

Theoretical study of the “K-pp” system: Prototype system of kaonic nuclei



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1. Introduction
2. “K-pp” investigated with ccCSM+Feshbach method
 - Outline of the methodology
 - Result with SIDDHARTA constraint for K-p scattering length
 - Double pole of “K-pp”?
3. Discussion on “K-pp”
4. Fully coupled-channel CSM study (On-going)
5. Summary, future plans and remarks

Takashi Inoue (Nihon univ.)
Takayuki Myo (Osaka Inst. Tech.)

1. Introduction

Kaonic nuclei

= Nuclear system with K^{bar} mesons



 K^-

$K^{\text{bar}}N$ two-body system

**Proton**

- Low energy scattering data, 1s level shift of kaonic hydrogen atom
- Hard to describe $\Lambda(1405)$ with Quark Model as a 3-quark state
- Success of Chiral Unitary Model with a meson-baryon picture

Excited hyperon $\Lambda(1405) = K^-$ proton quasi-bound state

Excited hyperon $\Lambda(1405)$

$\Lambda(1405) \ 1/2^-$

$$I(J^P) = 0(\frac{1}{2}^-)$$

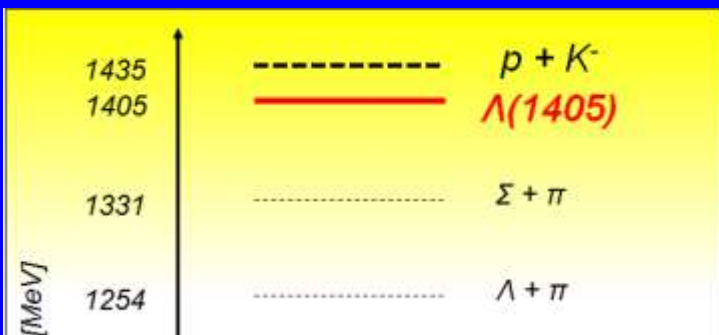
Mass $m = 1405.1^{+1.3}_{-1.0}$ MeV

Full width $\Gamma = 50 \pm 2$ MeV

Below $\overline{K}N$ threshold

$\Lambda(1405)$ DECAY MODES

$\Lambda(1405)$ DECAY MODES	Fraction (Γ_i/Γ)	p (MeV/c)
$\Sigma \pi$	100 %	155



$I=0$ $N-K^{\text{bar}}$ bound state

Not 3 quark state,

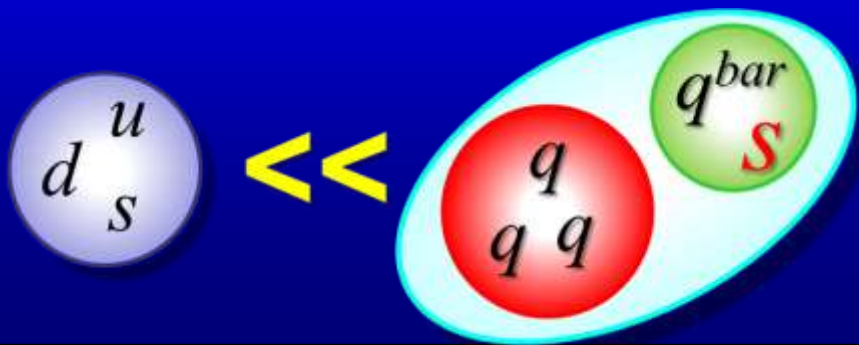
← A naive quark model fails.

N. Isgar and G. Karl, Phys. Rev. D18, 4187 (1978)

But rather a molecular state

T. Hyodo and D. Jido,

Prog. Part. Nucl. Phys. 67, 55 (2012)



K^-

$K^{\text{bar}}N$ two-body system

Proton

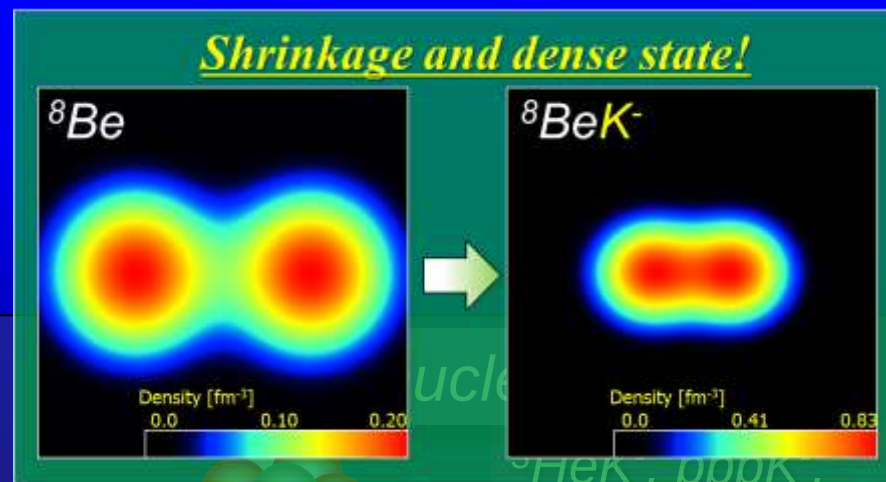
- Low energy scattering data, 1s level shift of kaonic hydrogen atom
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Excited hyperon $\Lambda(1405) = K^-$ proton quasi-bound state

Strongly attractive $K^{\text{bar}}N$ potential

- Doorway to **dense matter**[†]
→ Chiral symmetry restoration in dense matter
- Interesting structure[†]
- Neutron star

[†] A. D., H. Horiuchi, Y. Akaishi and T. Yamazaki, PRC70, 044313 (2004)

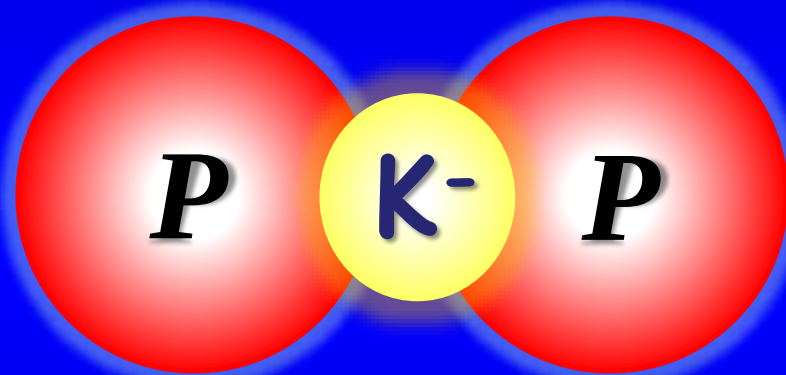


$^4\text{He}K^-$, $pppnK^-$,
..., $^8\text{Be}K^-$, ...

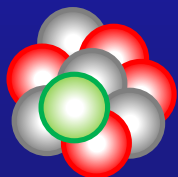


$K^{\text{bar}}N$ two-body system = $\Lambda(1405)$

Proton



Prototype system = $K^- pp$



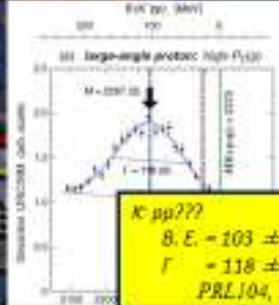
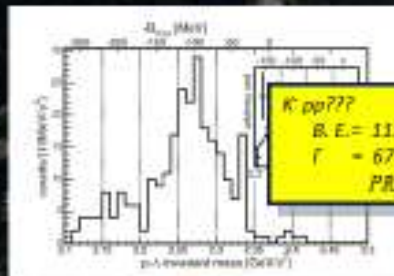
Kaonic nuclei

= Nuclear many-body system with antikaons

Experiments of K⁻pp search

FINUDA

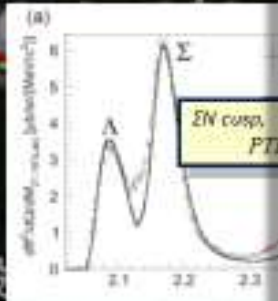
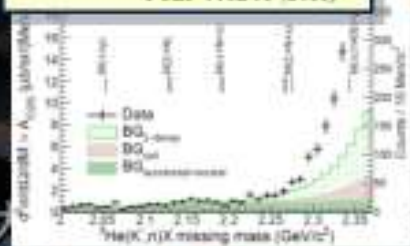
DISTO



