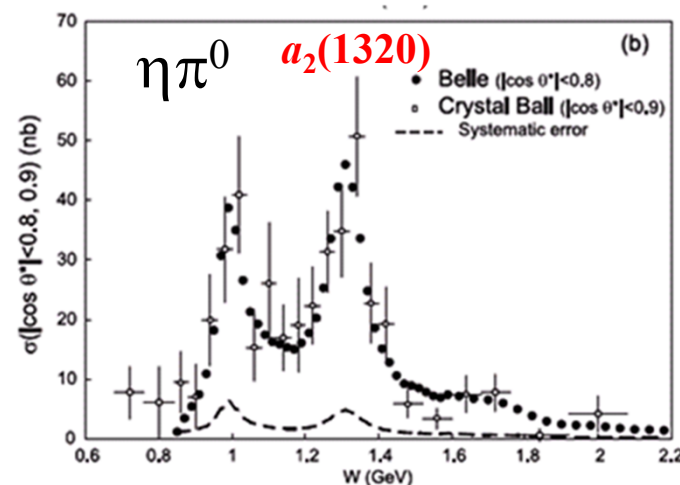
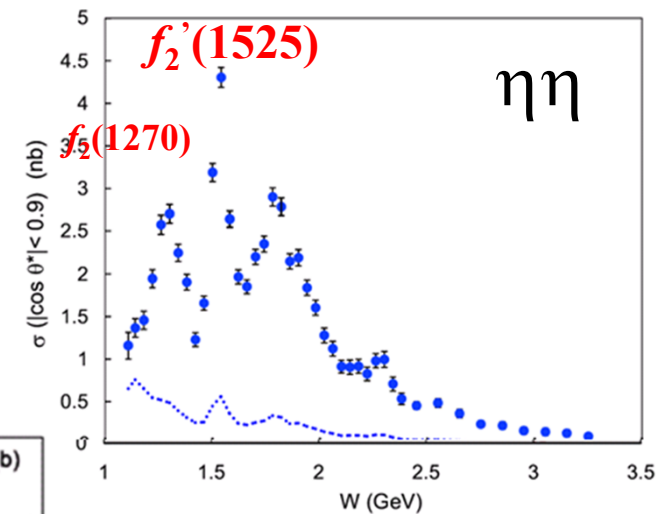
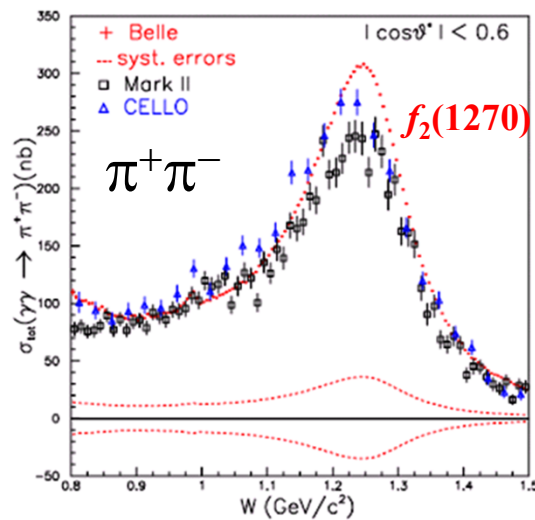


# The tensor-meson triplet, $f_2(1270)$ , $a_2(1320)$ , $f_2'(1525)$

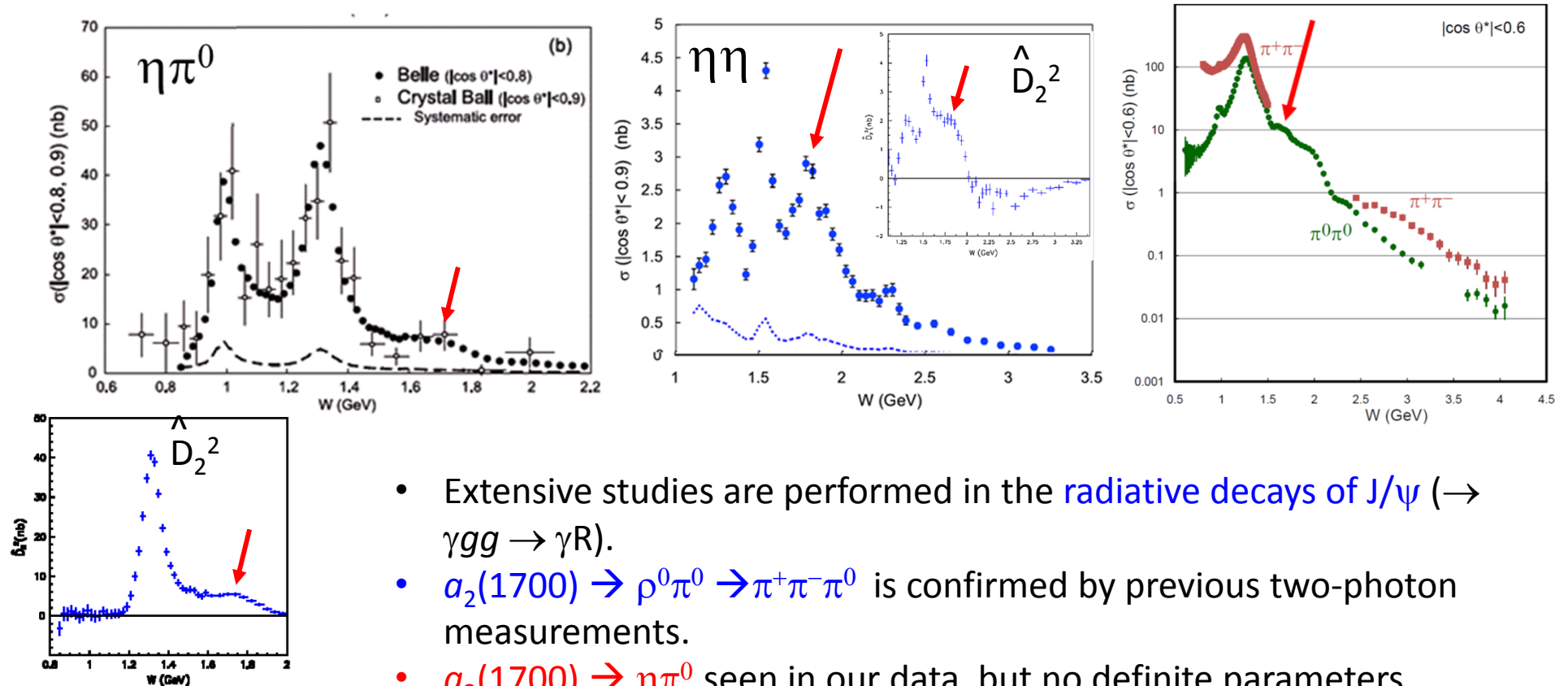
$f_2(1270)$ : The largest peak in  $\pi^+\pi^-$  and  $\pi^0\pi^0$ . Also seen in  $\eta\eta$

$a_2(1320)$ : Large peak in  $\eta\pi^0$

$f_2'(1525)$ : Large peak in  $\eta\eta$ ,  $K^+K^-$ , and  $K_S^0 K_S^0$



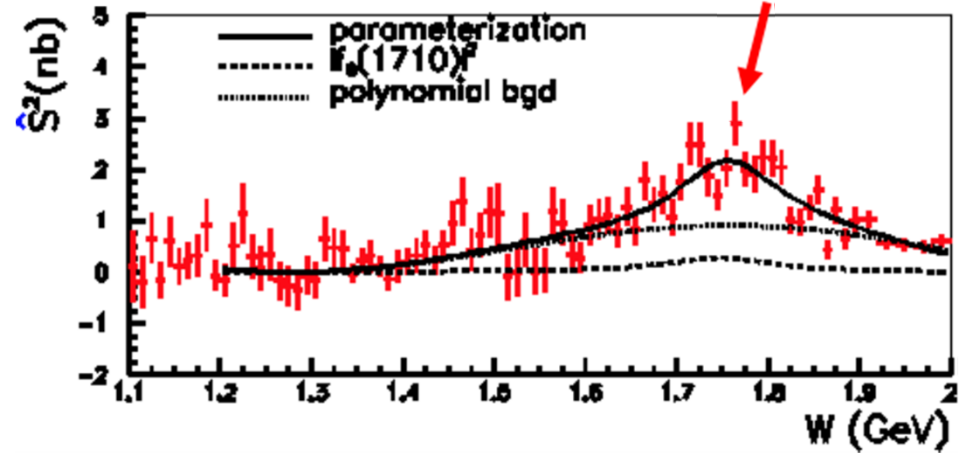
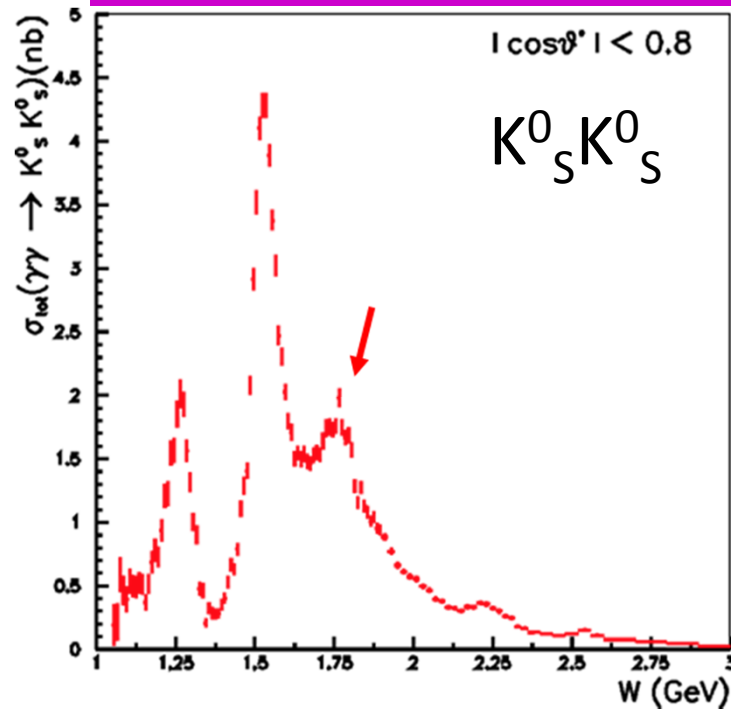
# 1.6 – 1.8 GeV: Mass region of the greatest difficulty



- Extensive studies are performed in the **radiative decays of  $J/\psi$**  ( $\rightarrow \gamma g g \rightarrow \gamma R$ ).
- $a_2(1700) \rightarrow \rho^0 \pi^0 \rightarrow \pi^+ \pi^- \pi^0$  is confirmed by previous two-photon measurements.
- $a_2(1700) \rightarrow \eta \pi^0$  seen in our data, but no definite parameters obtained.
- $f_2(1810) \rightarrow \eta \eta$  is confirmed in two-photon process.
- **An unidentified structure around  $\sim 1.6$  GeV is seen in  $\pi^0 \pi^0$ .** But, its correspondence to a single resonance of the mass is not sure.



# $f_0(1710)$ formation in $K_S^0 K_S^0$



Assuming a single resonance,  
 $J = 0$  or  $2$  ?  $J = 0$  is much preferred.

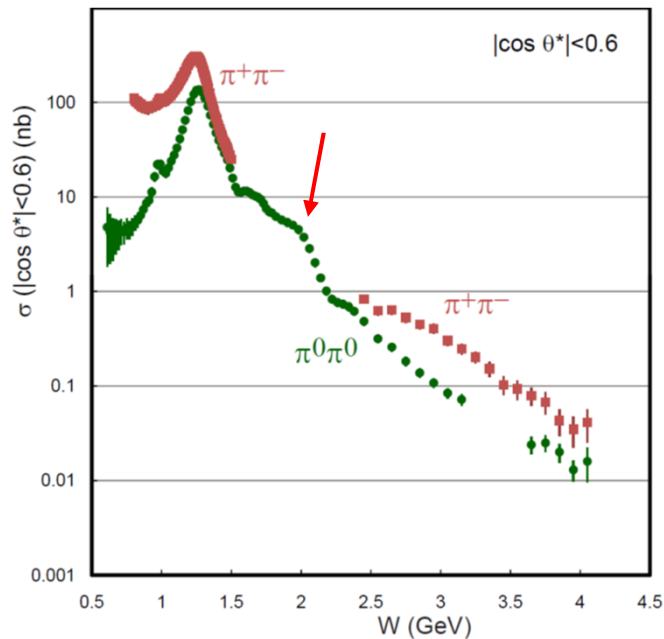
Parameter $f_J(1710)$	$f_0(1710)$ fit				$f_2(1710)$ fit	
	fit-H	fit-L	H,L combined	PDG	fit-H	fit-L
$\chi^2/ndf$	694.2/585	701.6/585	Two solutions of interference		796.3/585	831.5/585
Mass( $f_J$ ) (MeV/ $c^2$ )	$1750^{+5+29}_{-6-18}$	$1749^{+5+31}_{-6-42}$	$1750^{+6+29}_{-7-18}$	$1720 \pm 6$	$1750^{+6}_{-7}$	$1729^{+6}_{-7}$
$\Gamma_{\text{tot}}(f_J)$ (MeV)	$138^{+12+96}_{-11-50}$	$145^{+11+31}_{-10-54}$	$139^{+11+96}_{-12-50}$	$135 \pm 6$	$132^{+12}_{-11}$	$150 \pm 10$
$\Gamma_{\gamma\gamma} \mathcal{B}(K\bar{K})_{f_J}$ (eV)	$12^{+3+227}_{-2-8}$	$21^{+6+38}_{-4-26}$	$12^{+3+227}_{-2-8}$	unknown	$2.1^{+0.5}_{-0.3}$	$1.6 \pm 0.2$

$f_0(1710) \rightarrow K_S^0 K_S^0$  is confirmed in two-photon process.



