KEK theory center workshop on Hadron and Nuclear Physics in 2017 (KEK-HN-2017) January 7 - 10, 2017 Kobayashi Hall, KEK, Tsukuba, Japan

# Production of ΣNN quasibound states

## **Toru Harada**

Osaka Electro-Communication University/ J-PARC Branch, KEK Theory Center, IPNS, KEK

## **Dynamics in Strangeness Nuclear Systems**



Various effects on the hyperon mixing
Related to the 3BF in nuclei

Keyword: Hyperon-mixing

# Important role of $\Sigma$ hyperons in nuclear matter



**ANN 3BF** 



**PHYSICAL REVIEW C 47, 1000 (1993)** 

Resonances in  $\Lambda d$  scattering and the  $\Sigma$  hypertriton

I.R. Afnan, B.F. Gibson

Separable pot.+Faddeev calc.

"This suggests that a certain class of  $\Lambda N\mathcal{N}\Sigma N$  potentials we can form a  $\Sigma$  hypertriton with a width of about 8 MeV."

Nuclear Physics A 611 (1996) 461-483

#### Structure of the $A = 3 \Sigma$ -hypernuclei

Yoshimitsu H. Koike<sup>a,1</sup>, Toru Harada<sup>b,c,2</sup>

"There exist unstable bound (quasibound) states of S=1/2, T=1 ( $_{\Sigma}{}^{3}$ H,  $_{\Sigma}{}^{3}$ He,  $_{\Sigma}{}^{3}$ n), due to the coupling through the  $\Sigma$ N potential which strongly admixtures  ${}^{3}S_{1}$ ,  $T_{NN}=0$  and  ${}^{1}S_{0}$ ,  $T_{NN}=1$  states in the NN pair."

PHYSICAL REVIEW C 76, 034001 (2007)

 $\Lambda NN$  and  $\Sigma NN$  systems at threshold. II. The effect of D waves

H. Garcilazo, A. Valcarce, T. Fernandez-Carames

Chiral constituent quark model pot+ Faddeev calc. "We find that the  $\Sigma$ NN system has a quasibound state in the (I,J)=(1,1/2) channel very near threshold with a width of about 2.1 MeV. "

## **Our Purpose**

- We demonstrate the inclusive and semi-exclusive spectra in the <sup>3</sup>He(K<sup>-</sup>,π<sup>∓</sup>) reactions theoretically within a distorted-wave impulse approximation by using a coupled (2N-Λ)+(2N-Σ) model with a *spreading* potential.
- Is there a quasibound in  $\Sigma NN$  systems ?

I will focus on

- (1) the structure of the  $\Sigma NN$  quasibound states,
- (2) the  $\Sigma$ NN signal appeared in the  $\pi^-$  and  $\pi^+$  spectra,
- (3) an important role of the channel coupling in  $\Sigma NN$ .

Keyword: Hyperon-mixing

# **Outline**

- 1.  $\Sigma$  hyperon in nuclei (Introduction)
- 2. Calculations
  - Microscopic Y-(2N) folding-model potential
  - $\Sigma$ NN quasibound states  ${}_{\Sigma}^{3}$ He,  ${}_{\Sigma}^{3}$ H,  ${}_{\Sigma}^{3}$ n
  - Production within DWIA (K<sup>-</sup>,  $\pi^-$ ), (K<sup>-</sup>,  $\pi^+$ ) reactions
- 3. Results and Discussion
  - $\pi^-$  and  $\pi^+$  spectra for the  $\Sigma$ NN quasibound states  ${}^{3}_{\Sigma}$ He,  ${}^{3}_{\Sigma}$ n
  - no peak of the  $\pi^+$  spectrum in BNL-E774 data
- 4. Summary

# **1. Σ hyperon in nuclei** (Introduction)

## **Study of a Σ-hyperon in Nuclei (1)**

#### Neutron star core

= "An interesting neutron-rich hypernuclear system"







**Repulsion inside the nucleus and shallow attraction outside the nucleus** 

Due to the insufficient quality of the these data, the potential is not so sensitive to the radial behavior of  $U_{\Sigma}$  inside the nucleus.