J-PARC E15

J-PARC E2

Attraction in K⁻pp subthreshold region
PTEP 061D01 (2015)



Theoretical studies of "K⁻pp"

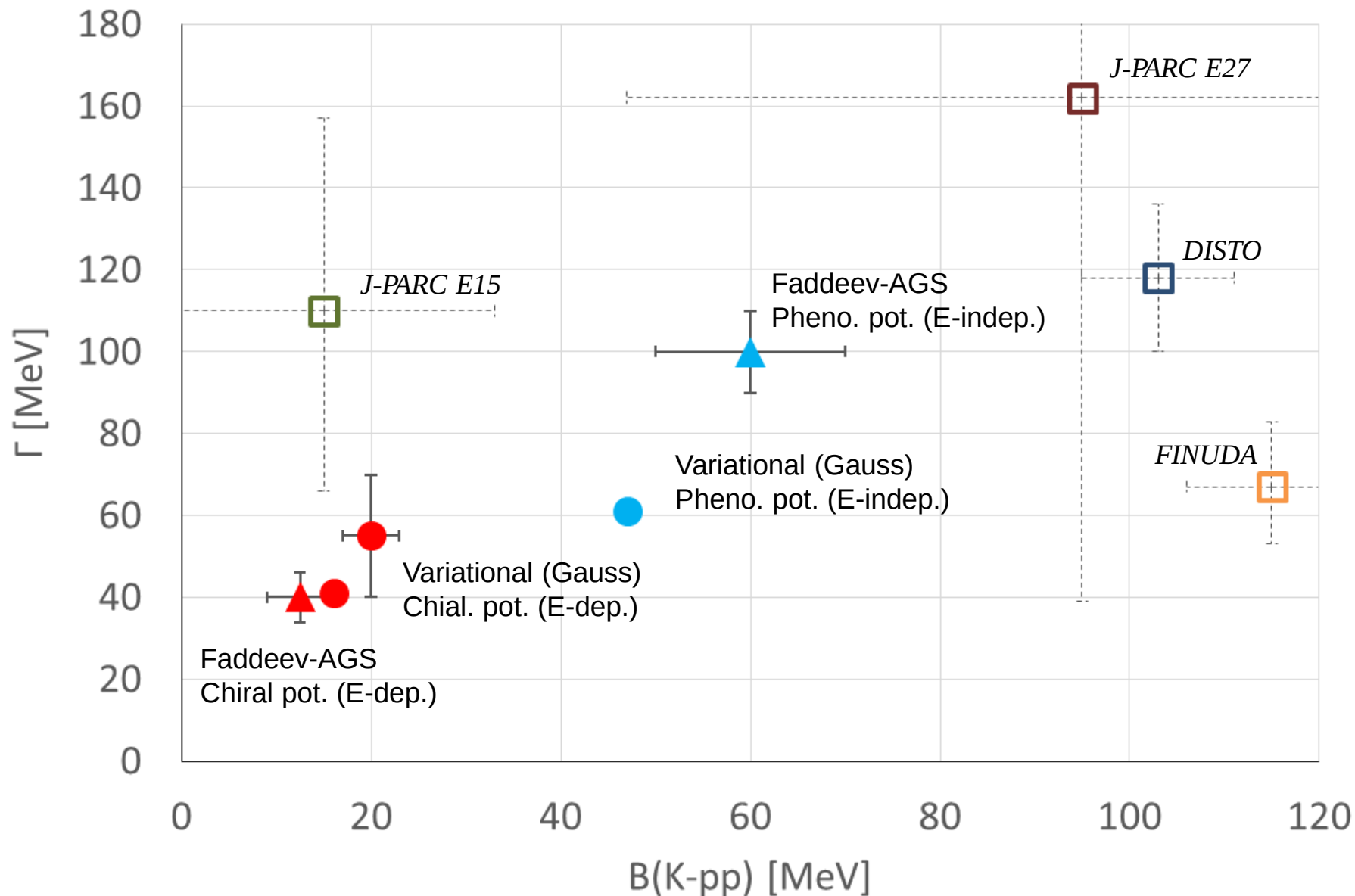
- Variational / Faddeev-AGS approaches
- Chiral / Phenomenological potentials

	Dote-Hyodo-Weise	Barnea-Gal-Liverts	Akaishi-Yamazaki	Ikeda-Kamano-Sato	Shevchenko-Gal-Mares
	PRC79, 014003 (2009)	PLB712, 132 (2012)	PRC76, 045201 (2007)	PTP124, 533 (2010)	PRC76, 044004 (2007)
B(K ⁻ pp)	20 ± 3	16	47	9 ~ 16	50 ~ 70
Γ	40 ~ 70	41	61	34 ~ 46	90 ~ 110
Method	Variational (Gauss)	Variational (H. H.)	Variational (Gauss)	Faddeev-AGS	Faddeev-AGS
Potential	Chiral (E-dep.)	Chiral (E-dep.)	Pheno.	Chiral (E-dep.)	Pheno.