# The 1.8 – 2.2 GeV region

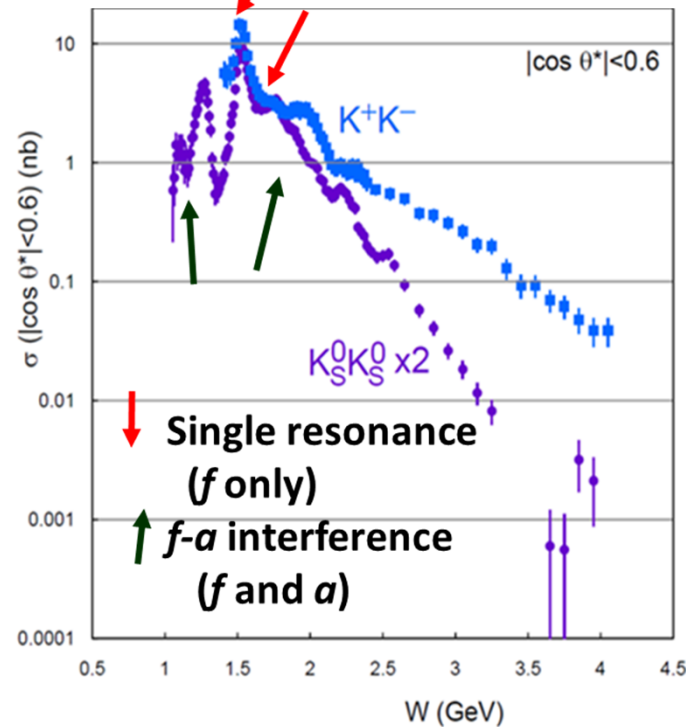
- $f_2(1950) \rightarrow \pi^0\pi^0$  shows a broad structure
- Similar structure exists in  $K^+K^-$  (but, they can be different states)
- No peak in  $\eta\pi^0$ ,  $\eta\eta$  and  $K_S^0 K_S^0$  in this mass region



Parameter	$f_4(2050)$	" $f_2(1950)$ "	Unit
Mass	$1885^{+14}_{-13} {}^{+218}_{-25}$	$2038^{+13}_{-11} {}^{+12}_{-73}$	MeV/ $c^2$
$\Gamma_{\text{tot}}$	$453 \pm 20 {}^{+31}_{-129}$	$441^{+27}_{-25} {}^{+28}_{-192}$	MeV
$\Gamma_{\gamma\gamma} \mathcal{B}(\pi^0\pi^0)$	$7.7^{+1.2}_{-1.1} {}^{+23.5}_{-5.2}$	$54^{+23}_{-14} {}^{+379}_{-68}$	eV

$\chi^2(ndf)$  323.2 (311)

$I=0$  ( $f$ ) and  $I=1$  ( $a$ ) interference in  $K\bar{K}$



S.Uehara, KEK, Jan. 2017





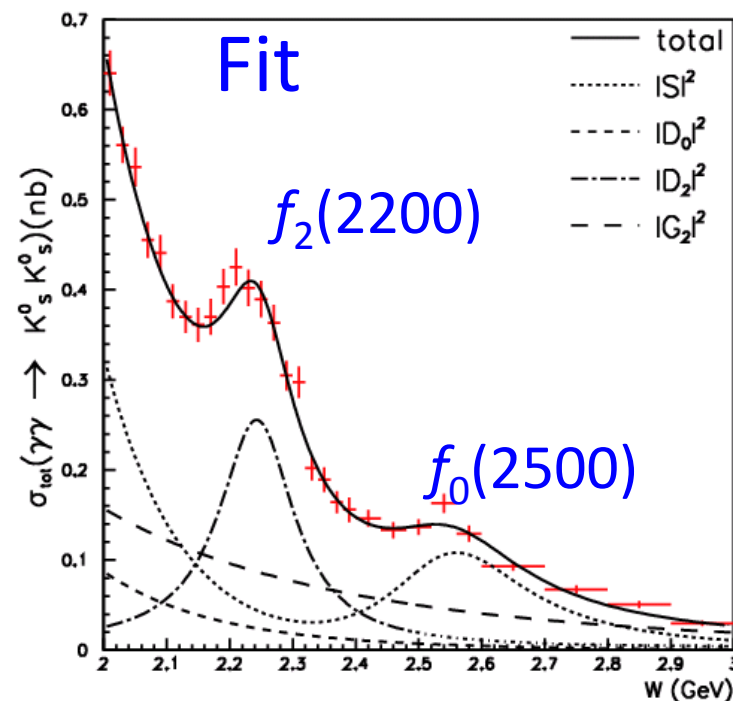
# Fit Results for resonances in $K^0_s K^0_s$

$f_2(2200)-f_0(2500)$  is the best solution (in all the J= 0, 2, 4 combinations)

Parameter	$f_2(2200)$	$f_0(2500)$
Mass (MeV/ $c^2$ )	$2243^{+7+3}_{-6-29}$	$2539 \pm 14^{+38}_{-14}$
$\Gamma_{\text{tot}}$ (MeV)	$145 \pm 12^{+27}_{-34}$	$274^{+77+126}_{-61-163}$
$\Gamma_{\gamma\gamma} \mathcal{B}(K\bar{K})$ (eV)	$3.2^{+0.5+1.3}_{-0.4-2.2}$	$40^{+9+17}_{-7-40}$

## Significances

- $3.4\sigma$  for  $f_2(2200)$  over  $f_0(2200)$
- $4.3\sigma$  for  $f_0(2500)$  over  $f_2(2500)$

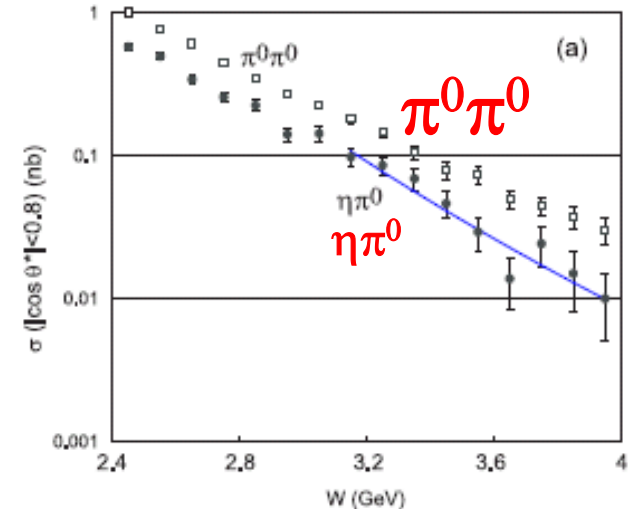
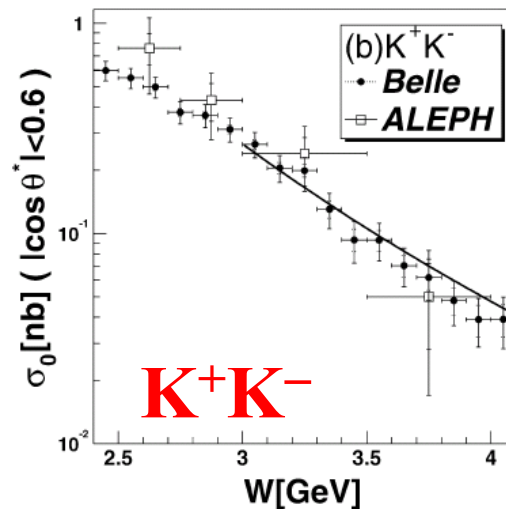
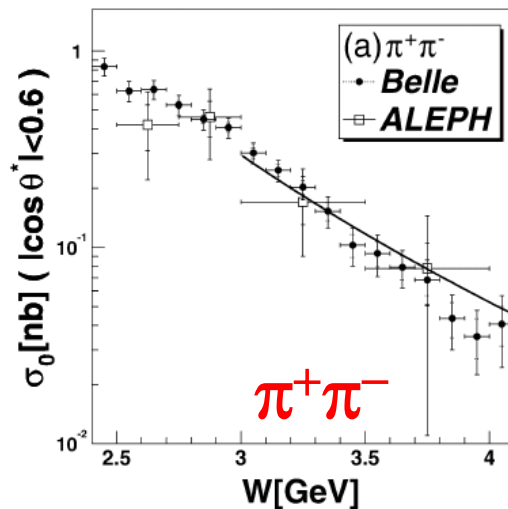


- There can be an only wide state around 2240 MeV.
- Narrow appearances in previous measurements may be due to an interference effect and/or statistical fluctuation.
- A high-mass state at 2.5 GeV may be the heaviest light-quark scalar meson so far found.



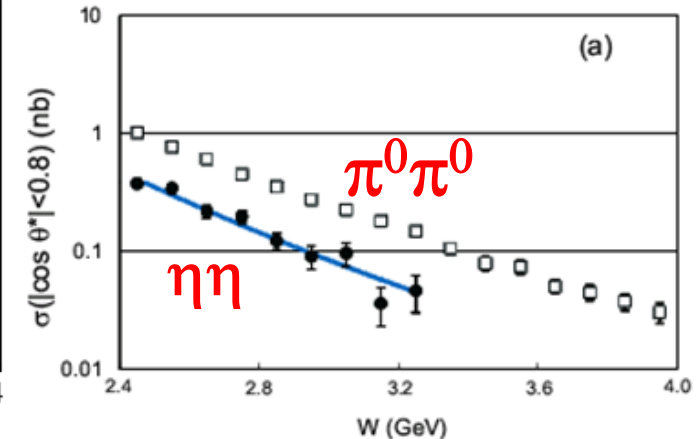
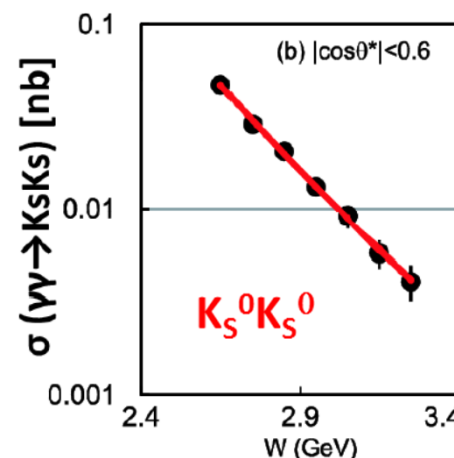
# W-dependences at high energies

Assume or expect  $\sigma(W) \sim W^{-n}$



Fitted and reproduced  
Slope parameter  $n$  different  
among the reactions

Charmonium contributions  
not included/removed



# Cross sections and their ratios

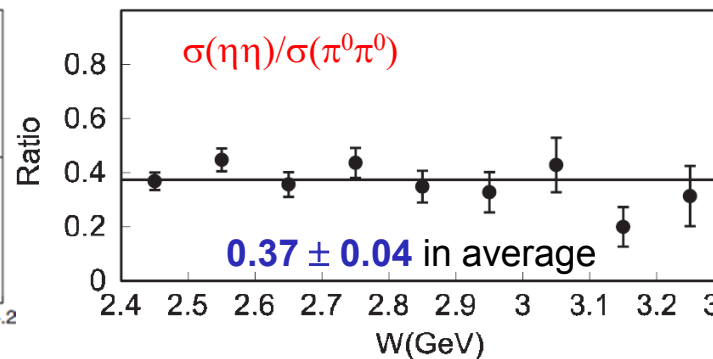
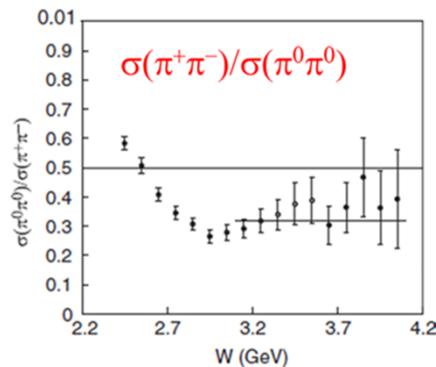
Process	$n$	$W(\text{GeV})$	$ \cos \theta^* $	BL	BC	DKV
$K_S^0 K_S^0$	$11.0 \pm 0.4 \pm 0.4$	$2.4 - 4.0^\dagger$	$< 0.8$		10	
$\pi^+ \pi^-$	$7.9 \pm 0.4 \pm 1.5$	$3.0 - 4.1$	$< 0.6$	6	6	
$K^+ K^-$	$7.3 \pm 0.3 \pm 1.5$	$3.0 - 4.1$	$< 0.6$	6	6	
$\pi^0 \pi^0$	$8.0 \pm 0.5 \pm 0.4$	$3.1 - 4.1^\dagger$	$< 0.8$		10	
$\eta \pi^0$	$10.5 \pm 1.2 \pm 0.5$	$3.1 - 4.1$	$< 0.8$		10	
$\eta \eta$	$7.8 \pm 0.6 \pm 0.4$	$2.4 - 3.3$	$< 0.8$		10	
Process	$\sigma_0$ ratio	$W(\text{GeV})$	$ \cos \theta^* $	BL	BC	DKV
$K^+ K^- / \pi^+ \pi^-$	$0.89 \pm 0.04 \pm 0.15$	$3.0 - 4.1$	$< 0.6$	2.3	1.06	
$K_S K_S / K^+ K^-$	$\sim 0.10$ to $\sim 0.03$	$2.4 - 4.0$	$< 0.6$		0.005	2/25
$\pi^0 \pi^0 / \pi^+ \pi^-$	$0.32 \pm 0.03 \pm 0.06$	$3.1 - 4.1$	$< 0.6$		0.04-0.07	0.5
$\eta \pi^0 / \pi^0 \pi^0$	$0.48 \pm 0.05 \pm 0.04$	$3.1 - 4.0$	$< 0.8$	$0.24 R_f (0.46 R_f)^\ddagger$		
$\eta \eta / \pi^0 \pi^0$	$0.37 \pm 0.02 \pm 0.03$	$2.4 - 3.3$	$< 0.8$	$0.36 R_f^2 (0.62 R_f^2)^\ddagger$		

$^\dagger$  Exclude  $\chi_{cJ}$  region, 3.3 - 3.6 GeV.

$^\ddagger$  Assuming  $\eta$  is a member of SU(3) octet (superposition of octet and singlet with mixing angle of  $\theta_p = -18^\circ$ ).  
 $R_f$  is a ratio of decay constants,  $f_\eta^2 / f_{\pi^0}^2$ .

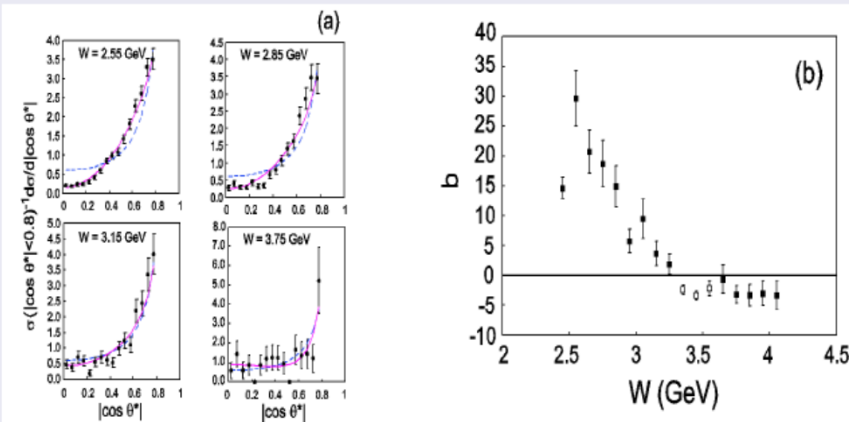
- $n$  ranges 7 to 11. Close or not far from QCD prediction of 6 and 10.
- Cross section ratios tend to be constant above 3 GeV.