## **Study of a Σ-hyperon in Nuclei (3)**



$$U_{\Sigma} = \frac{2}{1 + \exp[(r - R)/a]}$$

(V, W) = (+90 MeV, -40 MeV)

This analysis suggests that the  $\Sigma$ -nucleus potential has a repulsion with a sizable imaginary.

## Inclusive spectrum in ${}^{28}Si(\pi^-, K^+)$ reaction at 1.2GeV/c

Exp. Data from P.K.Saha, H. Noumi, et al., PRC70(2004)044613



 $(V_{\Sigma}, W_{\Sigma}) = (+30, -40)$  MeV by  $\chi^2/N$ -fitting

#### Short-range repulsive core in baryon-baryon intreaction



S = 0 state	[51]	[33]	
1			ΛΛ-ΞΝ-ΣΣ(I=0), H-dibaryon
8 <sub>8</sub>	1		$\Sigma N(I=1/2, {}^{1}S_{0})$ <b>Pauli forbidden</b>
27	4/9	5/9	$NN(^{1}S_{0})$
S = 1 state	[51]	[33]	
8 <sub>A</sub>	5/9	4/9	
10	0.10	1 /0	
10	8/9	1/9	$\Sigma N(I=3/2, S_1)$ almost Pauli forbidden

>SU(6) symm. → Strongly spin-isospin dependence

<u> $\Sigma N$  threshold cusp (I = 1/2, {}^{3}S\_{1}) in K^{-}d \rightarrow \pi^{-}\Lambda p Reactions</u>



## <u>Two-body $\Sigma N$ potentials in free space</u>

Simple, But easy to understand

#### Effective Sigma-nucleon (absorptive) potential : SAP

T.Harara, S.Shinmura, Y.Akaishi, H.Tanaka, NPA507 (1990) 715.

S-matrix equivalent to Nijmegen model-D (model-F)



> There is strong spin-isospin dependence in  $\Sigma N$  potential.

## **Observation of a** ${}^{4}\Sigma$ He Bound State



$$\Sigma^{+} = 7 \pm 0.3$$
 MeV   
(*a*) BNL-AGS  
 $U^{\pi} = 0^{+}$   $T \simeq 1/2$ 

T. Nagae, et al., PRL. 80(1998)1605.

BBBB (T=1/2,S=0) [28\*]: "Strangeness partner of α-particle"



## Baryon-Baryon force in SU(3) basis from lattice QCD

T. Inoue et al., HAL QCD Collaboration, arXiv:1612.08399v1.  $[8] \otimes [8] = [27] \oplus [8_s] \oplus [1] \oplus [10^*] \oplus [10] \oplus [8_a]$ 



# **2.** Calculations

( $\Sigma$ NN quasibound state and its production)

# Y-2N folding-model potentials

Microscopic (2N)-Y folding-model potentials

$$U_{\alpha\alpha'}(\boldsymbol{R}) = \int \rho_{\alpha\alpha'}(\boldsymbol{r}) (\overline{g}_{\alpha\alpha'}(\boldsymbol{r}_1) + \overline{g}_{\alpha\alpha'}(\boldsymbol{r}_2)) d\boldsymbol{r}$$

YN g-matrices obtained by D2'

Nucleon or transition density for NN (CDCC)

$$\rho_{\alpha\alpha'}(\boldsymbol{r}) = \langle \phi_{\alpha}^{(2N)} | \sum_{i} \delta(\boldsymbol{r} - \boldsymbol{r}_{i}) | \phi_{\alpha'}^{(2N)} \rangle$$





Coupled Bethe-Goldstone eq.

$$\begin{bmatrix} \Psi_{\Lambda} \\ \Psi_{\Sigma} \end{bmatrix} = \begin{bmatrix} \Phi_{\Lambda} \\ 0 \end{bmatrix} + \frac{Q}{e} v \begin{bmatrix} \Psi_{\Lambda} \\ \Psi_{\Sigma} \end{bmatrix}$$

## Microscopic Y-(2N) folding-model potentials



 $\succ$  The channel coupling is important to describe the YNN systems.