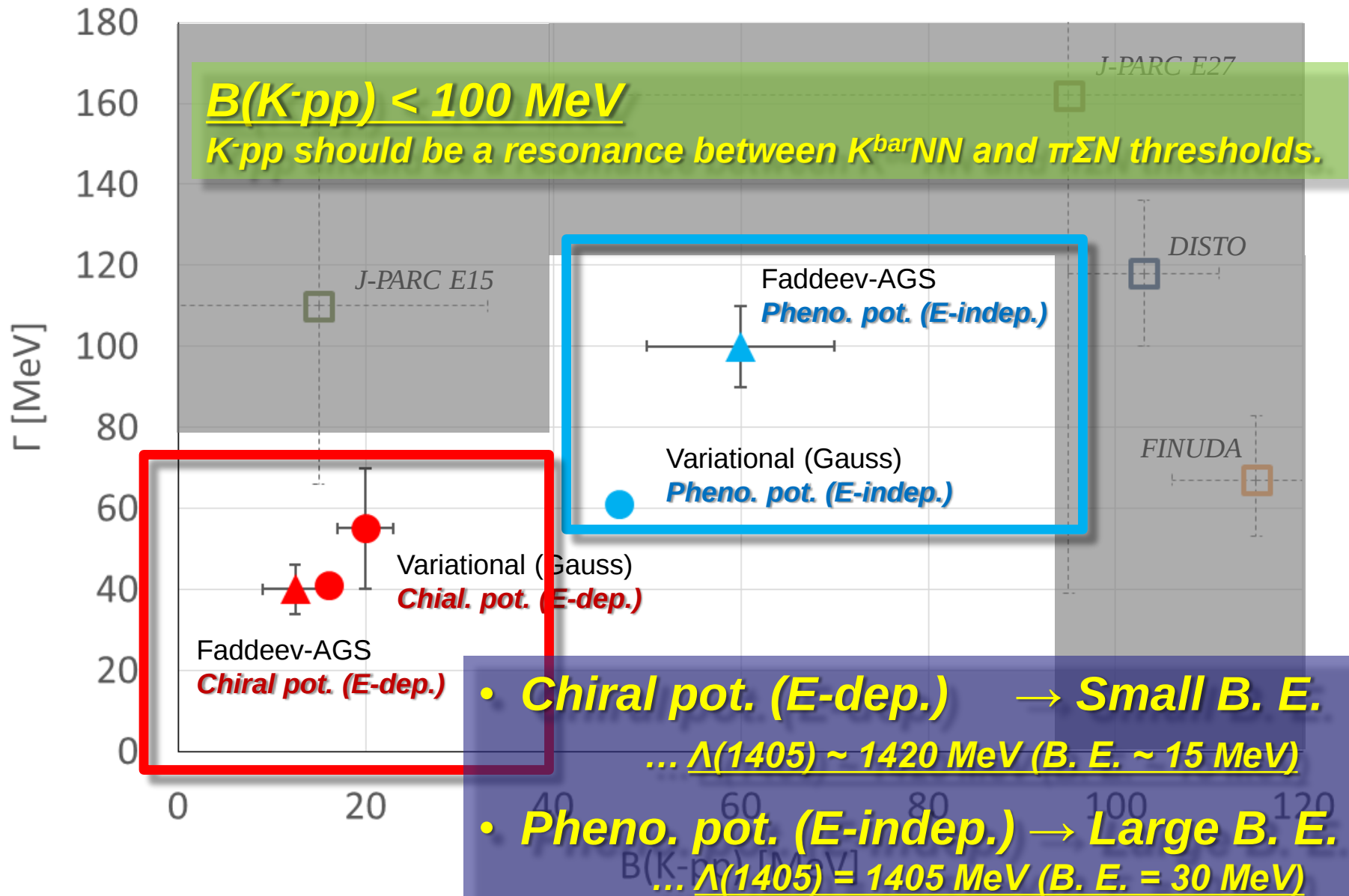
• Latest progress

- Systematic study of kaonic clusters ($A+1 \leq 7$) with Stochastic Variational Method
--> Dr. S. Ohnishi's talk
- Study of kaonic clusters ($A+1, A+2 \leq 4$) with Hyperspherical Harmonics approach in momentum-space
(R. Y. Kezerashvili, et al., arXiv:1510.00478)

Current situation of “K-pp”

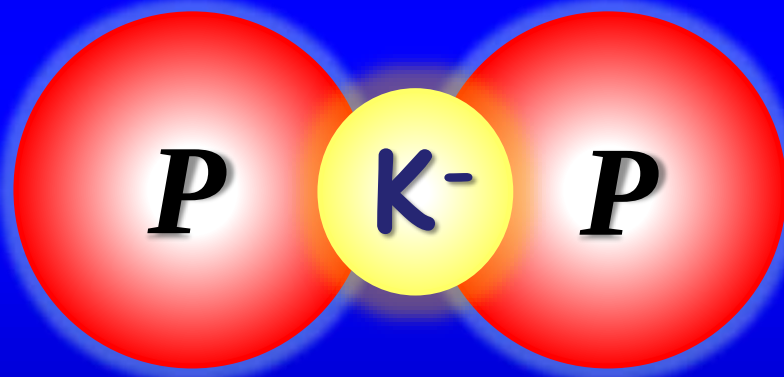


Theoretical studies of “K-pp”



2. “K⁻pp” investigated with ccCSM+Feshbach method

Collaboration with
Takashi Inoue(Nihon univ.)
Takayuki Myo (Osaka Inst. Tech.)



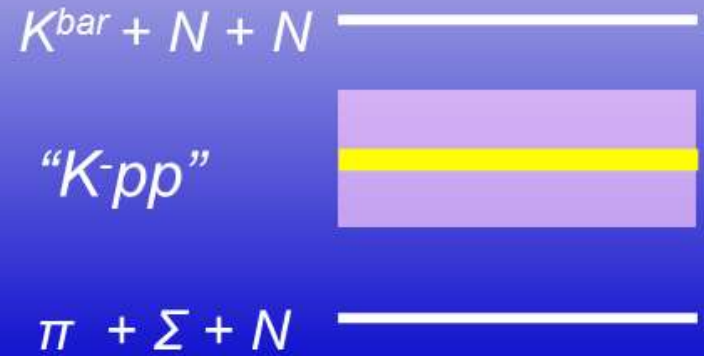
$$\text{“}K^-pp\text{”} = K^{\text{bar}}NN - \pi\Sigma N - \pi\Lambda N \quad (J^\pi = 0^-, T=1/2)$$

- $\Lambda(1405) = \text{Resonant state \& } K^{\text{bar}}N \text{ coupled with } \pi\Sigma$

- “K-pp” ... Resonant state of
 $K^{\text{bar}}NN\text{-}\pi YN$ coupled-channel system

Doté, Hyodo, Weise, PRC79, 014003(2009). Akaishi, Yamazaki, PRC76, 045201(2007)
Ikeda, Sato, PRC76, 035203(2007). Shevchenko, Gal, Mares, PRC76, 044004(2007)
Barnea, Gal, Liverts, PLB712, 132(2012)

- Resonant state
- Coupled-channel system



⇒ “coupled-channel
Complex Scaling Method”

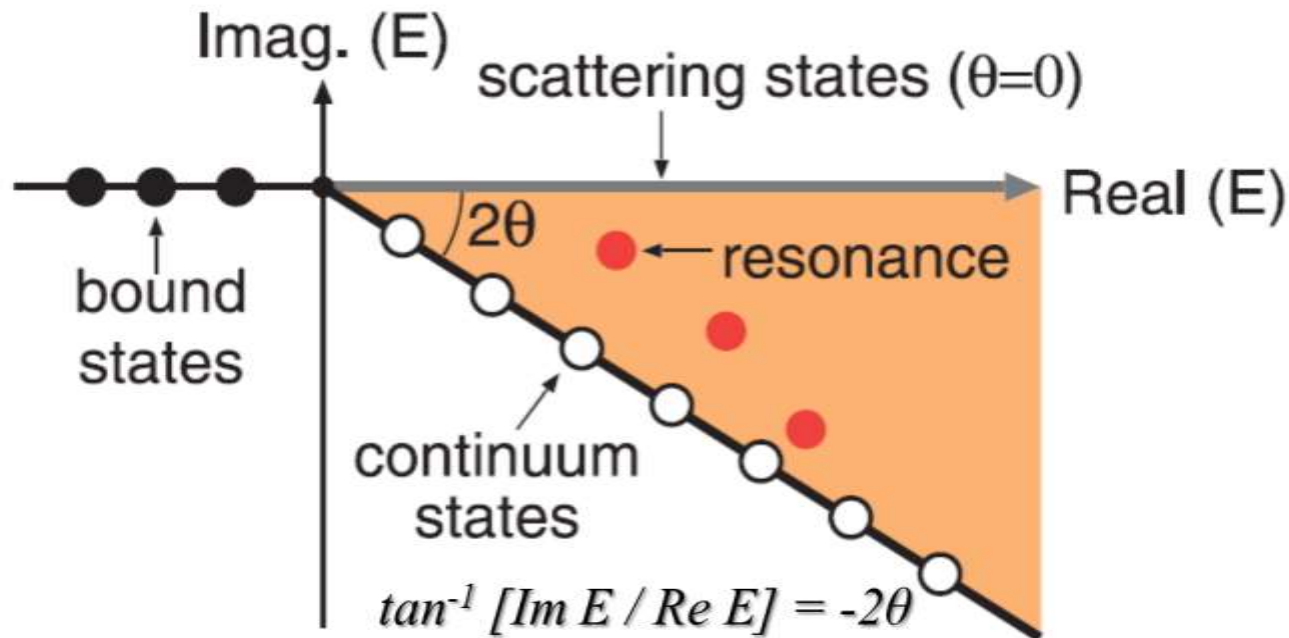
Complex Scaling Method

... *Powerful tool for resonance study of many-body system*

Complex rotation (Complex scaling) of coordinate
Resonance wave function $\rightarrow L^2$ integrable

$$U(\theta): \mathbf{r} \rightarrow \mathbf{r} e^{i\theta}, \quad \mathbf{k} \rightarrow \mathbf{k} e^{-i\theta}$$

Diagonalize $H_\theta = U(\theta) H U^{-1}(\theta)$ with Gaussian base,



- Continuum state appears on 2ϑ line.
- Resonance pole is off from 2ϑ line, and independent of ϑ . (ABC theorem)

Chiral SU(3) potential with a Gaussian form

A. D., T. Inoue, T. Myo, Nucl. Phys. A 912, 66 (2013)

- **Anti-kaon = Nambu-Goldstone boson**

⇒ Chiral SU(3)-based $K^{\text{bar}}N$ potential

- Weinberg-Tomozawa term of effective chiral Lagrangian
- Gaussian form in r -space
- Semi-rela. / Non-rela.
- Based on Chiral SU(3) theory
→ **Energy dependence**