Summarized by H.Nakazawa  
Hadron2013



# Angular dependence

$$\gamma\gamma \rightarrow \pi^0\pi^0$$

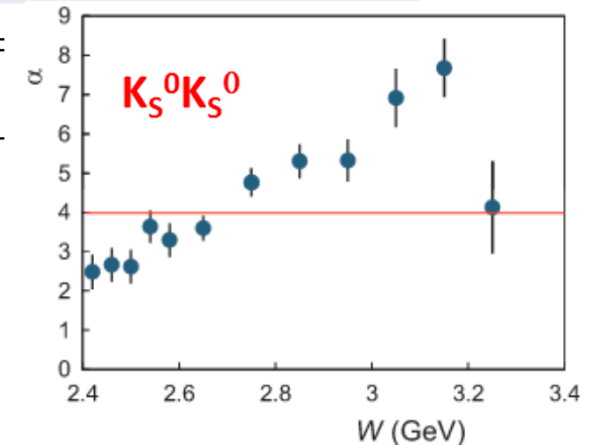


$d\sigma/d|\cos\theta^*| \propto \sin^{-4}\theta^*$  is predicted by  $q\bar{q}$ -meson model and perturbative QCD

- Fit to  $\sin^{-4}\theta^* + b \cos\theta^*$
- $b$  becomes constant above 3.2 GeV.

mode	$\alpha$ in $\sin^{-\alpha}\theta^*$	GeV	$ \cos\theta^* $
$K_S K_S$	3 - 8	2.6 - 3.3	< 0.8
$\pi^+ \pi^-$	Good agreement with 4	3.0 - 4.1	< 0.6
$K^+ K^-$	Good agreement with 4	3.0 - 4.1	< 0.6
$\pi^0 \pi^0$	Better agreement with $\sin^{-4}\theta^* + b \cos\theta^*$ Approaches $\sin^{-4}\theta^*$ above 3.1 GeV	2.4 - 4.1 <sup>†</sup>	< 0.8
$\eta \pi^0$	Good agreement with 4 above 2.7 GeV	3.1 - 4.1	< 0.8
$\eta \eta$	Poor agreement with 4 Close to 6 above 3 GeV	2.4 - 3.3	< 0.9

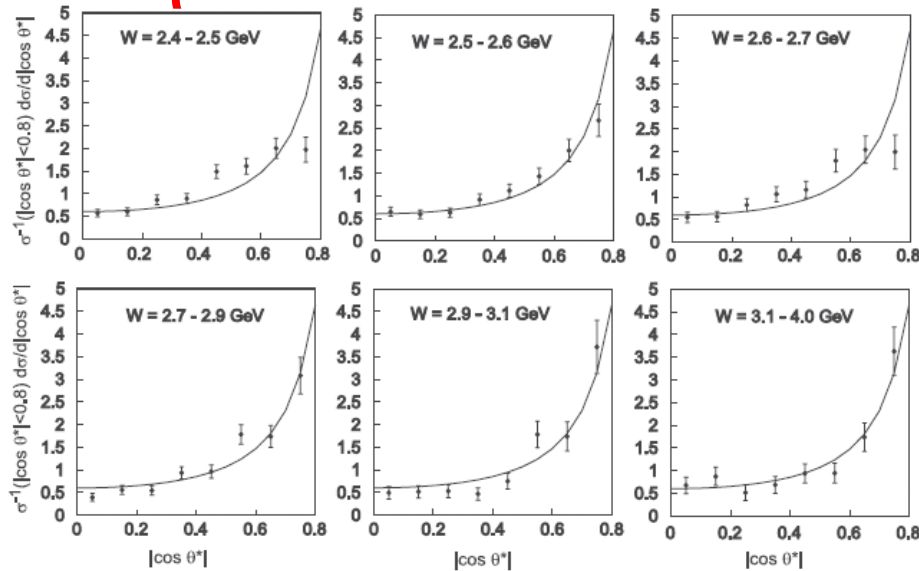
Exclude  $\dagger \chi_{\omega J}$  region, 3.3 - 3.6 GeV



Summarized by H.Nakazawa  
Hadron2013

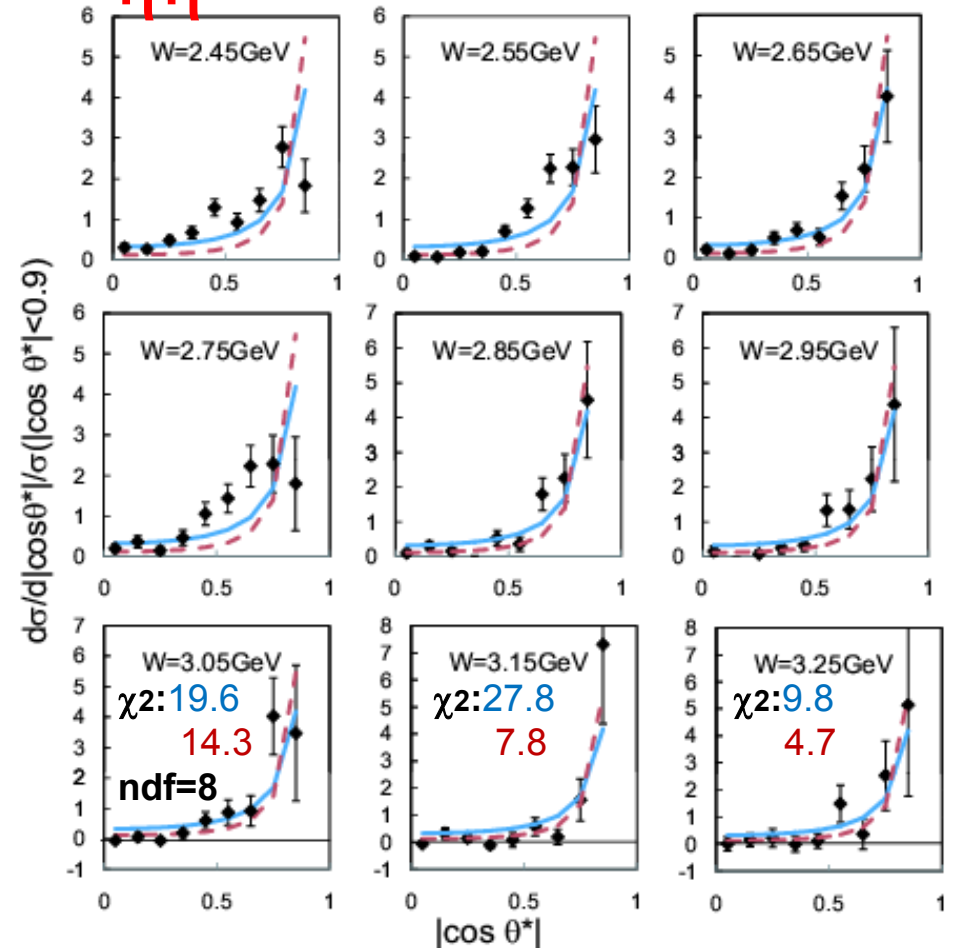
# $\pi^0\eta$ and $\eta\eta$

$\pi^0\eta$



The agreement with  $1/\sin^4 \theta^*$   
is good for  $W > 2.7 \text{ GeV}$

$\eta\eta$

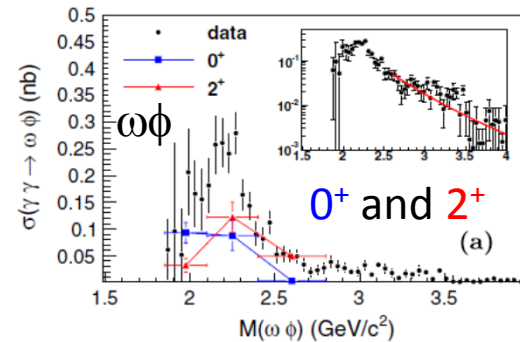
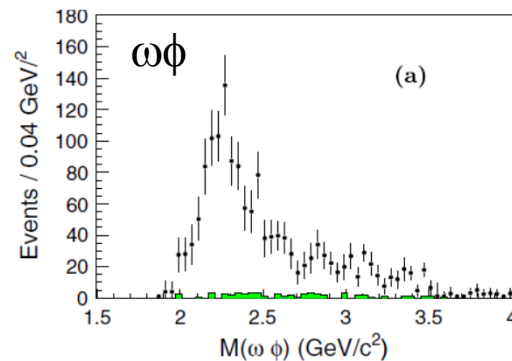


—  $\sim 1/\sin^4 \theta^*$  is not good anywhere.  
- - -  $\sim 1/\sin^6 \theta^*$  is better for  $W > 3.0 \text{ GeV}$



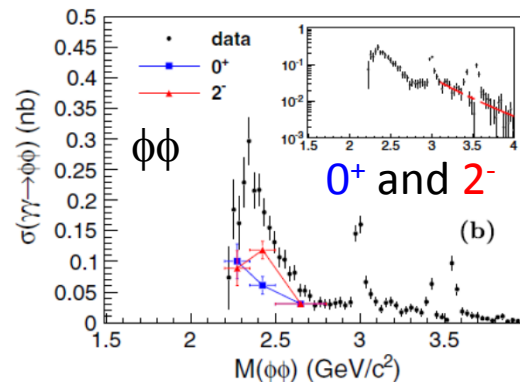
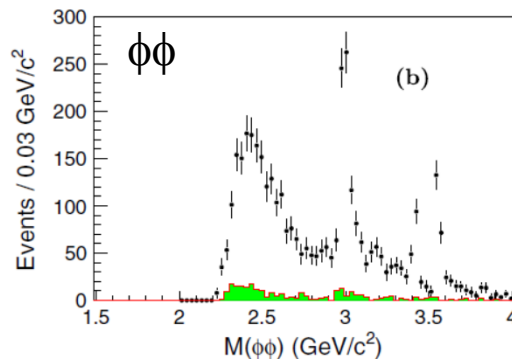
# “ $\gamma\gamma \rightarrow$ Vector-meson pair” from Belle

## Observation of New Resonant Structures in $\gamma\gamma \rightarrow \omega\phi$ , $\phi\phi$ , and $\omega\omega$



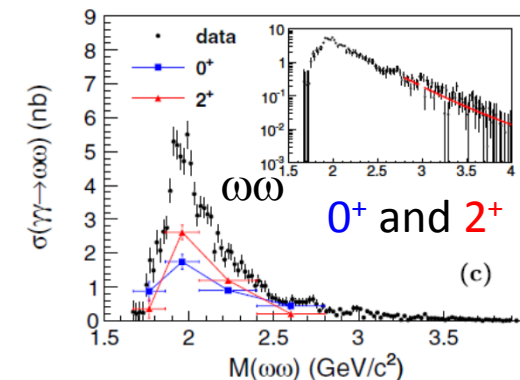
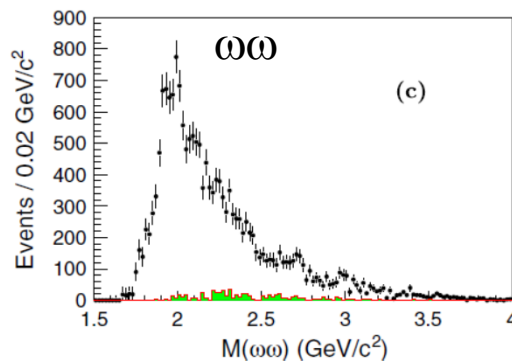
Belle, PRL 108, 232001 (2012)

There is a resonance-like structures at 2.0 – 2.5 GeV in each of the final states.



Preferred  $J^P$  combinations are determined by the angular analysis of production and decay of  $\omega$  and  $\phi$ .

Cross-section size for  $\omega\phi$  cannot be well explained.



Slope parameters for high W:

$$\begin{aligned} n &= 7.2 \pm 0.6 \quad (\omega\phi) \\ &8.4 \pm 1.1 \quad (\phi\phi) \\ &9.1 \pm 0.6 \quad (\omega\omega) \end{aligned}$$



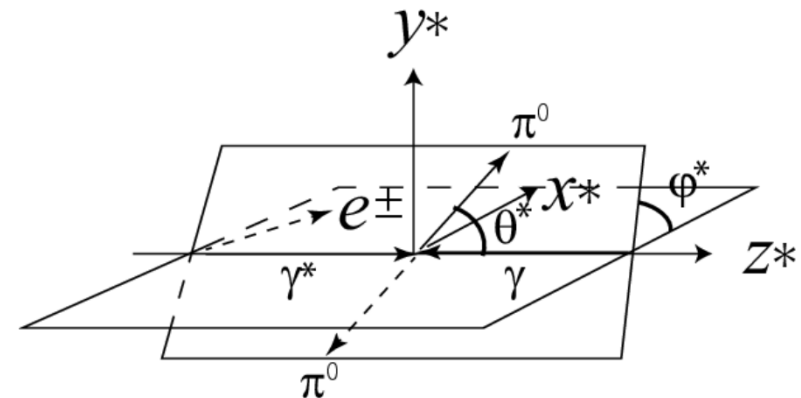
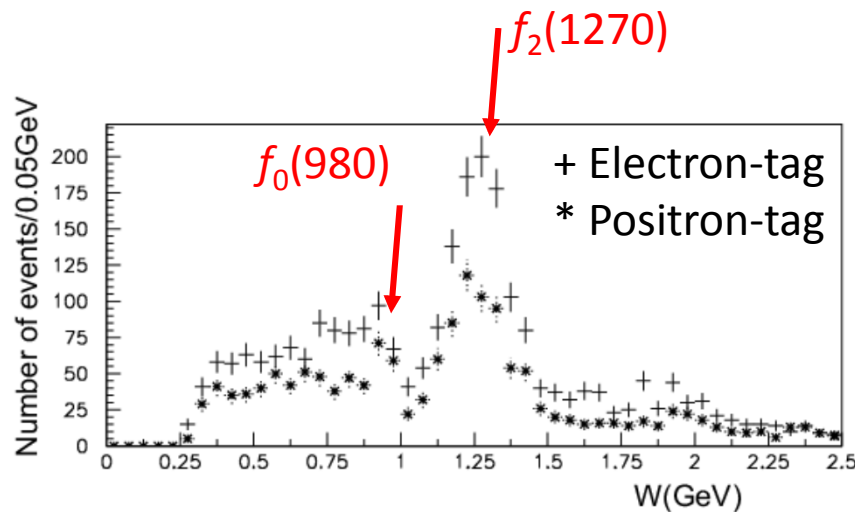
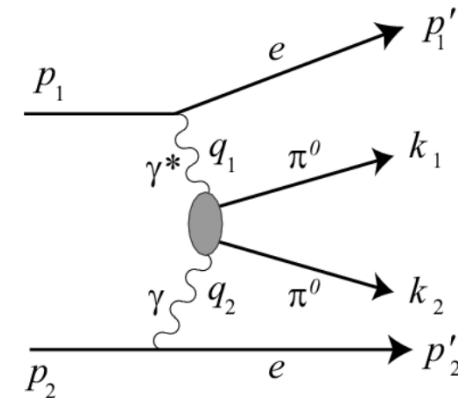
# $\gamma^*\gamma \rightarrow \pi^0\pi^0 : f_0(980) \text{ and } f_2(1270) \text{ TFF's}$

## TFF: Transition Form Factor

### Physics motivations:

- $Q^2$  dependence of TFF for scalar and tensor mesons  
(This is the first measurement)
- Test of QCD of  $q\bar{q}$  meson model
- Light-by-Light – hadronic contribution for  $g-2|_\mu$

PRD 93, 032003 (2016)



The  $f_0/f_2$  ratio is larger than in the no-tag case.