# $\Sigma NN$ quasibound states

$${}_{\Sigma}^{3}$$
He,  ${}_{\Sigma}^{3}$ H,  ${}_{\Sigma}^{3}$ n  
(T = 1, S = 1/2)

$$(T = 1, S = \frac{3}{2})$$
  $(T = 0, 2, S = \frac{1}{2}, \frac{3}{2})$  repulsive

T. Harada, Y. Hirabayashi, PRC89(2014) 054603.

### Energies and widths of $\Sigma NN$ (S=1/2, T=1)



## Hyperon mixing probabilities of the $\Sigma$ NN states

States	Components	Probabilities (%)
<sup>3</sup> <sub>Σ</sub> He	$ \{pp\}\Lambda  (T = 1) \\ [pn]\Sigma^+ $	2.07 54.9
$\{N_1, N_2\} = N_1 N_2 + N_2 N_1 : {}^1S_0$	$\{pn\}\Sigma^+$ $\{pp\}\Sigma^0$ $T = 1 (I_2 = 0, S_2 = 1)$	$\begin{array}{ccc} 24.7 & 99.6\% \\ 18.3 & 54.9 & (97.4\%) \end{array}$
$[N_1, N_2] = N_1 N_2 - N_2 N_1 : {}^3S_1$	$T = 1 (I_2 = 1, S_2 = 0)$ T = 2	42.5 0.45
$\frac{3}{\Sigma}n$	$\{nn\}\Lambda  (T = 1)$ $[pn]\Sigma^{-}$ $\{pn\}\Sigma^{-}$ $\{nn\}\Sigma^{0}$	2.42 39.5 20.9 37.2 97.9%
	$T = 1 (I_2 = 0, S_2 = 1)$ $T = 1 (I_2 = 1, S_2 = 0)$ T = 2	39.5 56.0 2.10

<u>Production by  $K^-$  beam from <sup>3</sup>He targets</u>



# Distorted-wave impulse approximation (DWIA)



Double differential cross sections within the DWIA

$$\frac{d^2\sigma}{dE_{\pi}d\Omega_{\pi}} = \beta \frac{1}{[J_A]} \sum_{M_A} \sum_{B} |\langle \Psi_B | \hat{F} | \Psi_A \rangle|^2 \,\,\delta(E_{\pi} + E_B - E_K - E_A)$$

Production operators with zero-range interaction

$$\hat{F} = \int d\boldsymbol{r} \, \chi_{\pi}^{(-)*}(\boldsymbol{p}_{\pi},\boldsymbol{r}) \chi_{K}^{(+)}(\boldsymbol{p}_{K},\boldsymbol{r}) \sum_{j=1}^{A} \bar{f}_{(Y\pi)}(\omega_{\bar{K}N}) \delta(\boldsymbol{r}-\boldsymbol{r}_{j}) \hat{O}_{j}$$
Mesons distorted-waves

Momentum and energy transfer

*Transition*-amplitude for  $K^-N \rightarrow \pi Y$ .

$$\boldsymbol{q} = \boldsymbol{p}_K - \boldsymbol{p}_{\pi}, \qquad \omega = E_K - E_{\pi},$$

Kinematical factor

$$\beta = \left(1 + \frac{E_{\pi}^{(0)}}{E_Y^{(0)}} \frac{p_{\pi}^{(0)} - p_K^{(0)} \cos \theta_{\text{lab}}}{p_{\pi}^{(0)}}\right) \frac{p_{\pi} E_{\pi}}{p_{\pi}^{(0)} E_{\pi}^{(0)}},$$