A non-relativistic potential (NRv2c)

$$V_{ij}^{(I=0,1)}(r) = -\frac{C_{ij}^{(I=0,1)}}{8f_\pi^2}(\omega_i + \omega_j) \sqrt{\frac{1}{m_i m_j}} g_{ij}(r)$$

$$g_{ij}(r) = \frac{1}{\pi^{3/2} d_{ij}^3} \exp\left[-(r/d_{ij})^2\right] \quad ; \text{ Gaussian form }$$

ω_i : meson energy

Constrained by $K^{\text{bar}}N$ scattering length

- Old analysis by Martin

$$a_{KN(I=0)} = -1.70 + i0.67 \text{ fm}, \quad a_{KN(I=1)} = 0.37 + i0.60 \text{ fm}$$

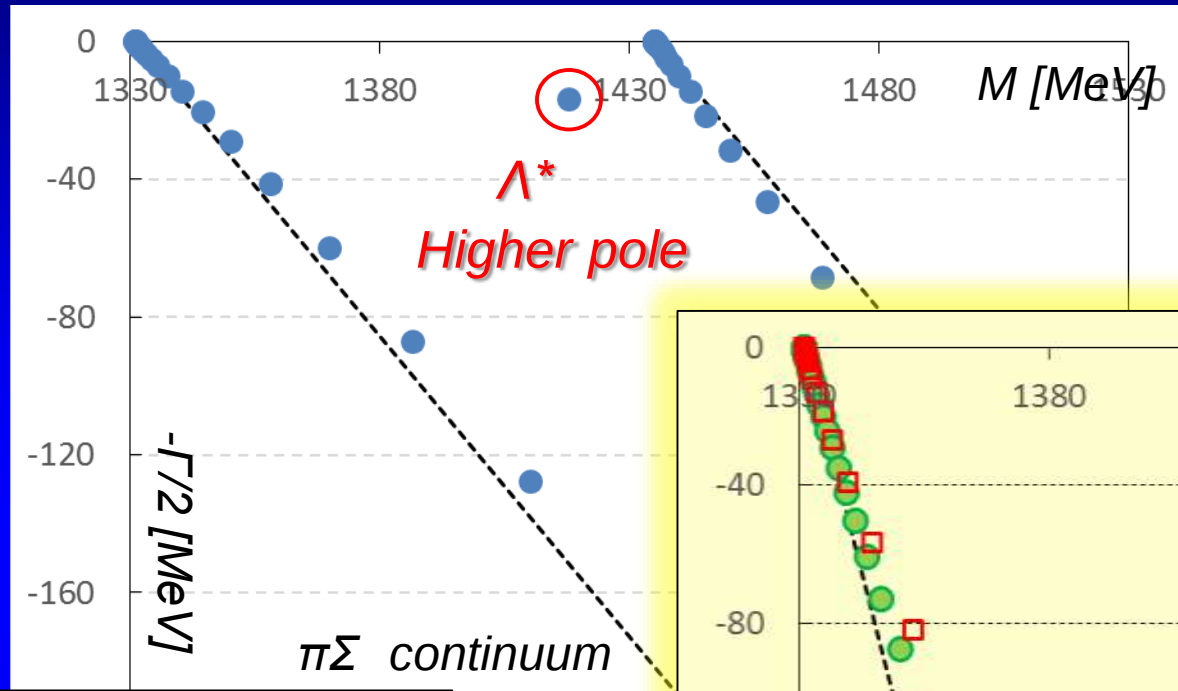
A. D. Martin, NPB179, 33(1979)

- Analysis of **SIDDHARTA Kp data** with **a coupled-channel chiral dynamics**

$$a_{K-p} = -0.65 + i0.81 \text{ fm}, \quad a_{K-n} = 0.57 + i0.72 \text{ fm}$$

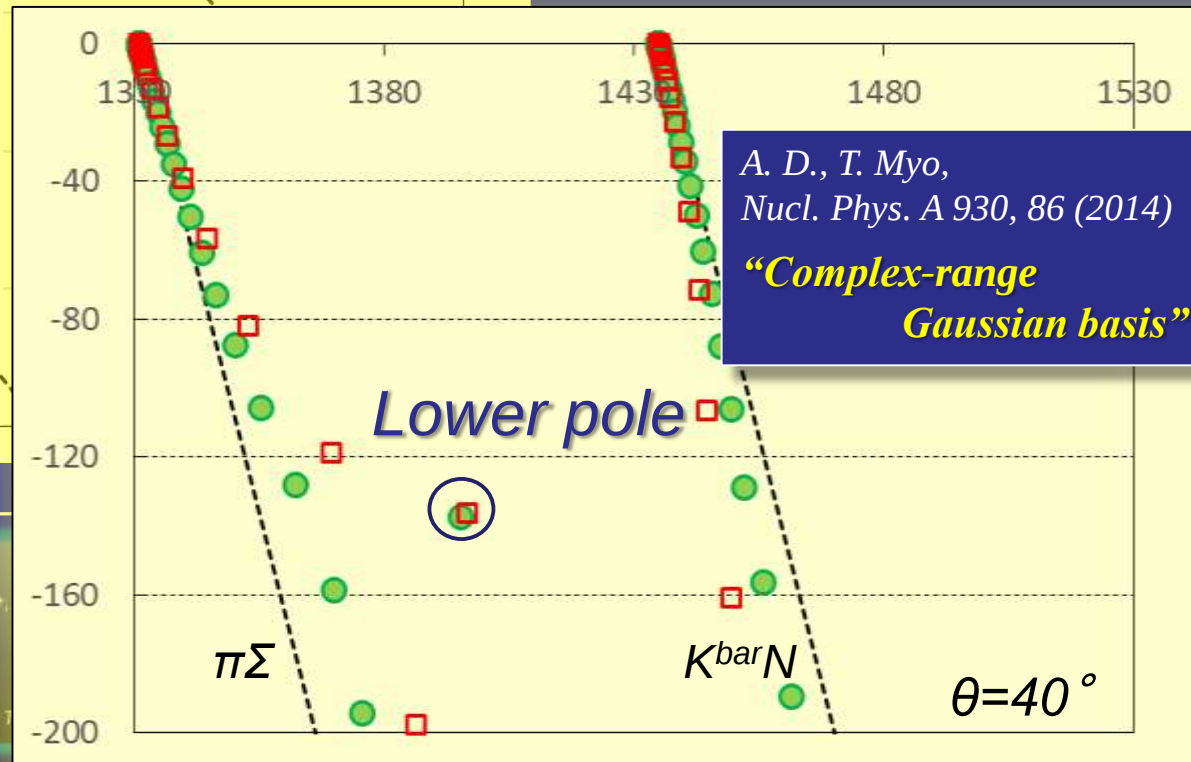
Y. Ikeda, T. Hyodo and W. Weise,
NPA 881, 98 (2012)

$\Lambda(1405)$ pole with a chiral $SU(3)$ -based potential

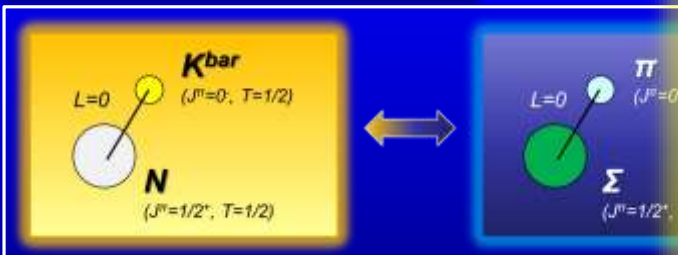


$K^{\text{bar}}N$ potential:
a chiral $SU(3)$ potential
(NRv2, $f_\pi=110$,
Martin constraint)

A. D., T. Inoue, T. Myo,
Nucl. Phys. A 912, 66 (2013)



A. D., T. Myo,
Nucl. Phys. A 930, 86 (2014)
"Complex-range
Gaussian basis"



Double-pole structure of $\Lambda(1405)$

Outline: ccCSM+Feshbach calc. of “ K^-pp ”

A. D., T. Inoue, T. Myo, PTEP 2015, 043D02

$$“K^-pp” = K^{\text{bar}}NN - \pi\Sigma N - \pi\Lambda N \quad (J^\pi = 0^-, T=1/2)$$

Highly computational cost, due to the channel coupling

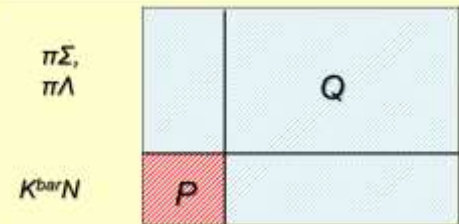
U_{KN}^{Eff}

Derive an effective $K^{\text{bar}}N$ single-channel potential by means of Feshbach projection on CSM.