# Formalism of PWA

$$|F(Q^2)| = \sqrt{\frac{\sigma_R^\lambda(Q^2)}{\sigma_R^\lambda(0)(1+\frac{Q^2}{M^2})}}$$

TFF is defined for each resonance  $R$  produced with each helicity  $\lambda$

To obtain the resonance amplitudes:

Perform PWA, parameterizing  $W$  dependence of the resonance and continuum components of each helicity amplitude, e.g.,

$$\frac{d\sigma(\gamma^*\gamma \rightarrow \pi^0\pi^0)}{d\Omega} = \sum_{n=0}^2 t_n \cos(n\varphi^*),$$

$$\begin{aligned} t_0 &= |M_{++}|^2 + |M_{+-}|^2 + 2\epsilon_0 |M_{0+}|^2, \\ t_1 &= 2\epsilon_1 \Re((M_{+-}^* - M_{++}^*)M_{0+}), \\ t_2 &= -2\epsilon_0 \Re(M_{+-}^* M_{++}), \end{aligned}$$

$$M_{++} = S + D_0,$$

$$S = B_S(W) + A_{f_0}(W)$$

$$D_0 = 4\pi [B_{D_0}(W) + A_{f_2}(W)\sqrt{r_{20}}] Y_2^0$$

etc.

Determine each component as well as the relative phase by a fit

$++$  etc. --- Helicity state of the incident photons

$S, D_0$  etc. -- Partial-wave amplitude in  $\pi^0\pi^0$  scattering

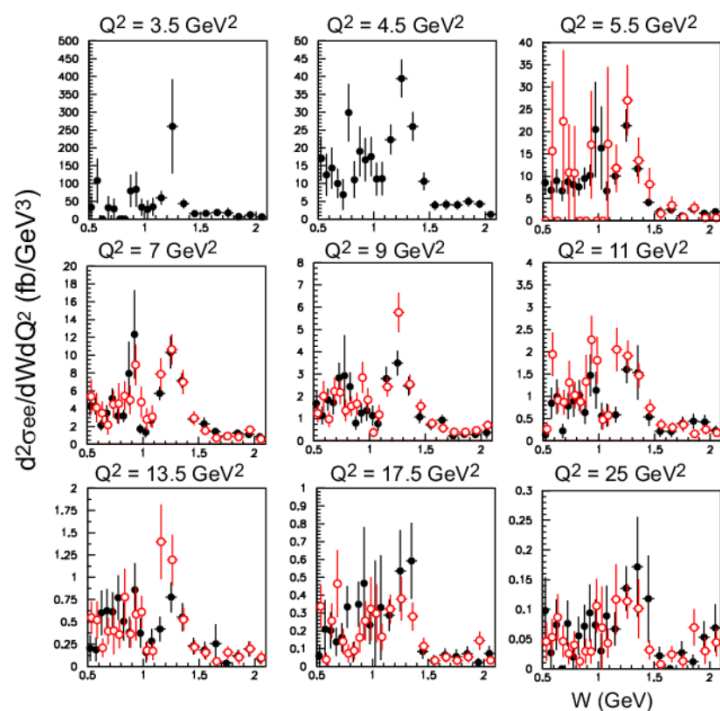
$B, A_f$  -- Background and  $f$ -resonance components.

$\epsilon_0, \epsilon_1$  --- A spin-dependent flux factor ratio for the virtual-photons

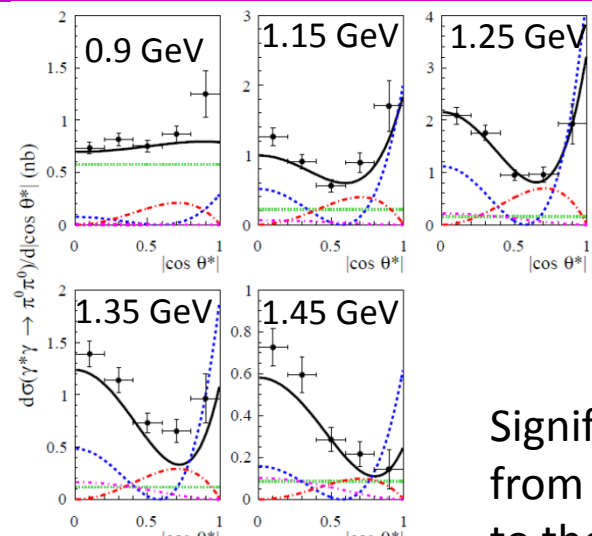


# Cross-section results and fit

Consistency check between  
electron-tag(●) and positron-tag(○)



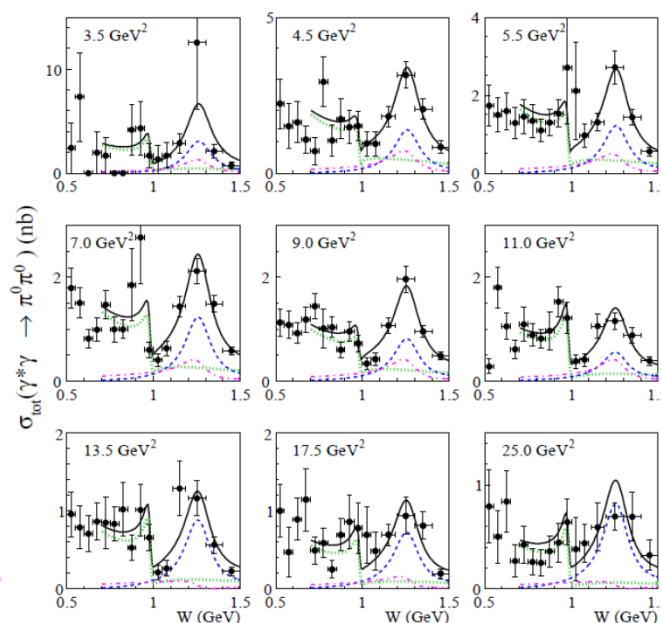
The curves are PWA fit constructed by  
parameterized resonant ( $f_0(980)$  and  
 $f_2(1270)$ ) and continuum amplitudes.



$|\cos \theta^*|$  dependence  
for  $Q^2 = 9 \text{ GeV}^2$  and  
different W bins

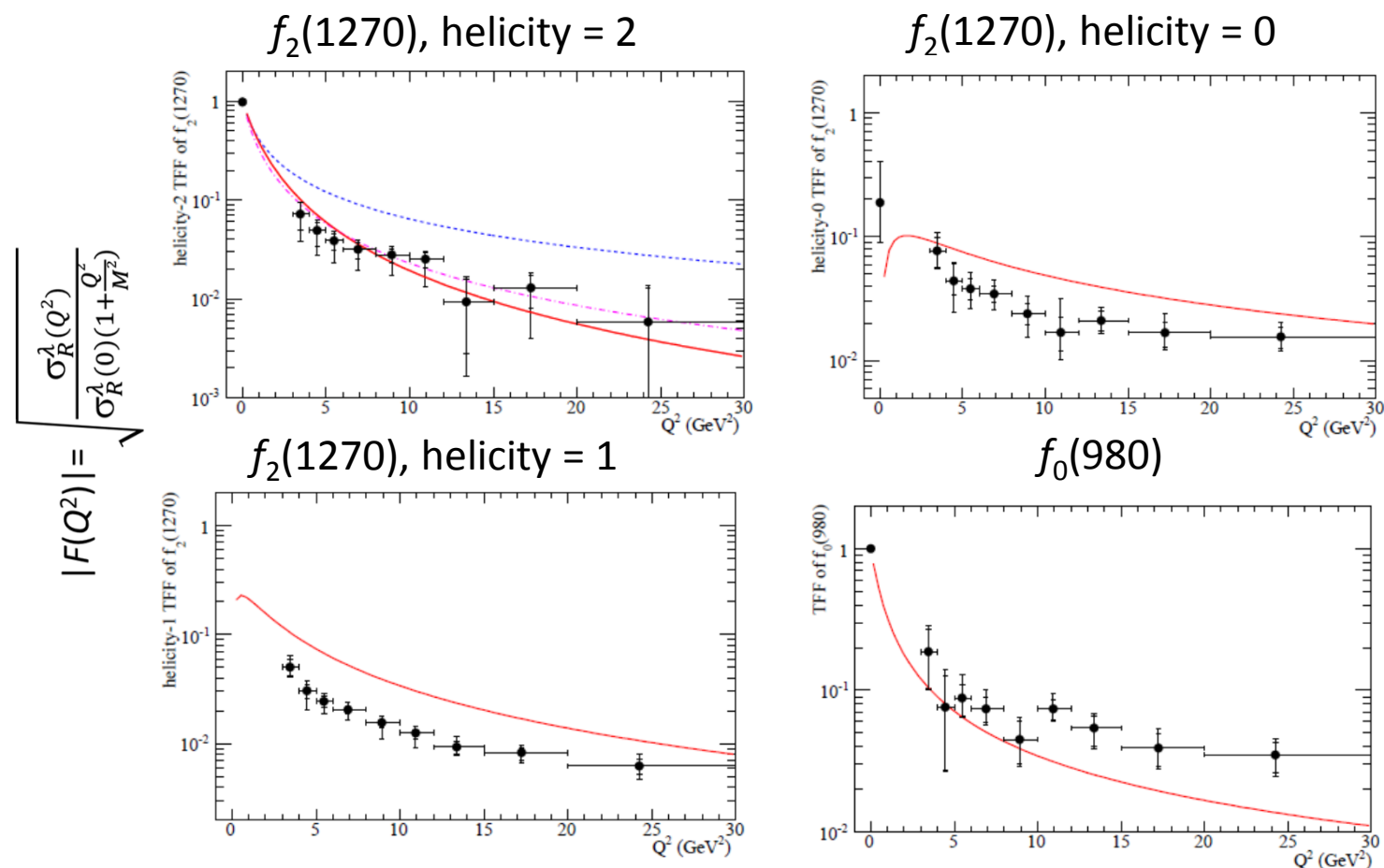
lines: solid= total,  
dotted=  $|S|^2$ , dashed=  $|D_0|^2$ ,  
and dash-dotted=  $|D_2|^2$

Significant contributions  
from hel.=0 and 1 in contrast  
to the no-tag ( $Q^2=0$ ) case



Final result of  
 $\gamma^*\gamma$  cross sections  
and PWA fits

# Q<sup>2</sup> dependence of resonant amplitudes



Theoretical predictions:

- Schuler, Berends, van Gulik, a heavy quark approx. NPB 523, 423 (1998)
- Pascaluts, Pauk, Vanderhaeghen, saturated sum rule, PRD 85, 116001 (2012),  $\eta$ 's
- - - ibid., axial-vector mesons



# Summary

---

- $\gamma\gamma \rightarrow$  pseudoscalar-meson pair have been measured in six different final states. Measure  $\Gamma_{\gamma\gamma}(\times \text{BF})$  for various  $J^{PC}=(\text{even})^{++}$  mesons
- Resonant signals in the 1.6 – 2.6 GeV region are also found in the VV.

We confirm that light-quark resonance effects are important up to  $W \sim 2.6$  GeV in two-photon processes of exclusive final-state processes.

- In  $W$  between  $\sim 2.5$  and 4 GeV, QCD tests are performed in  $W$  and angular dependences and cross-section ratios.
- TFFs for  $f_0(980)$  and  $f_2(1270)$ , in their  $Q^2$  dependence, have been measured for the first time.



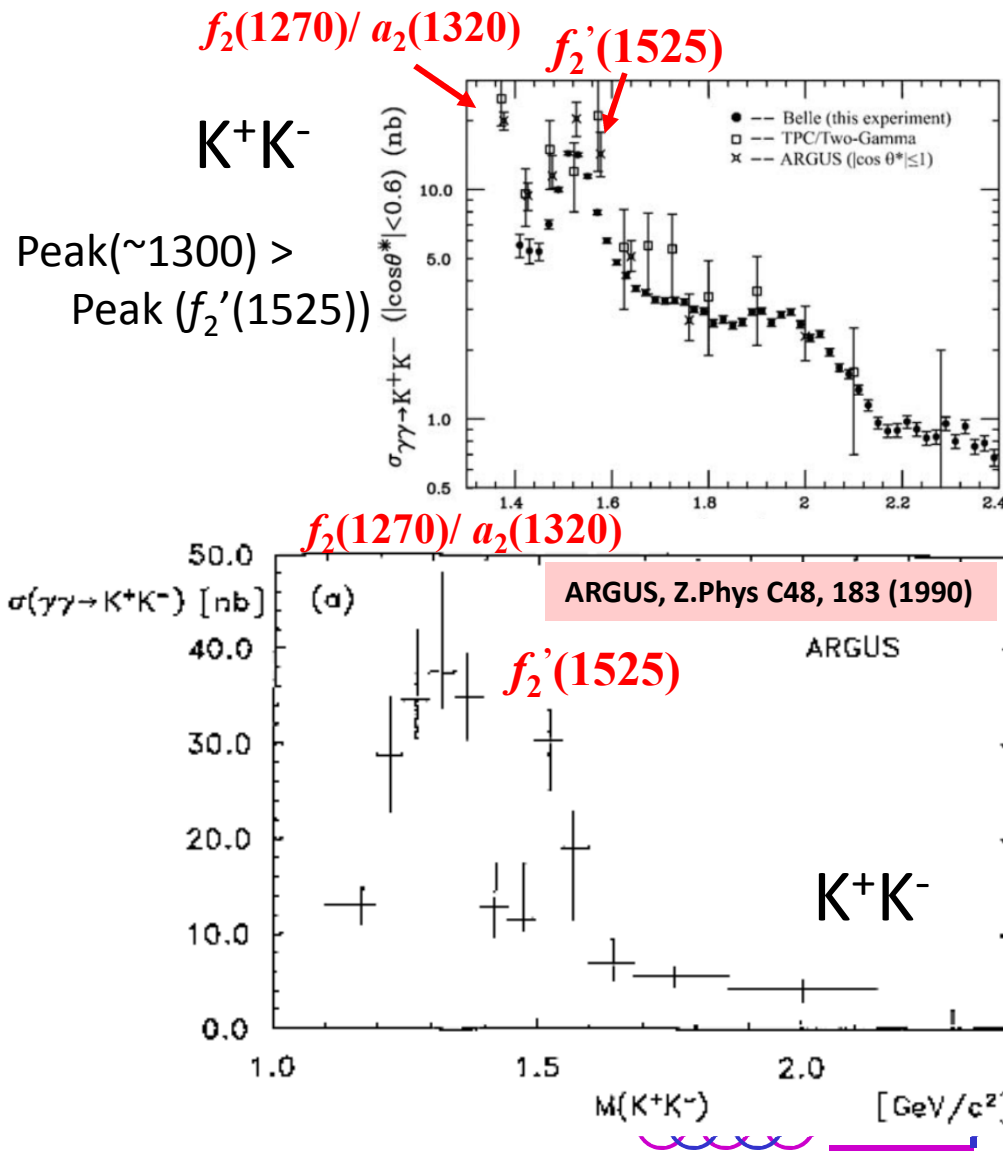
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# Backup