#### Wavefunction of the initial state for a 3He target nucleus

$$|\Psi_A\rangle = \hat{\mathcal{A}} \left[ \left[ \phi_0^{(2N)} \otimes \varphi_0^{(N)} \right]_{L_A} \otimes X_{T_A, S_A}^A \right]_{J_A}^{M_A} \\ X_{T_A, S_A}^A = \left[ \chi_{I_2, S_2}^{(2N)} \otimes \chi_{1/2, 1/2}^{(N)} \right]_{1/2, 1/2},$$

Wavefunctions of final states for ppY

$$\begin{split} |\Psi_B\rangle &= \sum_{\alpha} \left[ \left[ \phi_{\alpha}^{(2N)} \otimes \varphi_{\ell_Y}^{(Y)} \right]_{L_B} \otimes X_{Y_{\alpha},S_{\alpha}}^B \right]_{J_B}^{M_B} \\ X_{Y_{\alpha},S_{\alpha}}^B &= \left[ \chi_{I_2,S_2}^{(2N)} \otimes \chi_{I_Y,1/2}^{(Y)} \right]_{Y_{\alpha},S_{\alpha}}, \end{split}$$

Continuum-discretized coupled-channel (CDCC) w.f.

$$\tilde{\phi}_{\alpha,i}^{(2N)}(\boldsymbol{r}) = \frac{1}{\sqrt{\Delta k}} \int_{k_i}^{k_{i+1}} \phi_{\alpha}^{(2N)}(k,\boldsymbol{r}) dk,$$

The momentum bin method for the pp-systems

 $\left(T_{\alpha} + v_{\alpha}^{(NN)}(\boldsymbol{r}) - \varepsilon_{\alpha}\right)\phi_{\alpha}^{(2N)}(\boldsymbol{k}, \boldsymbol{r}) = 0$ 



R

,

### <u>Fermi-averaged amplitude for $K^-N \rightarrow \pi Y$ elementary processes</u>



Multichannel Green's function  $(N \times N)$ 

$$\sum_{B} |\Psi_B\rangle \langle \Psi_B | \delta(E - E_B) = -\frac{1}{\pi} \text{Im}\hat{G}(E).$$

Morimatsu, Yazaki, NPA483 (1988) 493.

Inclusive spectra for the production cross sections

$$\frac{d^2\sigma}{dE_{\pi}d\Omega_{\pi}} = \beta \frac{1}{[J_A]} \sum_{M_A} S_{\pi}, \qquad S_{\pi} = -\frac{1}{\pi} \operatorname{Im} \langle F | \hat{G}(E) | F \rangle,$$

For 3He(K-, $\pi$ -) reactions Im $\hat{G} = \hat{\Omega}^{(-)\dagger}(\text{Im}\hat{G}^{(0)})\hat{\Omega}^{(-)} + \hat{G}^{\dagger}(\text{Im}\hat{U})\hat{G},$ 

-1

$$S_{\pi^{-}} = S_{\pi^{-}}^{\{pp\}\Lambda} + S_{\pi^{-}}^{[pn]\Sigma^{+}} + S_{\pi^{-}}^{\{pn\}\Sigma^{+}} + S_{\pi^{-}}^{\{pp\}\Sigma^{0}} + S_{\pi^{-}}^{(\text{Conv})} \quad (4 \times 4)$$

$$S_{\pi}^{\alpha} = -\frac{1}{\pi} \langle F | \hat{\Omega}^{(-)\dagger} (\text{Im} \hat{G}_{\alpha}^{(0)}) \hat{\Omega}^{(-)} | F \rangle$$

$$S_{\pi}^{(\text{Conv})} = -\frac{1}{\pi} \sum_{\alpha\alpha'} \langle F | \hat{G}_{\alpha}^{\dagger} W_{\alpha\alpha'} \hat{G}_{\alpha'} | F \rangle$$