“Extended Closure Relation”

$$G_q^\theta(E) = \frac{1}{E - H_{QQ}^\theta} \approx \sum_n |\chi_n^\theta\rangle \frac{1}{E - \varepsilon_n^\theta} \langle \chi_n^\theta|$$

$$\int_C \sum_{R+B} |\chi_n^\theta\rangle \langle \chi_n^\theta| = 1$$



$$“K^-pp” = K^{\text{bar}}NN - \pi\Sigma N - \pi\Lambda N \quad (J^\pi = 0^-, T=1/2)$$

$K^{\text{bar}}NN$ single-channel three-body problem with an effective $K^{\text{bar}}N$ potential

Outline: ccCSM+Feshbach calc. of “K⁻pp”

1. Solve the K^{bar}NN three-body Schroedinger eq. with Gaussian Expansion Method

$$\left(T_{K^{bar}NN} + V_{NN} + \sum_{i=1,2} U_{K^{bar}N_i(I)}^{Eff} \left(E_{K^{bar}N} \right) \right) \Phi_{K^{bar}NN} = E \Phi_{K^{bar}NN}$$

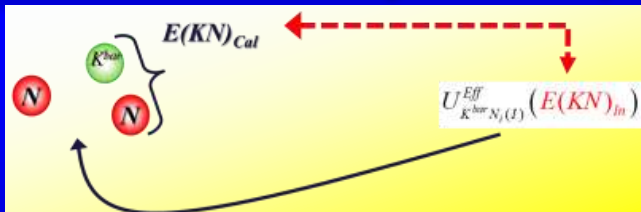
Trial wave function

$$\begin{aligned} |\Phi_{K^{bar}NN}\rangle = & \sum_a C_a^{(KNN,1)} \left\{ G_a^{(KNN,1)}(\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) + G_a^{(KNN,1)}(-\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) \right\} |S_{NN}=0\rangle \left[[K[NN]]_1 \right]_{T=1/2} \rangle \\ & + \sum_a C_a^{(KNN,2)} \left\{ G_a^{(KNN,2)}(\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) - G_a^{(KNN,2)}(-\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) \right\} |S_{NN}=0\rangle \left[[K[NN]]_0 \right]_{T=1/2} \rangle \end{aligned}$$

$$G_a^{(KNN,i)}(\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) = N_a^{(KNN,i)} \exp \left[-(\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) A_a^{(KNN,i)} \begin{pmatrix} \mathbf{x}_1^{(3)} \\ \mathbf{x}_2^{(3)} \end{pmatrix} \right]$$

Basis function = Correlated Gaussian
...including 3-types Jacobi-coordinates

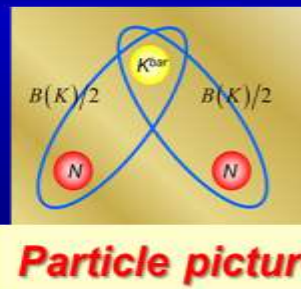
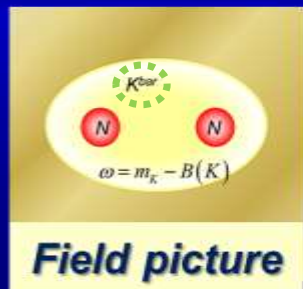
2. Self-consistency for complex K^{bar}N energy



- $E(KN)_{In}$: assumed in the K^{bar}N potential
- $E(KN)_{Cal}$: calculated with the obtained K^{bar}pp

$$E(KN)_{In} = E(KN)_{Cal}$$

3. The energy of a K^{bar}N pair in K⁻pp is estimated in two ways.

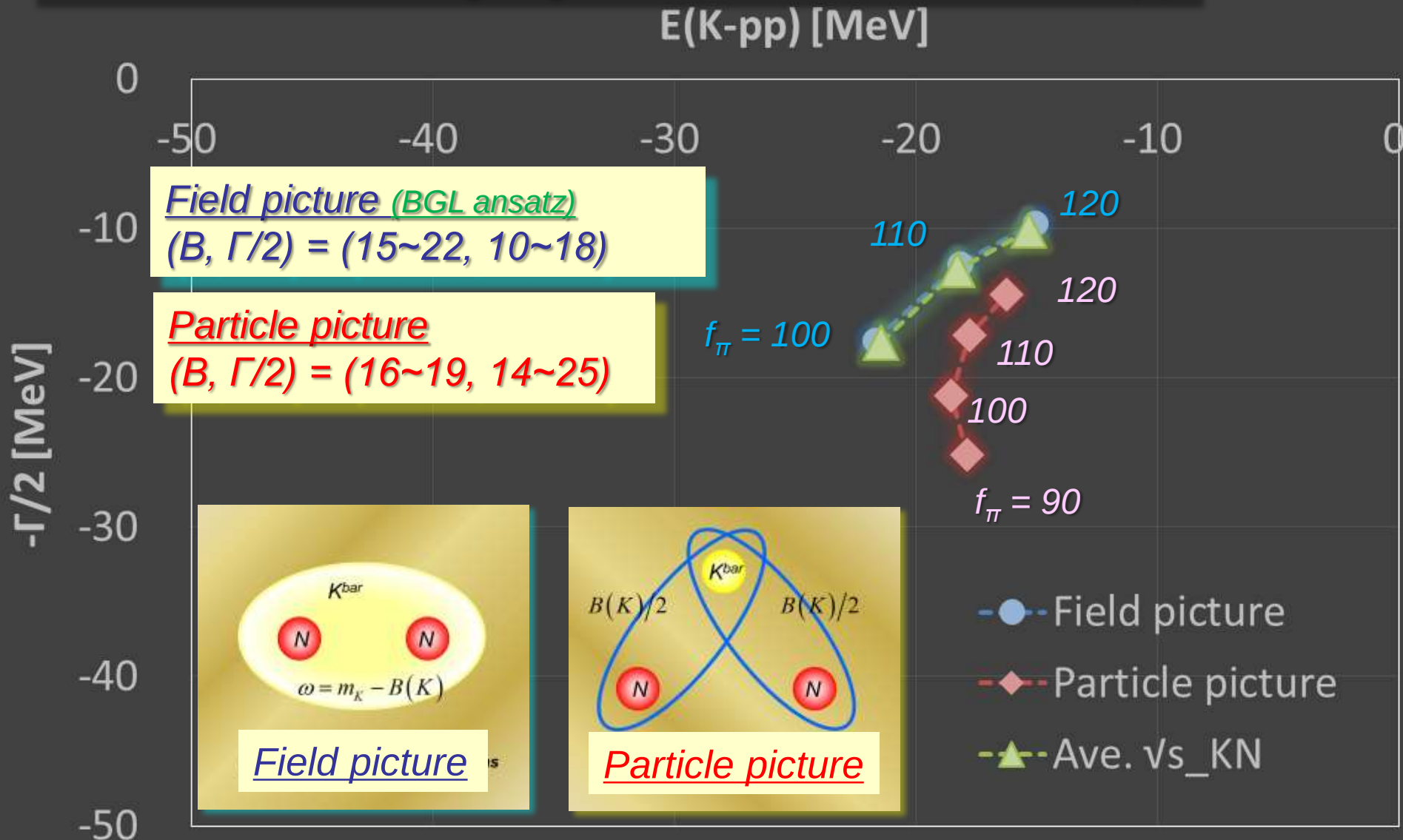


$$E(KN) = M_N + \omega = \begin{cases} M_N + m_K - B(K) & : \text{Field pict.} \\ M_N + m_K - B(K)/2 & : \text{Particle pict.} \end{cases}$$

Pole position of “K-pp”

NN pot. : Av18 (Central)
 K^{bar} N pot. : NRv2a-IHW pot.
 ($\theta = 90 - 120^\circ$)

A chiral SU(3)-based potential constrained with
the latest K^{bar} N scattering length data (based on “SIDDHARTA” exp.)