# $f_2(1270)$ - $a_2(1320)$ interference in $K\bar{K}$



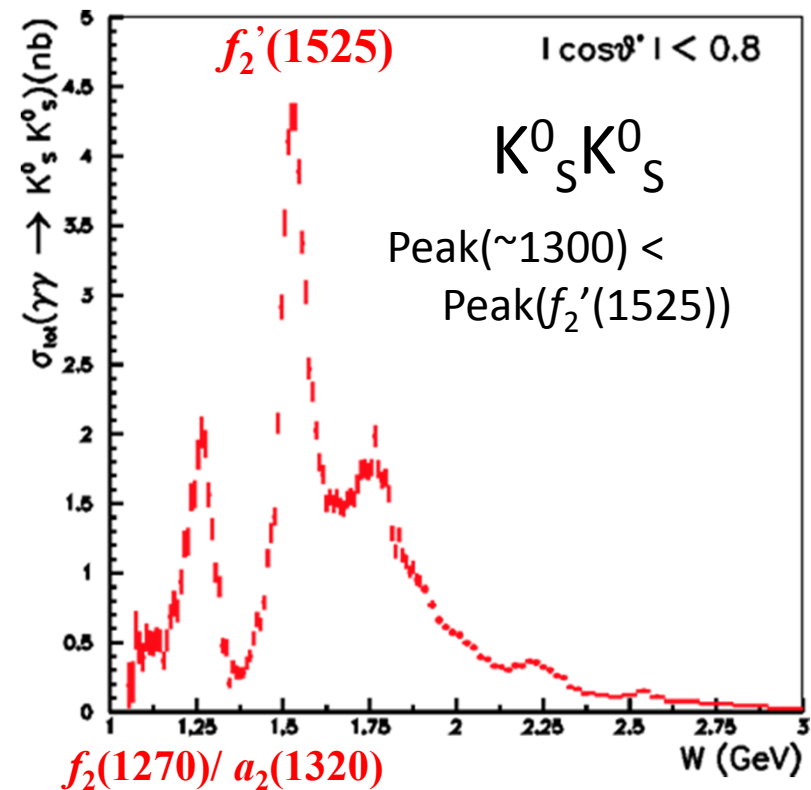
Constructive interference

$f_2(1270)+a_2(1320)$  in  $K^+K^-$

Destructive interference

$f_2(1270)-a_2(1320)$  in  $K_S^0 K_S^0$

Explained by a phase relation in isospin composition



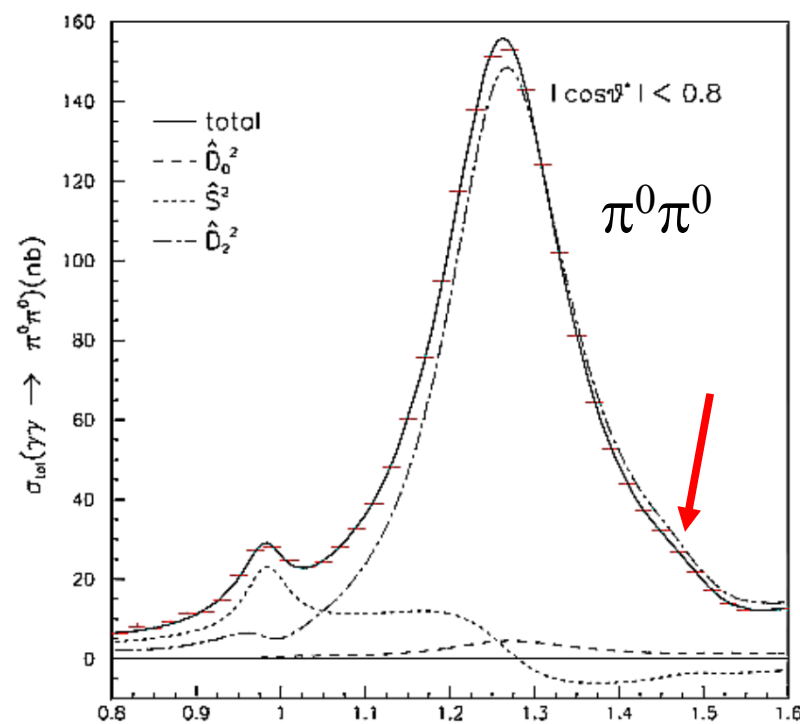
# Scalars in the 1.2 – 1.6 GeV region

- Hadron experiments report a wide  $f_0(1370)$  and a narrow  $f_0(1500)$ .
- Some of previous two-photon measurements provide a hint of  $f_0(1100-1400) \rightarrow \pi\pi$  under the huge peak of  $f_2(1270)$
- Belle's  $\pi^0\pi^0$  measurement reports  $f_0(1470)$ .  
May be visible in the line shape.  
→ favorable to the narrow  $f_0(1500)$ ,  
but also consistent with  $f_0(1370)$ .

<b><math>f_0(1370)</math> [1]</b>			
$I^G(J^{PC}) = 0^+(0^{++})$			
Mass $m = 1200$ to $1500$ MeV			
Full width $\Gamma = 200$ to $500$ MeV			
$f_0(1370)$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)	
$\pi\pi$	seen	672	

<b><math>f_0(1500)</math> [n]</b>			
$I^G(J^{PC}) = 0^+(0^{++})$			
Mass $m = 1505 \pm 6$ MeV ( $S = 1.3$ )			
Full width $\Gamma = 109 \pm 7$ MeV			
$f_0(1500)$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor	$p$ (MeV/c)
$\pi\pi$	$(34.9 \pm 2.3) \%$	1.2	741



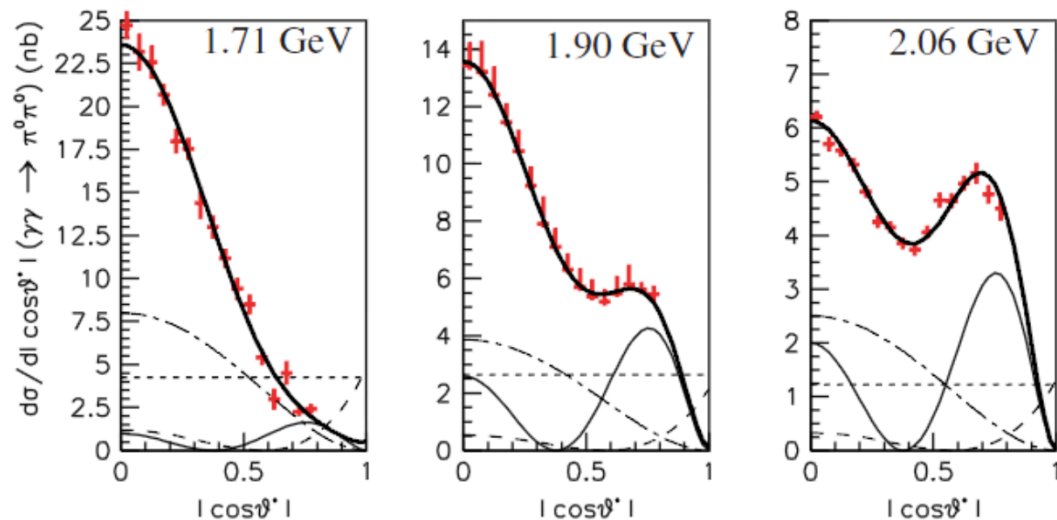
Parameter	Belle ( $\pi^0\pi^0$ )	Crystal Ball	Unit
Mass	$1470^{+6+72}_{-7-255}$	1250	MeV/c <sup>2</sup>
$\Gamma_{\text{tot}}$	$90^{+2+50}_{-1-22}$	$268 \pm 70$	MeV
$\Gamma_{\gamma\gamma} \mathcal{B}(\pi^0\pi^0)$	$11^{+4+603}_{-2-7}$	$430 \pm 80$	eV



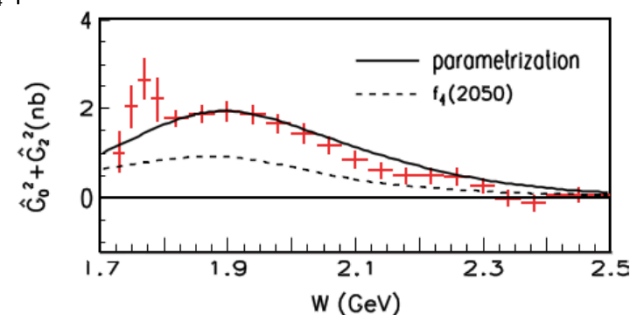
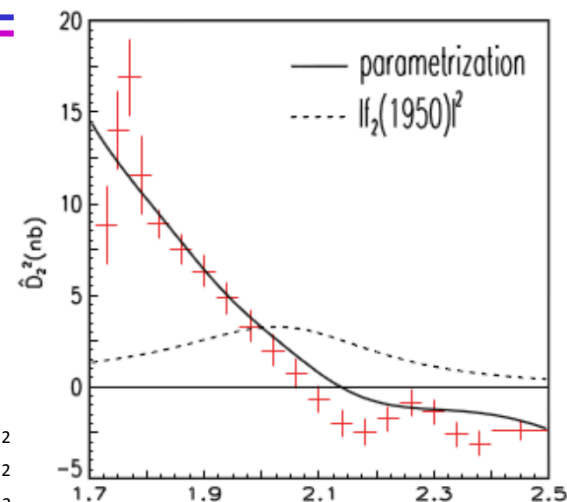


# $J=2$ and $J=4$ components in $\pi^0\pi^0$

Angular ( $|\cos\theta^*|$ ) dependence of the differential cross section



Curves:  
 - - -  $|S|^2$   
 - - -  $4\pi|D_0Y_2^0|^2$   
 - - -  $4\pi|D_2Y_2^2|^2$   
 - - -  $4\pi|G_2Y_4^2|^2$   
 — Total



Parameter	$f_4(2050)$	" $f_2(1950)$ "	Unit
Mass	$1885^{+14}_{-13} {}^{+218}_{-25}$	$2038^{+13}_{-11} {}^{+12}_{-73}$	MeV/ $c^2$
$\Gamma_{\text{tot}}$	$453 \pm 20 {}^{+31}_{-129}$	$441^{+27}_{-25} {}^{+28}_{-192}$	MeV
$\Gamma_{\gamma\gamma} \mathcal{B}(\pi^0\pi^0)$	$7.7^{+1.2}_{-1.1} {}^{+23.5}_{-5.2}$	$54^{+23}_{-14} {}^{+379}_{-68}$	eV
$\chi^2(\text{ndf})$	323.2 (311)		

The mass-magnitude relation to the spin between  $f_2$  and  $f_4$  is opposite between our measurement and PDG.

(That is possible between the  $J=2(2P)$  and  $J=4(1F)$  states.)





$$\gamma\gamma \rightarrow \eta' \pi^+ \pi^-$$

Production of light-quark mesons decaying to the **three pseudoscalar meson final state**. (The  $\eta_c$  production is also presented.)

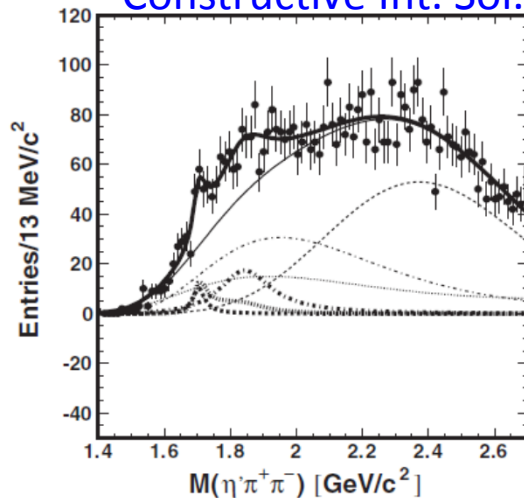
Belle, PRD 86, 052002 (2012)

**X(1835)** is an exotic resonance candidate found in the radiative decay of  $J/\psi$  by BES. Is it gluon-rich, or  $q\bar{q}$ -rich?

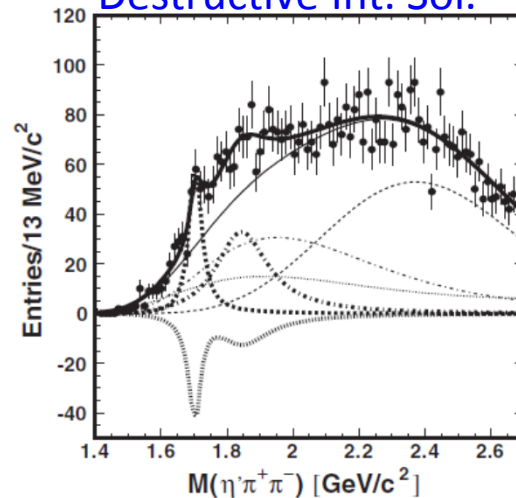
A hint of X(1835) –  $2.8\sigma$ ,  
but it is not very significant.

$\eta(1760) + X(1835) + \text{Non-Res} + \text{Backgrounds}$

Constructive Int. Sol.



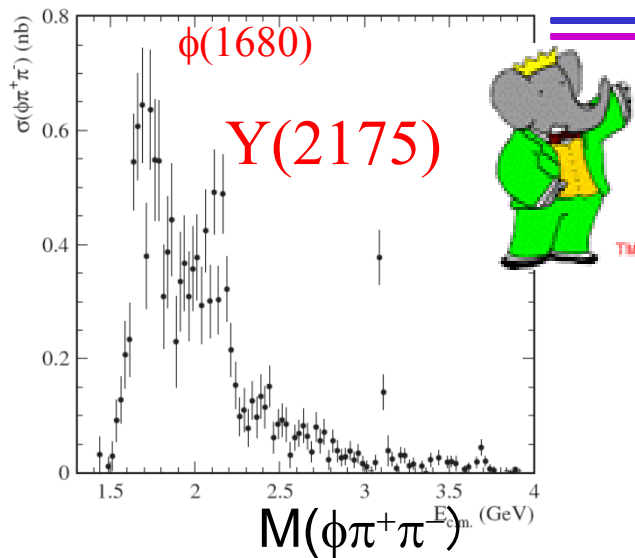
Destructive Int. Sol.