For 3He(K-,π+) reactions

$$S_{\pi^+} = S_{\pi^+}^{[pn]\Sigma^-} + S_{\pi^+}^{\{pn\}\Sigma^-} + S_{\pi^+}^{\{nn\}\Sigma^0} + S_{\pi^+}^{(\text{Conv})} \quad (4 \times 4)$$

## Multichannels Green's functions



# **3. Results and Discussion**



Inclusive spectrum in  ${}^{3}\text{He}(K^{-},\pi^{-})$  reactions at 600MeV/c



Inclusive spectrum in  ${}^{3}\text{He}(K^{-},\pi^{+})$  reactions at 600MeV/c



## **Remarks**

- There is a quasibound in  $\Sigma$ NN systems with  $J^p = 1/2^+$ , L = 0, S = 1/2 state.  ${}_{\Sigma}^{3}$ He,  ${}_{\Sigma}^{3}$ H,  ${}_{\Sigma}^{n}$ 
  - The pole is located as  $\mathcal{E}_{\Sigma^{+}}^{(\text{pole})} {3 \choose \Sigma} \text{He} = +0.96 - i \, 4.5 \text{ MeV} \qquad (K^{-}, \pi^{-})$   $\mathcal{E}_{\Sigma^{0}}^{(\text{pole})} {3 \choose \Sigma} n = -0.58 - i \, 5.3 \text{ MeV} \qquad (K^{-}, \pi^{+})$ measured from the  $d + \Sigma^{+}$  threshold.
  - The pole positions reside on the second Riemann sheet [-++] on the complex *E* plane.

 $[\mathrm{Im}k_{\{\mathrm{pp}\}\Lambda},\,\mathrm{Im}k_{[\mathrm{pn}]\Sigma^+}\,,\,\mathrm{Im}k_{\{\mathrm{pn}\}\Sigma^+}\,,\,\mathrm{Im}k_{\{\mathrm{nn}\}\Sigma0}\,]$ 

## Inclusive spectrum by ${}^{3}\text{He}(K^{-},\pi^{+})$ reactions at 600MeV/c

BNL-E774: Barakat, Hungerford, NPA547(1992)157c



*"There is no evidence for a state below*  $\Sigma$ *-d threshold."* Why can we see no peak of the  ${}^{3}{}_{\Sigma}n$  quasibound state?

## Production cross sections on ${}^{3}\text{He}(K^{-},\pi^{-/+})$ reactions

Dover and Gal, PLB110(1982)433

Table 2 Production cross sections on <sup>3</sup>He and width quenching factors Q for states in  ${}_{\Sigma}^{3}$ He and  ${}_{\Sigma}^{3}$ n of spin S, isospin I and core isospin T (I = 0 production is forbidden, since  $I_3 = \pm 1$ ).  $\sigma(K^-,\pi^+)$  $I(T) S Q \sigma(K^{-}, \pi^{-}) \pi^{-}$ 0(1) 1/2 3  $\Sigma[pn] \rightarrow 1(0) 1/2 1/3 3/2 |f_{p \rightarrow \Sigma^{+}}|^{2}$  $3/2 | f_{\mathbf{p} \rightarrow \Sigma^-}$ 1(0) 3/2 4/3 0 

Because Σ[pn] and Σ{pn} states couple each other, we must take into account the coupling effects in the <sup>3</sup>He(K<sup>-</sup>,π<sup>+</sup>) reaction.