NN correlation density

NN pot. : Av18 (Central)
 $K^{bar}N$ pot. : NRv2c potential
 $f_{\pi}=110$, Particle pict.

Correlation density in Complex Scaling Method

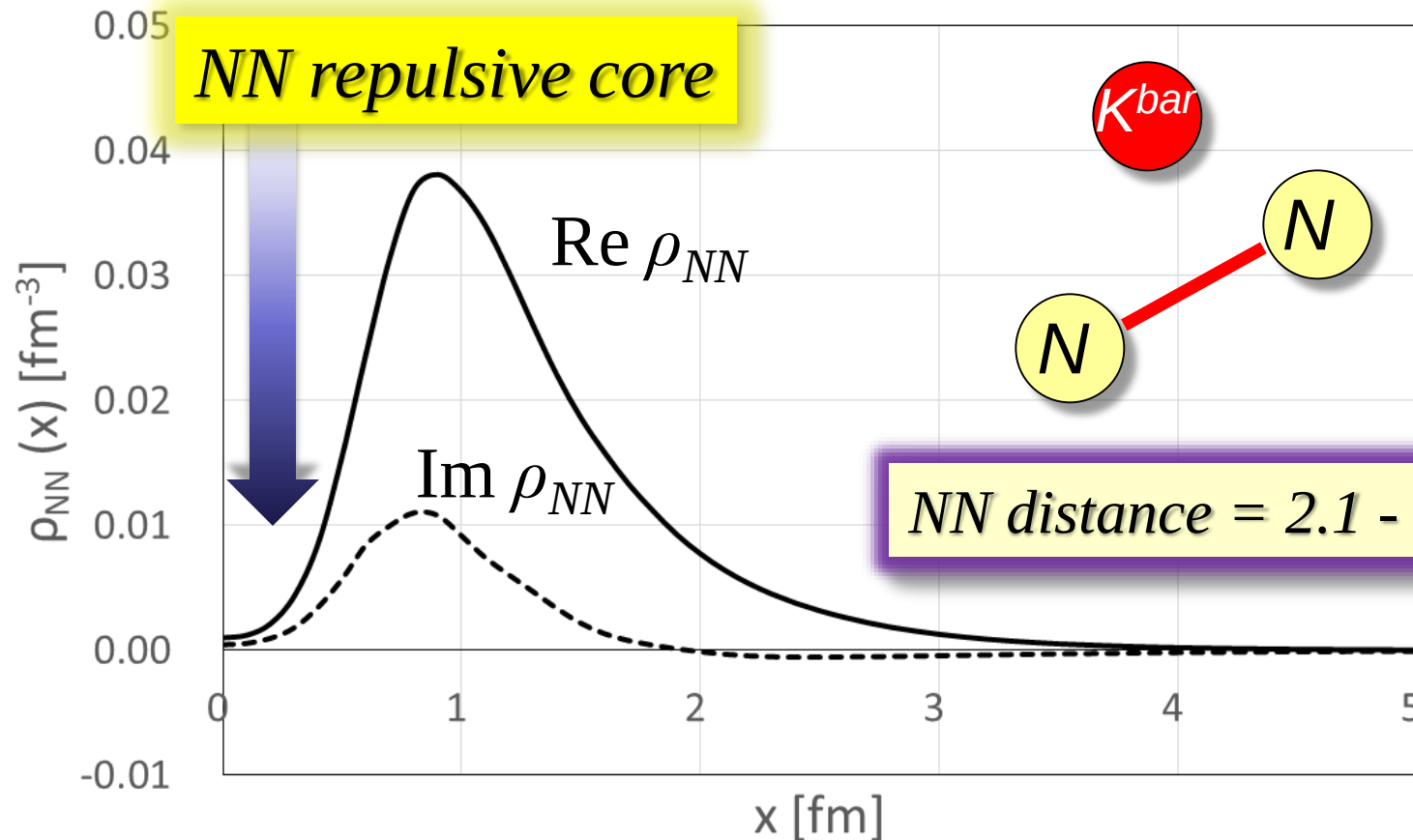
$$\hat{\rho}_{NN,\theta}(\mathbf{x}) = \delta^3(\hat{\mathbf{r}}_{NN,\theta} - \mathbf{x})$$

$$\hat{\mathbf{r}}_{NN,\theta} = \hat{\mathbf{r}}_{NN} e^{i\theta}$$



$$\rho_{NN}(\mathbf{x}) \equiv \langle \tilde{\Phi}_{\theta} | \hat{\rho}_{NN,\theta}(\mathbf{x}) | \Phi_{\theta} \rangle$$

$$= e^{-3i\theta} \int d^3\mathbf{R} \Phi_{\theta}^2(\mathbf{x}e^{-i\theta}, \mathbf{R})$$



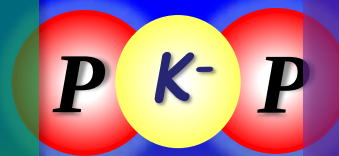
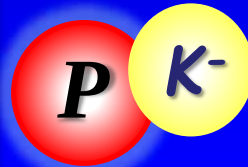
Dense matter or not?

Chiral SU(3) potential (E-dep.)

$$B. E. (\Lambda^*) \sim 15 \text{ MeV} \\ \Rightarrow \Lambda^* = \Lambda(1420)$$

$$B. E. (\text{"K-pp"}) \sim 20 \text{ MeV} \\ NN \text{ distance} \sim 2.2 \text{ fm}$$

$$\Rightarrow \sim \underline{\rho_0} \text{ } (=0.17 \text{ fm}^{-3})$$



Pheno. potential (E-indep.)

Y. Akaishi and T. Yamazaki,
PRC 65, 044005 (2002)

$$B. E. (\Lambda^*) \sim 28 \text{ MeV} \\ \Rightarrow \Lambda^* = \Lambda(1405)$$

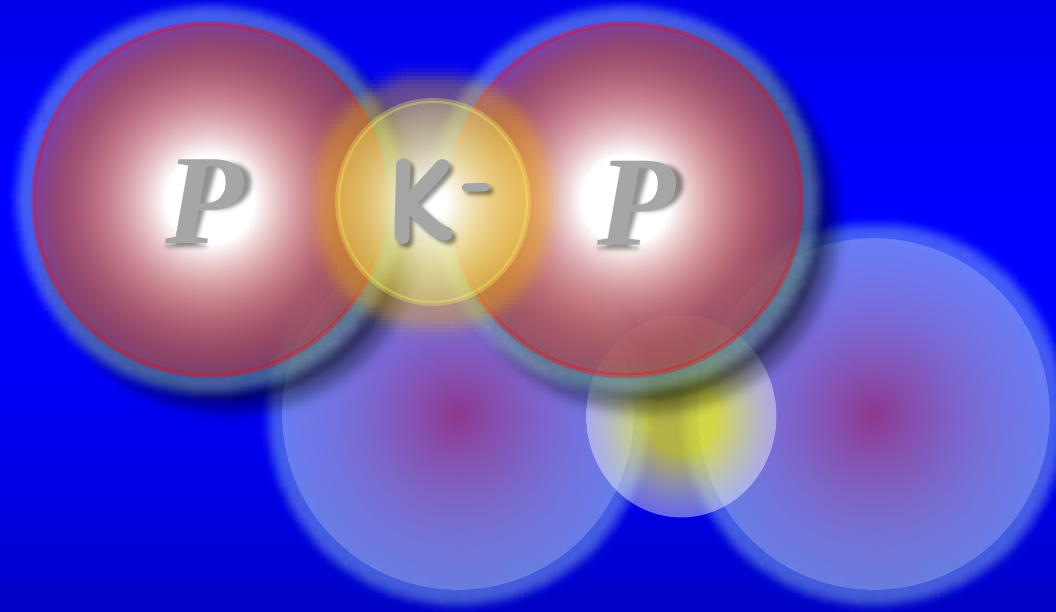
$$B. E. (\text{"K-pp"}) \sim 45 \text{ MeV} \\ NN \text{ distance} \sim 1.9 \text{ fm}$$