Parameter	Two interfering resonances		Reference
	Solution I	Solution II	
	X(1835)		
$M, \text{MeV}/c^2$	1836.5 (fixed)		$1836.5 \pm 3.0^{+5.6}_{-2.1}$
$\Gamma, \text{MeV}/c^2$	190 (fixed)		$190 \pm 9^{+38}_{-36}$
$\Gamma_{\gamma\gamma}\mathcal{B}, \text{eV}/c^2$	$18.2^{+7.7}_{-6.7} \pm 4.0$	$35^{+12}_{-13} \pm 8$	
$(\Gamma_{\gamma\gamma}\mathcal{B})_{90} \text{ eV},$	$<35.6$	$<83$	
$S, \sigma$	2.8		
	$\eta(1760)$		
$M, \text{MeV}/c^2$	$1703^{+12}_{-11} \pm 1.8$		$1756 \pm 9$
$\Gamma, \text{MeV}/c^2$	$42^{+36}_{-22} \pm 15$		$96 \pm 70$
$\Gamma_{\gamma\gamma}\mathcal{B}, \text{eV}/c^2$	$3.0^{+2.0}_{-1.2} \pm 0.8$	$18^{+13}_{-10} \pm 5$	
$S, \sigma$	4.1		
$\phi$	$(287^{+42}_{-51})^\circ$	$(139^{+19}_{-9})^\circ$	



Exotic in  $s\bar{s}$  sector ? ; (ISR)  $e^+e^- \rightarrow Y(2175) \rightarrow \phi\pi^+\pi^-$



PRD76,012008(2007)

BaBar: A clear structure above  $\phi(1680)$ , Identified as  $Y(2175)$ .

$$m_x = 2.175 \pm 0.010 \pm 0.015 \text{ GeV}/c^2$$

$$\Gamma_x = 0.058 \pm 0.016 \pm 0.020 \text{ GeV}/c^2$$

BESII confirms

$$\text{Mass} = 2.186 \pm 0.010 \pm 0.006 \text{ GeV}/c^2$$

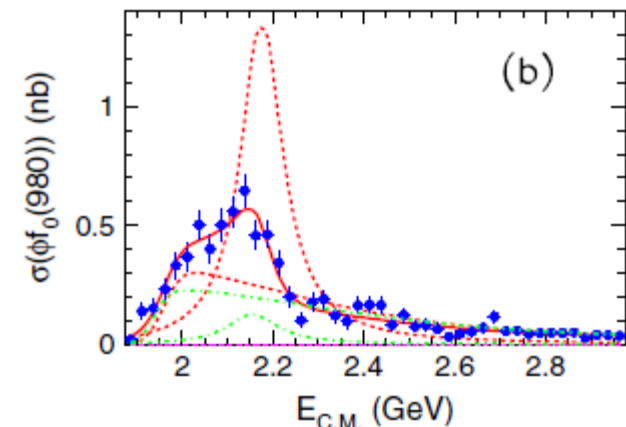
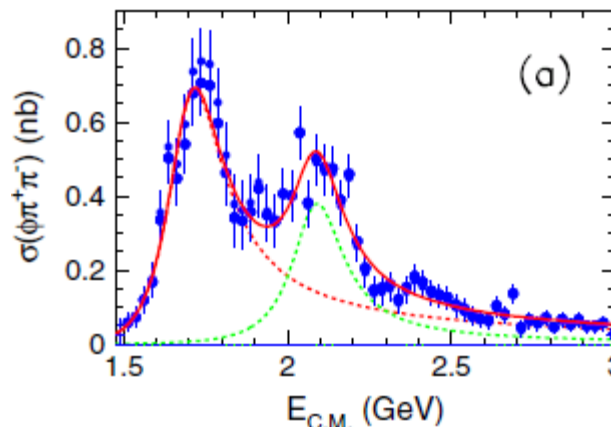
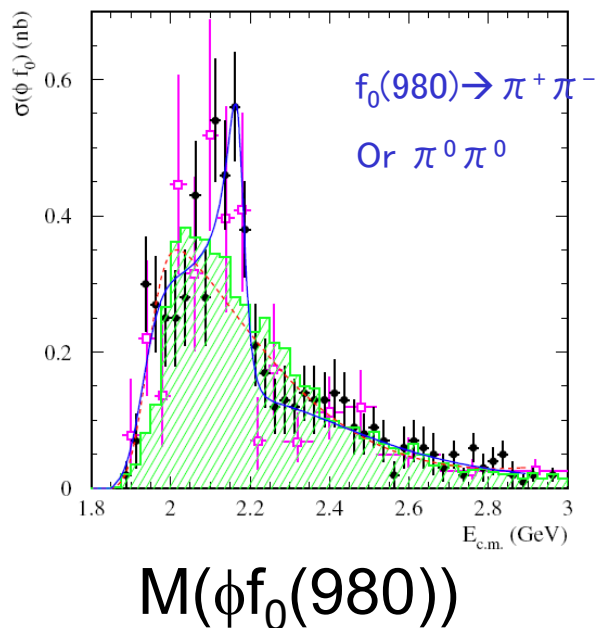
$$\text{Width} = 0.065 \pm 0.023 \pm 0.017 \text{ GeV}/c^2$$

$$M(Y(2175)) = 2079 \pm 13^{+79}_{-28} \text{ MeV}/c^2$$

$$\Gamma(Y(2175)) = 192 \pm 23^{+25}_{-61} \text{ MeV}/c^2$$



PRD 80, 031101(R) (2009)



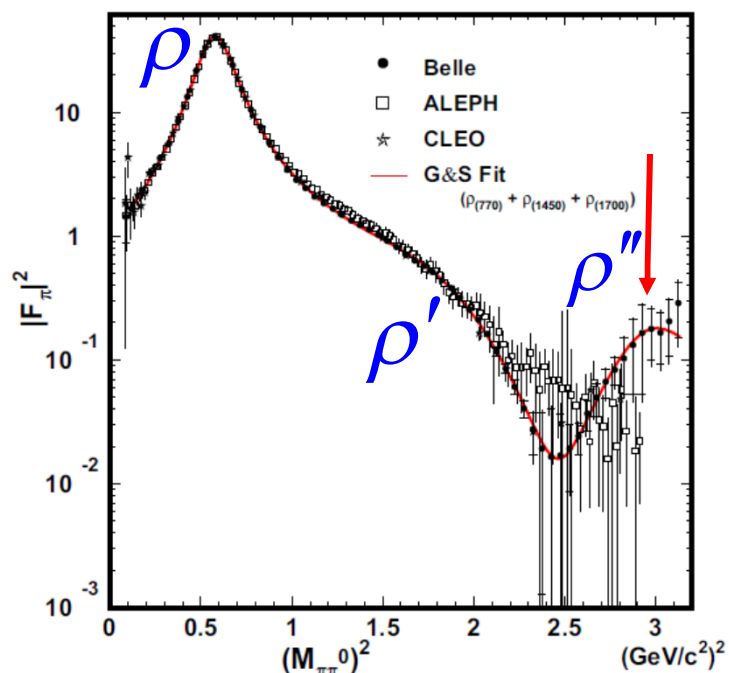
S.Uehara, KEK, Jan. 2017

# $\rho(1700)$ in $\tau^- \rightarrow \pi^- \pi^0 \nu$ Decay

PRD 78, 072006 (2008)

From 64M  $\tau^+\tau^-$  pairs, Belle

selects 5.5M  $\tau^- \rightarrow \pi^- \pi^0 \nu_\tau$  events!



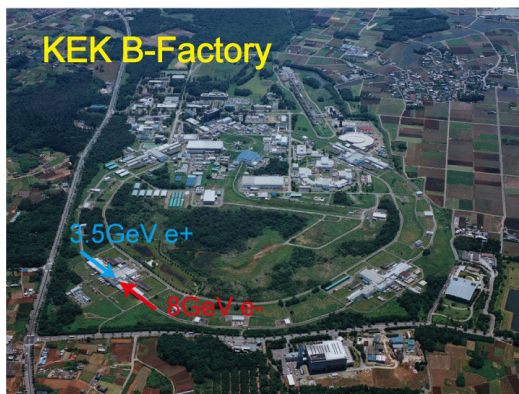
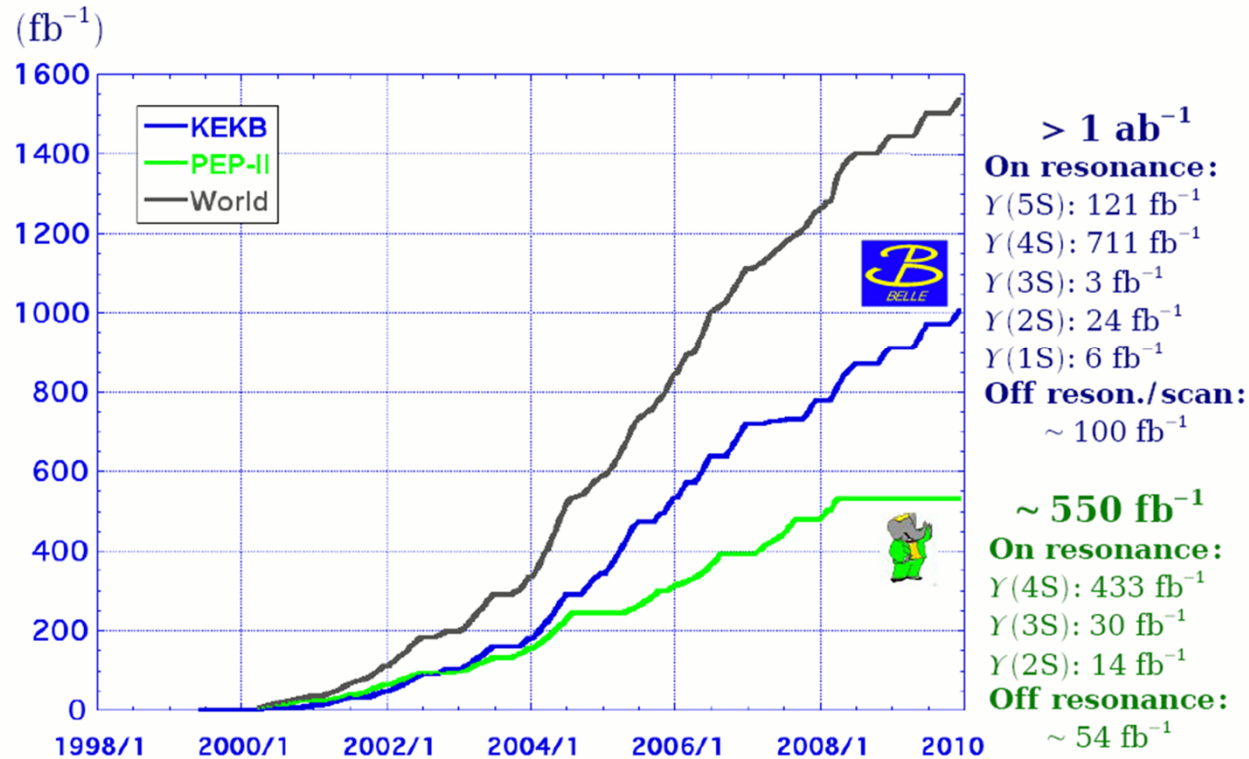
- Error bars include both statistical and systematic
- Interference between  $\rho'$  and  $\rho''$
- — Fit with BW

Fit parameter	Norm fixed
Norm $ F_\pi(0) ^2$	<b>[1.0]</b>
$M_\rho$ (MeV)	<b><math>774.6 \pm 0.2 \pm 0.5</math></b>
$\Gamma_\rho$ (MeV)	<b><math>148.1 \pm 0.4 \pm 1.7</math></b>
$M_{\rho'}$ (MeV)	<b><math>1446 \pm 7 \pm 28</math></b>
$\Gamma_{\rho'}$ (MeV)	<b><math>434 \pm 16 \pm 60</math></b>
$ \beta $	<b><math>0.15 \pm 0.05 \pm_{0.04}^{0.15}</math></b>
$\phi_\beta$ (degree)	<b><math>202 \pm 4 \pm_8^{41}</math></b>
$M_{\rho''}$ (MeV)	<b><math>1728 \pm 17 \pm 89</math></b>
$\Gamma_{\rho''}$ (MeV)	<b><math>164 \pm 21 \pm_{26}^{89}</math></b>
$ \gamma $	<b><math>0.028 \pm 0.020 \pm_{0.009}^{0.059}</math></b>
$\phi_\gamma$ (degree)	<b><math>24 \pm 9 \pm_{28}^{118}</math></b>
$\chi^2/\text{d.o.f}$	<b>80/52</b>



# History of integrated luminosity at Belle

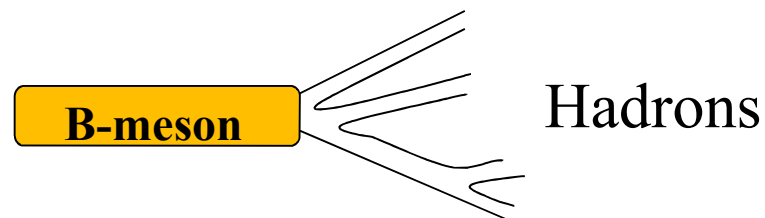
## Luminosity at B factories



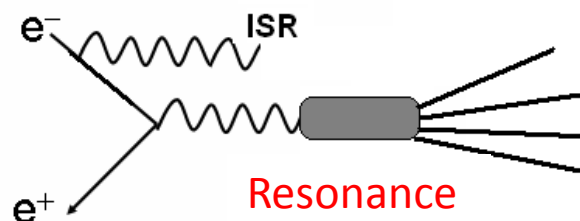
1999	The Belle experiment started
2001	CP violation in B mesons was verified and the KEB accelerator achieved the world's highest luminosity
2002	Anomalous CP violation in $b \rightarrow s$ was measured
2003	The $B \rightarrow K\ell\ell$ decay was discovered
2004	The New particle X (3872) was discovered
2005	Direct violation of CP in $B \rightarrow K\pi$ was found. The $B \rightarrow \rho\gamma$ decay was discovered
2006	$B \rightarrow \tau\nu$ was observed
2007	D meson mixing was discovered. A new particle composed of 4 quarks Z (4430) $^+$ was discovered
2008	Dr. Makoto Kobayashi and Dr. Toshihide Maskawa were awarded the Nobel Prize in Physics
2010	The Belle experiment was completed

# Introduction : Hadron production processes at B-factory Experiments

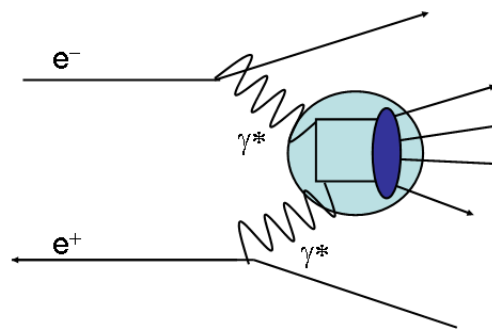
Hadronic decays of B meson



$e^+e^-$  annihilation processes  
ISR processes



two-photon collisions



# ● Nature of $I=0$ and $I=1$ interference in $K\bar{K}$

- Consider both isospin  $I=0$  and  $I=1$ , e.g.,  $f_J$  and  $a_J$
- Their Constructive and Destructive interference based on OZI (Okubo-Zweig-lizuka) rule and isospin  $I_z$  inversion.