## Interference between K-N- $\pi$ Y amplitudes in the spectra (I) For <sup>3</sup>He(K-, $\pi$ -) reactions

$$T^{(K^-,\pi^-)} \simeq f_{\Sigma^0} \langle \{pp\} \Sigma^0 |^3 \operatorname{He} \rangle + f_{\Sigma^+} \langle \{pn\} \Sigma^+ |^3 \operatorname{He} \rangle + f_{\Sigma^+} \langle [pn] \Sigma^+ |^3 \operatorname{He} \rangle$$
$$= \sqrt{\frac{1}{2}} f^{(3/2)} \langle T = 2 |^3 \operatorname{He} \rangle + \sqrt{\frac{1}{2}} f^{(1/2)}_s \langle T = 1_s |^3 \operatorname{He} \rangle + \sqrt{\frac{1}{2}} f^{(1/2)}_t \langle T = 1_t |^3 \operatorname{He} \rangle$$

dynamically admixtures due to the  $\Sigma N$  potential

$$= \sqrt{\frac{1}{2}} \left\{ \sqrt{\frac{1}{2}} f_{\Sigma^{+}} - f_{\Sigma^{0}} \right\} \langle T = 2|^{3} \mathrm{He} \rangle + \left\{ \left( \frac{\sqrt{3}+1}{2} \right) f_{\Sigma^{+}} + \frac{1}{2} f_{\Sigma^{0}} \right\} \langle T = 1^{(-)}|^{3} \mathrm{He} \rangle \xrightarrow{3}{\Sigma} \mathrm{He}_{g.s.}^{3} \mathrm{He}_{g.s.}^{3} + \left\{ \left( \frac{\sqrt{3}-1}{2} \right) f_{\Sigma^{+}} - \frac{1}{2} f_{\Sigma^{0}} \right\} \langle T = 1^{(+)}|^{3} \mathrm{He} \rangle \xrightarrow{3}{\Sigma} \mathrm{He}^{*}_{s.s.}^{3} \mathrm{He}^{*}_{s.}^{3} \mathrm{He}^{*}_{s.}^{3} \mathrm{He}^{*}_{s.s.}^{3} \mathrm{He}^{*}_{s.}^{3} \mathrm{He}^{*}_{s.$$

interference between  $K^-p \rightarrow \pi^-\Sigma^+$  and  $K^-n \rightarrow \pi^-\Sigma^0$  production amplitudes

## Interference between K-N- $\pi$ Y amplitudes in the spectra (II) For <sup>3</sup>He(K<sup>-</sup>, $\pi$ <sup>+</sup>) reactions

This reduction mechanism must appear in  ${}^{3}\text{He}(\text{K}^{-},\pi^{+})$ reactions !

## <u>"There is no evidence for a state below $\Sigma$ -d threshold."</u>



The calculated spectrum is in good agreement with the BNL-E774 data.

## **Remarks**

The calculated inclusive spectrum of the  ${}^{3}\text{He}(\text{K}^{-}, \pi^{+})$  reaction shows no peak of the  ${}^{3}_{\Sigma}n$  quasibound state that is located near the  $\Sigma$ -threshold with the width of 10.5 MeV.

This spectrum is consistent with the BNL-E774 data.



The reason is because the interference effects caused by  ${}^{3}S_{1}$ - ${}^{1}S_{0}$  admixture in the NN pair for  ${}^{3}{}_{\Sigma}n$  and properties of the  $\Sigma$ N interactions.

## **Summary**

## There is a quasibound in ΣNN systems !!

The coupled-channel framework is very important for calculating the spectra of the  ${}^{3}\text{He}(K^{-},\pi^{\mp})$  reactions.

Keyword: Hyperon-mixing

- The calculated spectra of the  ${}^{3}\text{He}(K^{-},\pi^{+})$  reaction may be consistent with the E774 data due to the admixture of the NN core states. the  $\Sigma$ NN structure depending on the 2N-Y potential.
- Both the  $\pi^-$  and  $\pi^+$  spectra provide valuable information to understand the nature of the  $\Sigma NN$  quasibound states and also the YN ( $\Sigma N$ ) interactions.

To determine a quasibound state [+-] or cusp state [-+].

Thank you very much for your attention.