$$\Rightarrow \sim \underline{1.6 \rho_0}$$

Normal matter

Dense matter

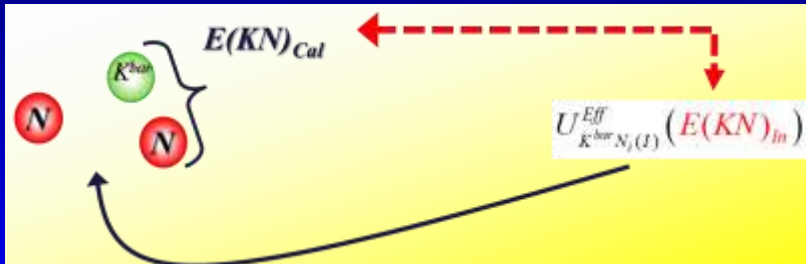
3. Discussion on “K-pp”



Double pole of “K-pp”?

Double pole of “K-pp”?

Chiral pot.
($f_\pi=110$ MeV, Martin)
Particle picture



Indicator of self-consistency

$$\Delta = |E(KN)_{Cal} - E(KN)_{In}|$$

$\Delta=0$ at $E(KN)=(29, 14)$

Self-consistent solution:

$$B(KNN) = 27.3$$

$$\Gamma/2 = 18.9 \text{ MeV}$$

Higher pole?

$\Delta=10$ at $E(KN)=(58, 64)$

Nearly self-consistent solution:

$$B(KNN) = 79$$

$$\Gamma/2 = 98 \text{ MeV}$$

Lower pole??

**“K-pp” has a double-pole structure
similarly to $\Lambda(1405)$?**

(Predicted with chiral unitary approaches

D. Jido, J.A. Oller, E. Oset, A. Ramos, U.-G. Meißner,
Nucl. Phys. A 725 (2003) 181)

K^-pp search at J-PARC

• J-PARC E27

$$d(\pi^+, K^+) \quad P_{\pi} = 1.7 \text{ GeV}/c$$

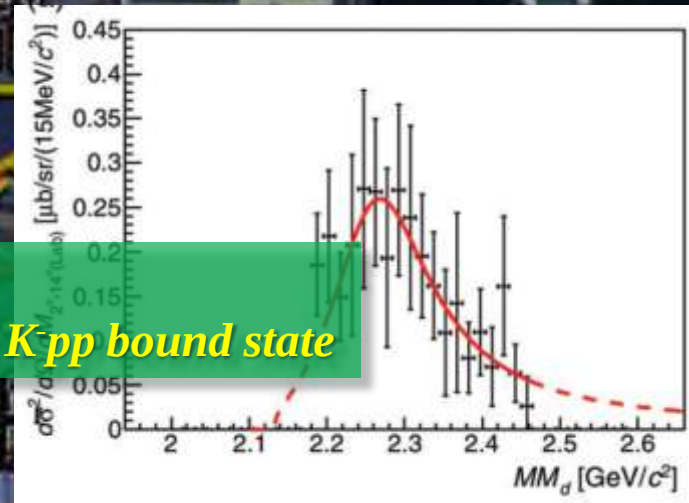
$$Mass = 2275_{-18}^{+17+21} \text{ MeV}$$

$$\Gamma = 162_{-45}^{+87+66} \text{ MeV}$$

$$B_{Kpp} \sim 95 \text{ MeV}$$

if the signal is a K^-pp bound state

Y. Ichikawa et al. PTEP 2015, 021D01



• J-PARC E15 (1st run)

$${}^3\text{He}(\text{inflight } K^-, \Lambda p)n_{\text{missing}} \quad P_K = 1.0 \text{ GeV}/c$$

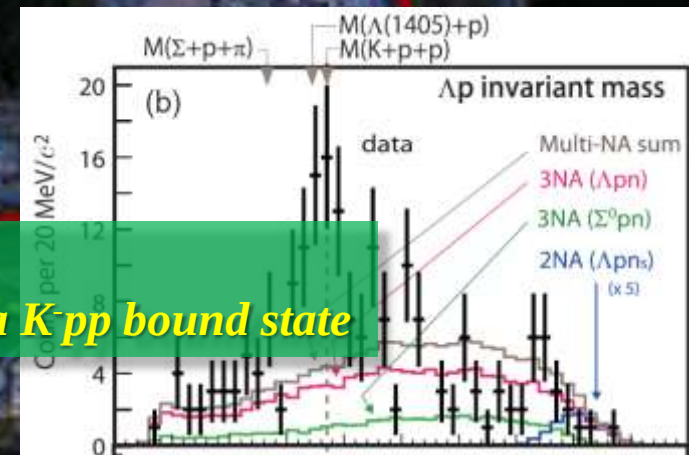
$$Mass = 2355_{-8}^{+6} \pm 12 \text{ MeV}$$

$$\Gamma = 110_{-17}^{+19} \pm 27 \text{ MeV}$$

$$B_{Kpp} \sim 15 \text{ MeV}$$

if the signal is a K^-pp bound state

Y. Sada et al. PTEP 2016, 051D01



Comparison of Theor. and Exp.

DISTO

$$B = 103 \pm 3 \pm 5 \text{ MeV}$$

$$\Gamma = 118 \pm 8 \pm 10 \text{ MeV}$$

J-PARC E27

$$B \sim 95 \text{ MeV}$$

$$\Gamma \sim 162 \text{ MeV}$$

J-PARC E15

$$B \sim 16 \text{ MeV}$$

$$\Gamma \sim 110 \text{ MeV}$$

(Preliminary?)



Double pole with a chiral potential (E-dep.)

ccCSM+Feshbach



$$B = 60\sim 80$$

$$\Gamma = 150\sim 210$$

Faddeev-AGS

Y. Ikeda, H. Kamano, T. Sato,
PTP 124, 533 (2010)



$$B = 67\sim 89$$

$$\Gamma = 244\sim 320$$



$$B = 15\sim 22$$

$$\Gamma = 20\sim 50$$

SIDDHARTA



$$B = 21\sim 32$$

$$\Gamma = 18\sim 64$$

Martin



$$B = 9\sim 16$$

$$\Gamma = 34\sim 66$$

Enhancement of $K^{\text{bar}}N$ interaction (E-indep.)



$$B = 102$$

$$V_{KN} \times 1.17$$



$$B = 52$$

S. Maeda, Y. Akaishi, T. Yamazaki, Proc. Jpn. Acad., Ser. B 89, 418 (2013)



$L=1$ excited state

pion-assisted dibaryon



$$B_{\pi\Sigma N} = 12\sim 20$$

$$\Gamma = 5\sim 8$$

“ $\pi\Lambda N - \pi\Sigma N$ system ($J^\pi = 2^+, T = 3/2$)”

H. Garcilazo, A. Gal, NPA 897, 167 (2013)

4. Fully coupled-channel CSM study (on-going)

$$“K^-pp” = K^{\text{bar}}NN - \pi\Sigma N - \pi\Lambda N \quad (J^\pi = 0^-, T=1/2)$$



Just diagonalize

the Hamiltonian matrix!

$$\begin{array}{c}
 \left[\begin{array}{ccc}
 K^{\text{bar}}NN & K^{\text{bar}}NN & K^{\text{bar}}NN \\
 - K^{\text{bar}}NN & - \pi \Sigma N & - \pi \Lambda N \\
 \hline
 * & \pi \Sigma N & \pi \Sigma N \\
 \hline
 * & - \pi \Sigma N & - \pi \Lambda N \\
 \hline
 * & * & \pi \Lambda N \\
 & & - \pi \Lambda N
 \end{array} \right]
 \end{array}$$

H

θ

ij

No channel elimination!!