D. Faiman, H.J. Lipkin and H.R. Rubinstein, PL 59B,269 (1975)

$$\begin{array}{lcl}
 \begin{array}{c} u \\ \hline \rightarrow \end{array} & \begin{array}{c} \searrow \\ \nearrow \end{array} & \begin{array}{c} \bar{s} \\ s \end{array} \begin{array}{c} K^+ \\ K^- \end{array} \\
 \begin{array}{c} \bar{u} \\ \hline \rightarrow \end{array} & \begin{array}{c} \searrow \\ \nearrow \end{array} & \begin{array}{c} \bar{s} \\ s \end{array} \begin{array}{c} K^+ \\ K^- \end{array} \\
 \begin{array}{c} d \\ \hline \rightarrow \end{array} & \begin{array}{c} \searrow \\ \nearrow \end{array} & \begin{array}{c} \bar{s} \\ s \end{array} \begin{array}{c} K^0 \\ \bar{K}^0 \end{array} \\
 \begin{array}{c} \bar{d} \\ \hline \rightarrow \end{array} & \begin{array}{c} \searrow \\ \nearrow \end{array} & \begin{array}{c} \bar{s} \\ s \end{array} \begin{array}{c} K^0 \\ \bar{K}^0 \end{array}
 \end{array}
 \quad
 \begin{array}{l}
 |u\bar{u}\rangle = \frac{1}{\sqrt{2}}(f_J + a_J) \\
 |d\bar{d}\rangle = \frac{1}{\sqrt{2}}(f_J - a_J)
 \end{array}$$

**Size of the cross sections for  $K^+K^-$  and  $K^0\bar{K}^0$**

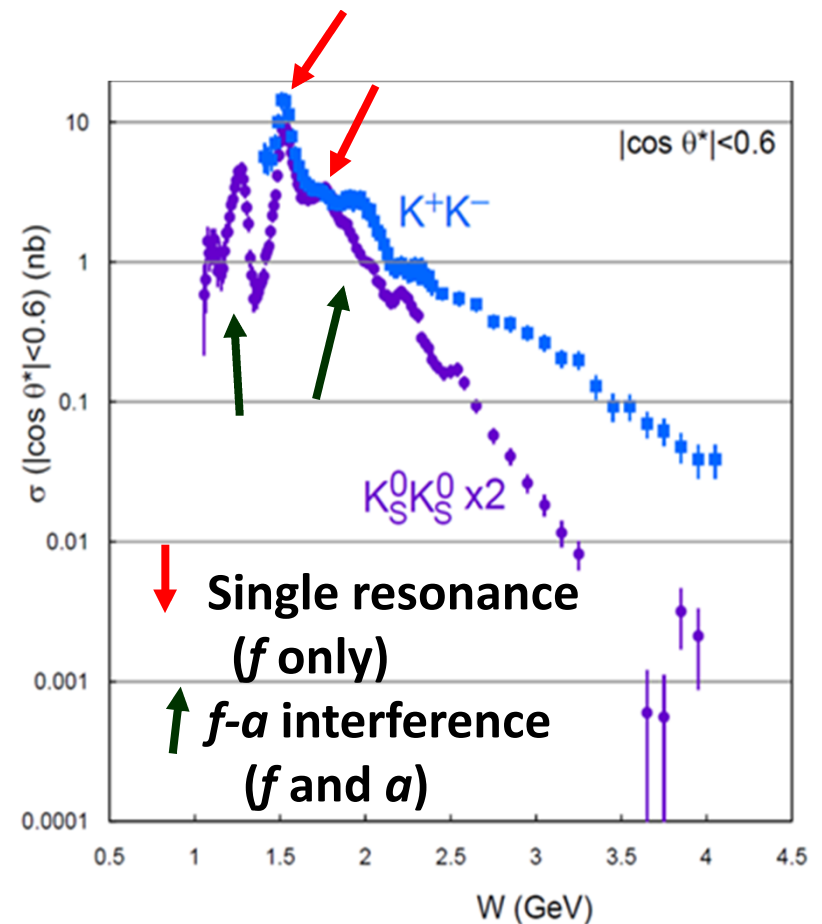
A single resonance production of  **$f$  or  $a$**  decaying with the strong interaction

→ The cross sections are **similar size**.

**If they are very different →**

Interference between  $I=0$  and  $I=1$  resonances, or effective (electromagnetic) continuum production

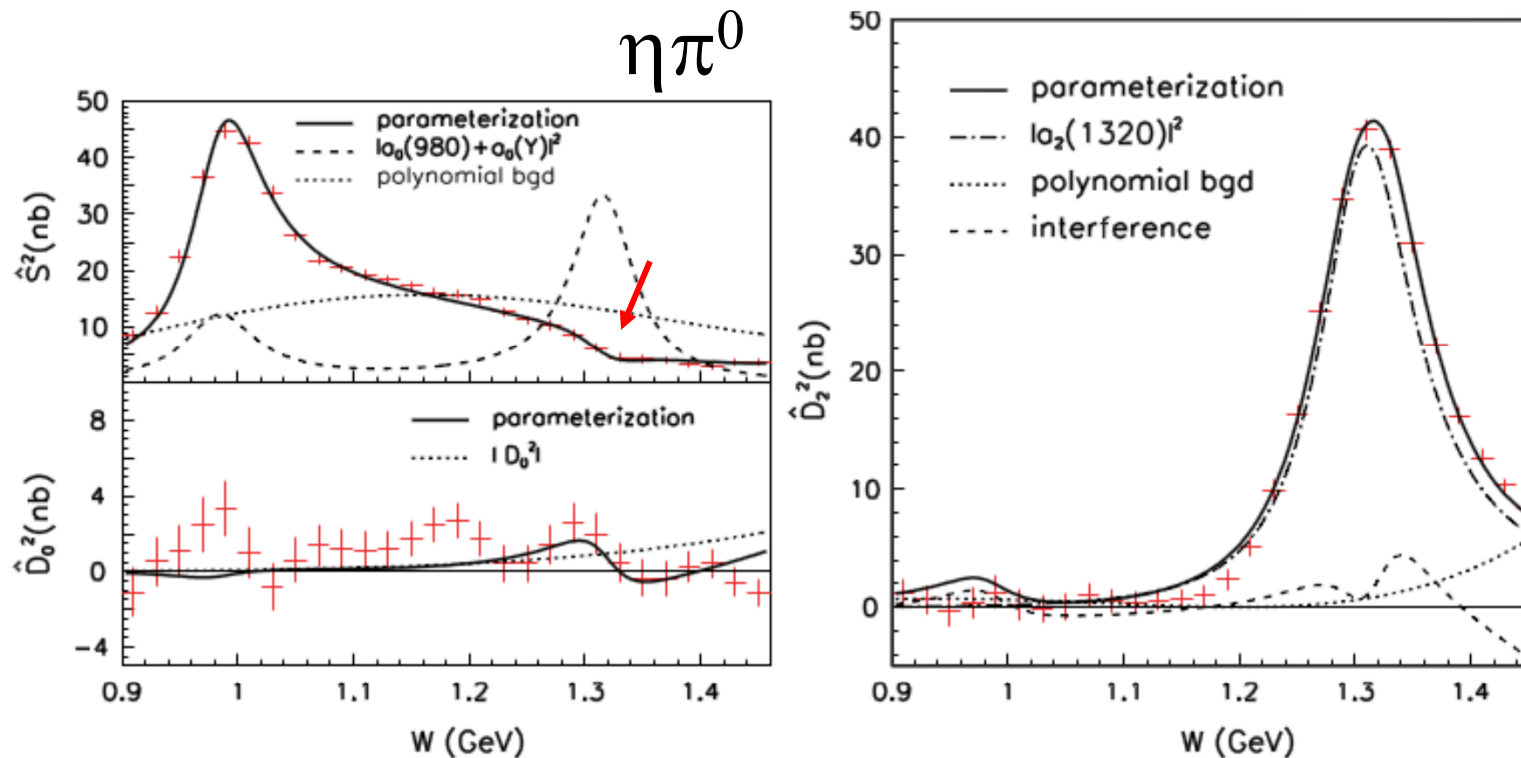
The difference above  $>\sim 2.4\text{GeV}$  is explained by electric-charge difference of the quarks.



S.Uehara, KEK, Jan. 2017

# The $I=1$ sector

- We find  $a_0(1320) \rightarrow \eta\pi^0$  just under  $a_2(1320)$ .
- The mass is not compatible with  $a_0(1450)$ ?



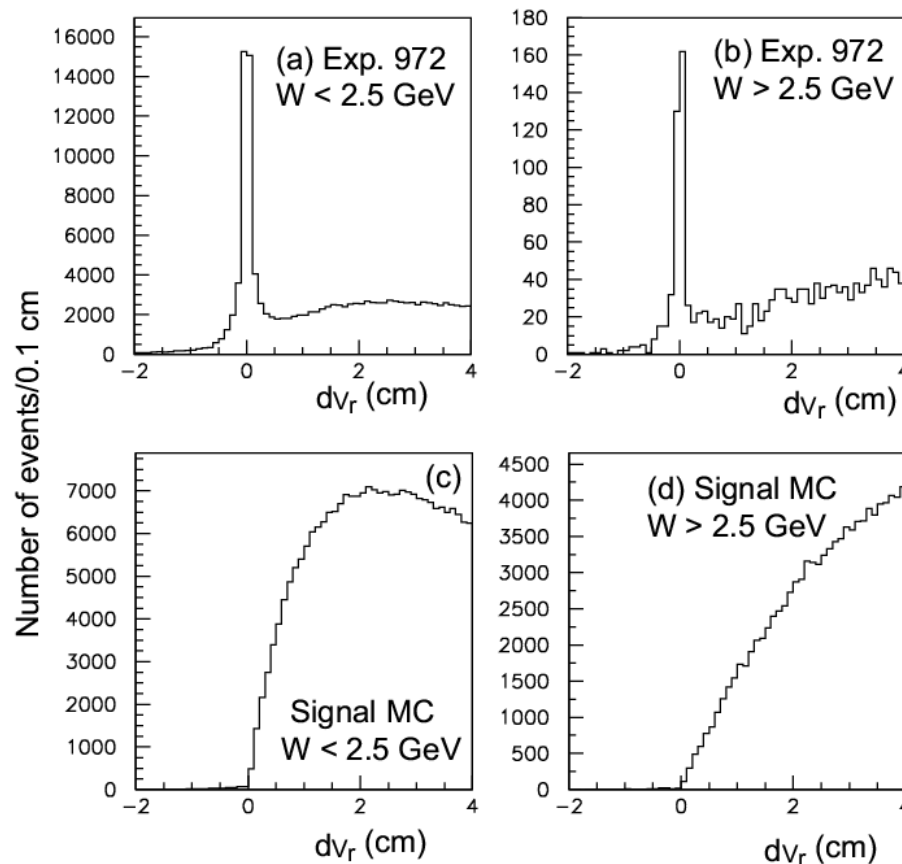
Parameter	This work	$a_0(1450)$ (PDG)	Unit
Mass	$1316.8^{+0.7+24.7}_{-1.0-4.6}$	$1474 \pm 19$	$\text{MeV}/c^2$
$\Gamma_{\text{tot}}$	$65.0^{+2.1+99.1}_{-5.4-32.6}$	$265 \pm 13$	MeV
$\Gamma_{\gamma\gamma}\mathcal{B}(\eta\pi^0)$	$432 \pm 6^{+1073}_{-256}$	unknown	eV

See Discussion in PDG-RPP2014,  
NOTE ON SCALAR MESONS  
BELOW 2GeV (pp 784 – 791)



# Ks Ks vertex distances

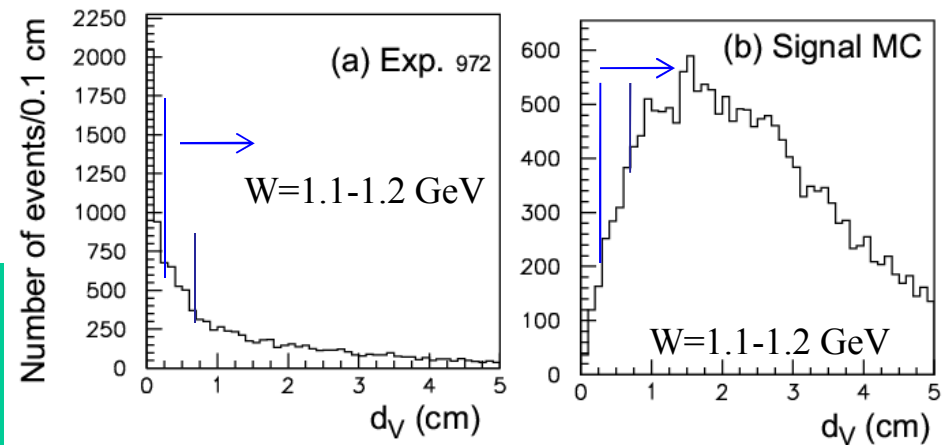
## 2D vertex distance



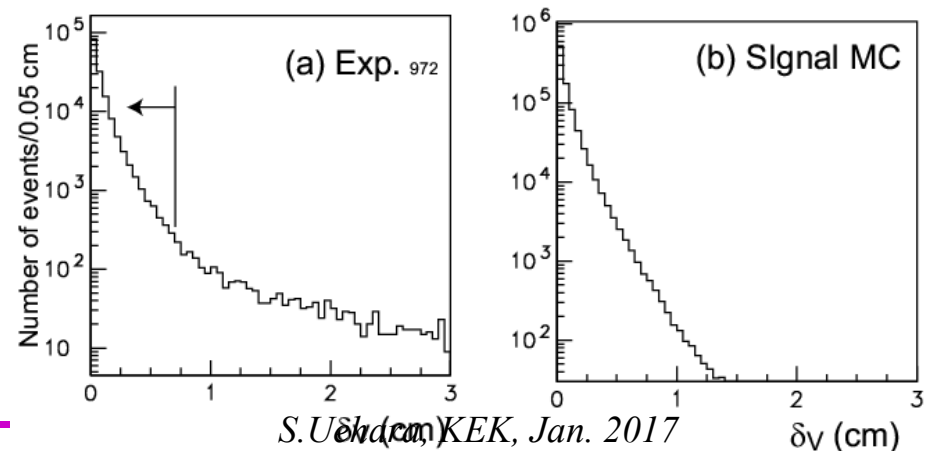
Sharp peaks near 0cm seen only in Exp. are from Direct  $4\pi$  ( $\pi^+\pi^-\pi^+\pi^-$ ) production backgrounds.



## 3D vertex distance



Tr. mometum diff. and vertex position diff. must be in parallel

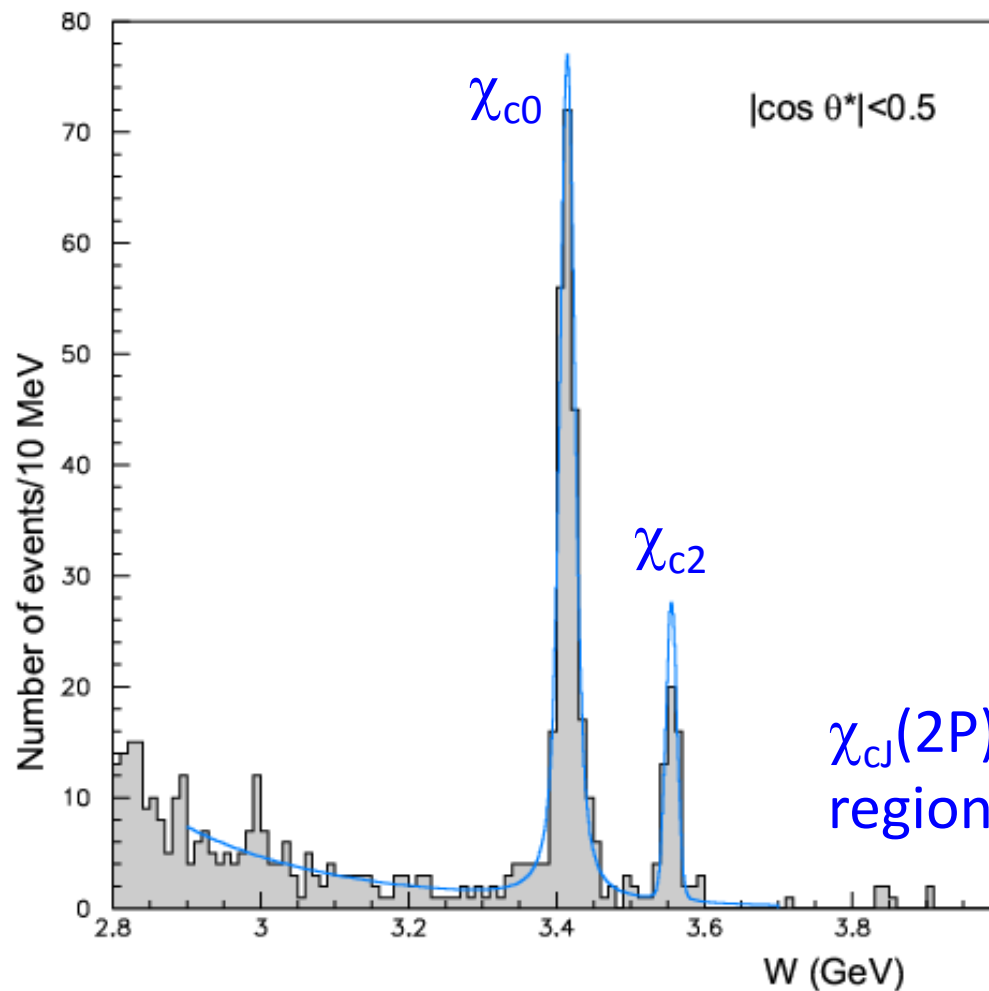




# Fit results for 13 assumptions

Assumption	No. of sol.	$\chi^2$	<i>ndf</i>
$f_0-f_0$	2	293.3, 293.9	214
$f_0-f_2$	4	320.9, 321.9, 324.5, 327.6	214
$f_0-f_4$	1	291.4	214
$f_2-f_0$	1	228.3	214
$f_2-f_2$	1	260.4	214
$f_2-f_4$	1	323.6, 306.7	214
$f_4-f_0$	1	411.6	214
$f_4-f_2$	2	468.6, 472.1	214
$f_4-f_4$	4	459.6, 464.1, 466.4, 467.5	214
Only- $f_0$	1	390.0	218
Only- $f_2$	1	323.6	218
Only- $f_4$	1	518.7	218
No resonances	1	659.32	222

# Charmonia $\chi_{c0}$ and $\chi_{c2}$



## Yield

Interference	$N_{\chi_{c0}}$	$N_{\chi_{c2}}$	$-2 \ln \mathcal{L}/ndf$
not included	$248.3^{+17.9}_{-17.2}$	$53.0^{+8.1}_{-7.4}$	57.34/73
included	$266 \pm 53$	$53^{+14}_{-12}$	57.22/71

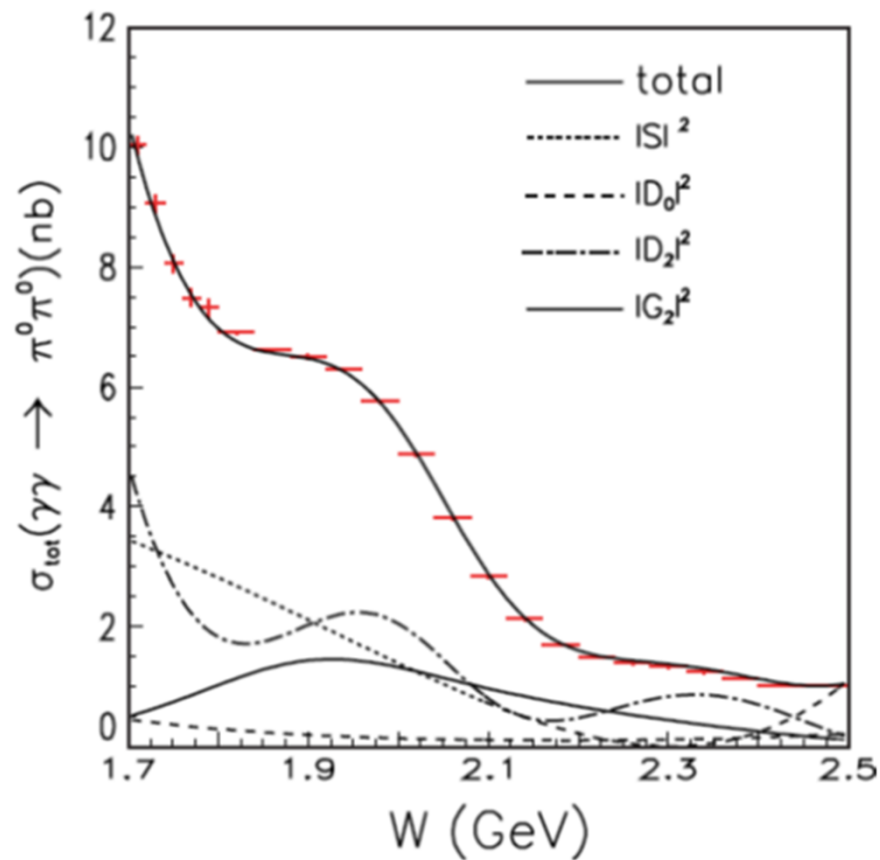
Interference between  $\chi_{c0}$  and continuum

Product of  
two-photon decay width  
and  $B(K^0_s K^0_s)$

Interference	$\Gamma_{\gamma\gamma} \mathcal{B}(\chi_{c0})$ (eV)	$\Gamma_{\gamma\gamma} \mathcal{B}(\chi_{c2})$ (eV)
not included	$8.09 \pm 0.58 \pm 0.83$	$0.268^{+0.041}_{-0.037} \pm 0.028$
included	$8.7 \pm 1.7 \pm 0.9$	$0.27^{+0.07}_{-0.06} \pm 0.03$
Belle 2007	$7.00 \pm 0.65 \pm 0.71$	$0.31 \pm 0.05 \pm 0.03$
PDG 2012	$7.3 \pm 0.5$	$0.297 \pm 0.026$



# Fit to $\pi^0\pi^0$ ( $W = 1.7 - 2.5$ GeV)



Parameter	$f_4(2050)$	" $f_2(1950)$ "	Unit
Mass	$1885^{+14}_{-13} \text{ } ^{+218}_{-25}$	$2038^{+13}_{-11} \text{ } ^{+12}_{-73}$	MeV/ $c^2$
$\Gamma_{\text{tot}}$	$453 \pm 20 \text{ } ^{+31}_{-129}$	$441^{+27}_{-25} \text{ } ^{+28}_{-192}$	MeV
$\Gamma_{\gamma\gamma} \mathcal{B}(\pi^0\pi^0)$	$7.7^{+1.2}_{-1.1} \text{ } ^{+23.5}_{-5.2}$	$54^{+23}_{-14} \text{ } ^{+379}_{-68}$	eV
$\chi^2(ndf)$	323.2 (311)		



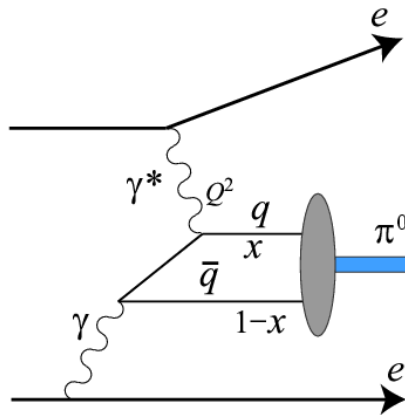
# $\pi^0$ Transition Form Factor

PRD 86, 092007 (2012)

$$\gamma\gamma^* \rightarrow \pi^0$$

Coupling of neutral pion with two photons

Good test for QCD at high  $Q^2$



Single-tag  $\pi^0$  production in two-photon process with a large- $Q^2$  and a small- $Q^2$  photon

Theoretically calculated from pion distribution amplitude and decay constant

$$F(Q^2) = \frac{\sqrt{2}f_\pi}{3} \int T_H(x, Q^2, \mu) \phi_\pi(x, \mu) dx$$

Measurement:

$$|F(Q^2)|^2 = |F(Q^2, 0)|^2 = (d\sigma/dQ^2)/(2A(Q^2))$$

$A(Q^2)$  is calculated by QED

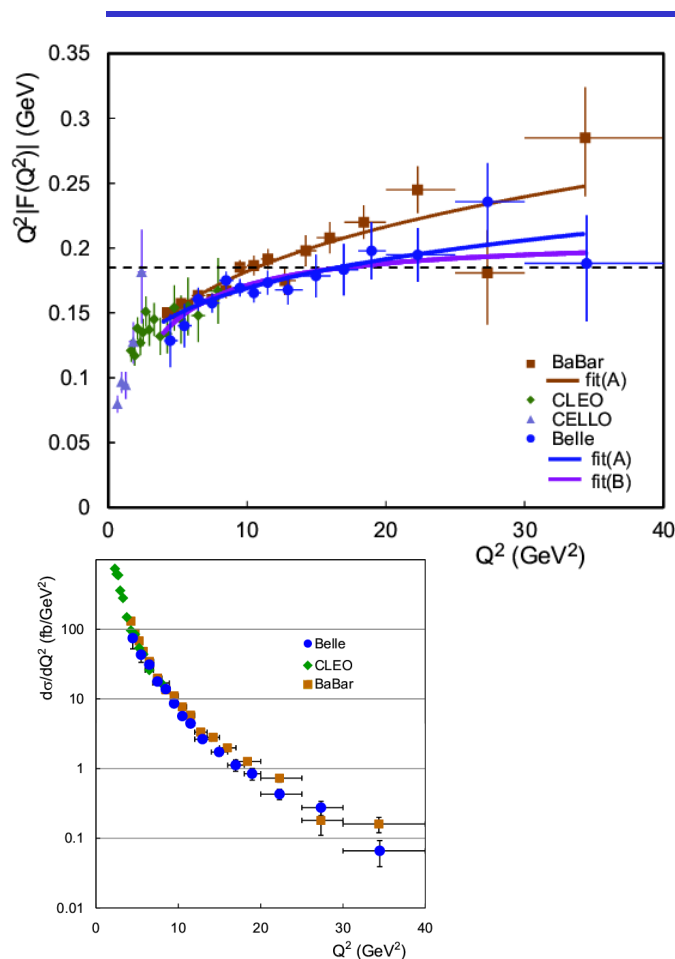
$$|F(0, 0)|^2 = 64\pi\Gamma_{\gamma\gamma}/\{(4\pi\alpha)^2 m_R^3\}$$

Detects  $e$  (tag side) and  $\pi^0$

$Q^2 = 2EE'(1 - \cos \theta)$  from energy and polar angle of the tagged electron



# Comparisons with Previous Measurements and Fits



No rapid growth above  $Q^2 > 9 \text{ GeV}^2$  is seen in Belle result.

$\sim 2.3\sigma$  difference between Belle and BaBar in  $9 - 20 \text{ GeV}^2$

Fit A (suggested by BaBar)

$$Q^2 |F(Q^2)| = A (Q^2/10 \text{ GeV}^2)^\beta$$

BaBar: —

$$A = 0.182 \pm 0.002 (\pm 0.004) \text{ GeV}$$

$$\beta = 0.25 \pm 0.02$$

BaBar, PRD 80, 052002 (2009)

Belle: —

$$A = 0.169 \pm 0.006 \text{ GeV}$$

$$\beta = 0.18 \pm 0.05$$

$$\chi^2/\text{ndf} = 6.90/13 \quad \sim 1.5\sigma \text{ difference from BaBar}$$

Fit B (with an asymptotic parameter)

$$Q^2 |F(Q^2)| = B Q^2 / (Q^2 + C)$$

Belle: —

$$B = 0.209 \pm 0.016 \text{ GeV}$$

$$C = 2.2 \pm 0.8 \text{ GeV}^2$$

$$\chi^2/\text{ndf} = 7.07/13$$

B is consistent with the QCD value (0.185 GeV)



# Selection of the $\pi^0\pi^0$ signals

## Important selection criteria:

One electron and two  $\pi^0$ 's

Three-body kinematics for tagged-e, untagged-e and the  $\pi^0\pi^0$  system

Small acoplanarity angle and pt-balance for tagged-e and the  $\pi^0\pi^0$