- Hamiltonian

$$H = T + V_{NN} + \sum_{\alpha, \beta = K^{bar} N, \pi \Sigma, \pi \Lambda} V_{(MB)\alpha - (MB)\beta}$$



Baryon



Meson



Baryon

- Wave function

$$\begin{aligned} |"K^- pp"> &= \sum_a C_a^{(K\{NN\}+)} G_a^{(K\{NN\}+)}(\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) |S_{NN}=0> \left| [K[NN]_1]_{T=1/2, Tz=1/2} \right> \\ &+ \sum_a C_a^{(K\{NN\}-)} G_a^{(K\{NN\}-)}(\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) |S_{NN}=0> \left| [K[NN]_0]_{T=1/2, Tz=1/2} \right> \\ &+ \sum_a C_a^{(\pi\{\Sigma N\}+)} G_a^{(\pi\{\Sigma N\}+)}(\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) |S_{\Sigma N}=0> \left| [[\pi\Sigma]_0 N]_{T=1/2, Tz=1/2}, \{\Sigma N\}_S \right> \\ &+ \sum_a C_a^{(\pi\{\Sigma N\}-)} G_a^{(\pi\{\Sigma N\}-)}(\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) |S_{\Sigma N}=0> \left| [[\pi\Sigma]_0 N]_{T=1/2, Tz=1/2}, \{\Sigma N\}_A \right> \\ &+ \sum_a C_a^{(\pi\{\Sigma N\}+)} G_a^{(\pi\{\Sigma N\}+)}(\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) |S_{\Sigma N}=0> \left| [[\pi\Sigma]_1 N]_{T=1/2, Tz=1/2}, \{\Sigma N\}_S \right> \\ &+ \sum_a C_a^{(\pi\{\Sigma N\}-)} G_a^{(\pi\{\Sigma N\}-)}(\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) |S_{\Sigma N}=0> \left| [[\pi\Sigma]_1 N]_{T=1/2, Tz=1/2}, \{\Sigma N\}_A \right> \\ &+ \sum_a C_a^{(\pi\{\Lambda N\}+)} G_a^{(\pi\{\Lambda N\}+)}(\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) |S_{\Lambda N}=0> \left| [[\pi\Lambda]_1 N]_{T=1/2, Tz=1/2}, \{\Lambda N\}_S \right> \\ &+ \sum_a C_a^{(\pi\{\Lambda N\}-)} G_a^{(\pi\{\Lambda N\}-)}(\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) |S_{\Lambda N}=0> \left| [[\pi\Lambda]_1 N]_{T=1/2, Tz=1/2}, \{\Lambda N\}_A \right> \end{aligned}$$

Ch. 1: $K^{bar}NN$, $NN=1E$

Ch. 2: $K^{bar}NN$, $NN=1O$

Ch. 3: $\pi\Sigma N$, $[\pi\Sigma]_{l=0}$, $\{\Sigma N\}_{Sym.}$

Ch. 4: $\pi\Sigma N$, $[\pi\Sigma]_{l=0}$, $\{\Sigma N\}_{Asym.}$

Ch. 5: $\pi\Sigma N$, $[\pi\Sigma]_{l=1}$, $\{\Sigma N\}_{Sym.}$

Ch. 6: $\pi\Sigma N$, $[\pi\Sigma]_{l=1}$, $\{\Sigma N\}_{Asym.}$

Ch. 7: $\pi\Lambda N$, $[\pi\Lambda]_{l=1}$, $\{\Lambda N\}_{Sym.}$

Ch. 8: $\pi\Lambda N$, $[\pi\Lambda]_{l=1}$, $\{\Lambda N\}_{Asym.}$

Spatial part: Correlated Gaussian projected onto a parity eigenstate of $B_1 B_2$, including 3 types of Jacobi coordinates

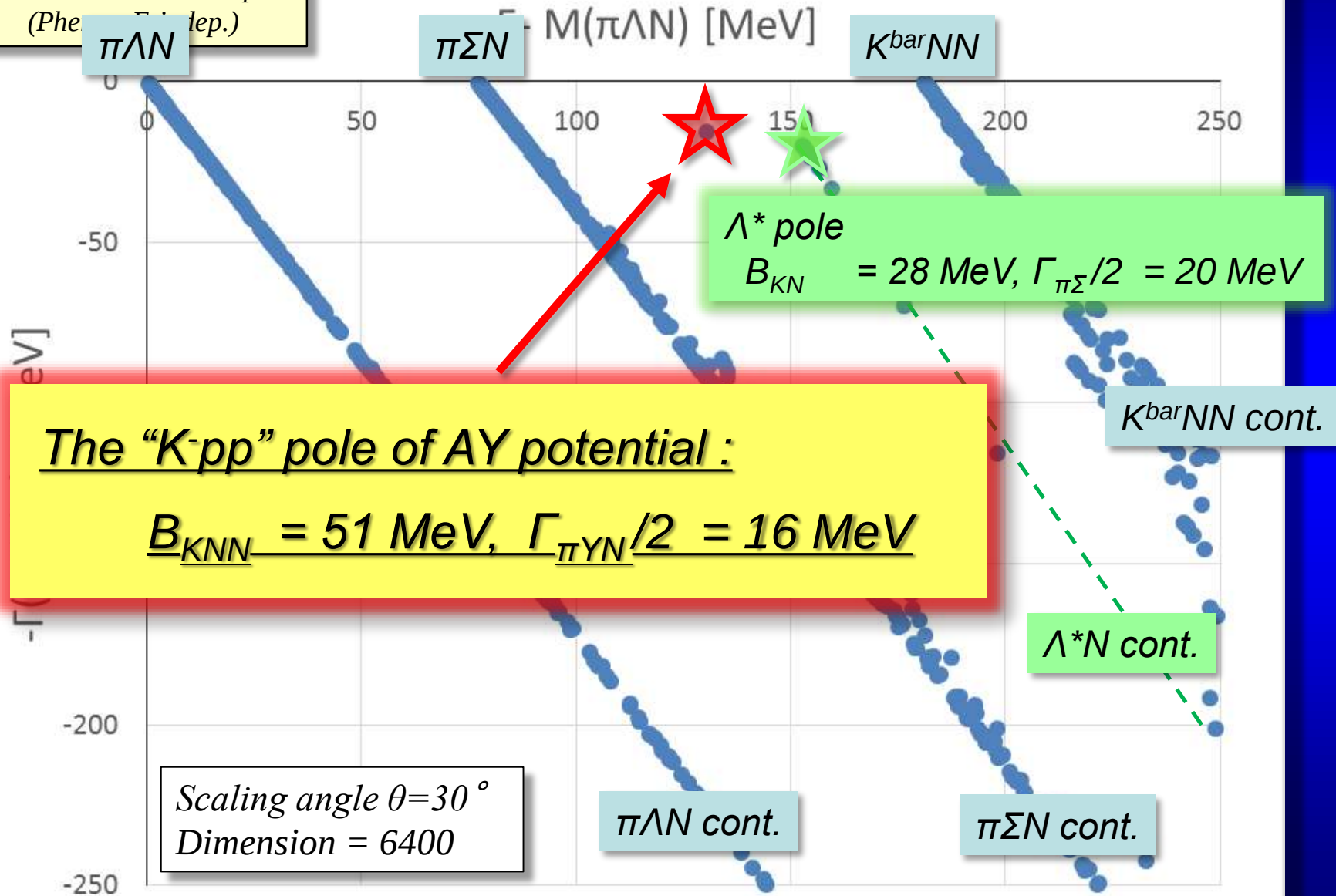
$$G_a^{(X\pm)}(\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) = G_a^{(X)}(\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) \pm G_a^{(X)}(-\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)})$$



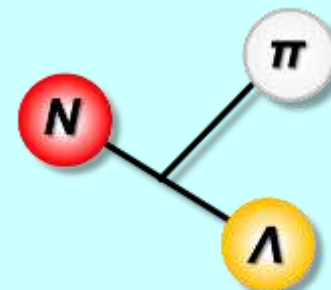
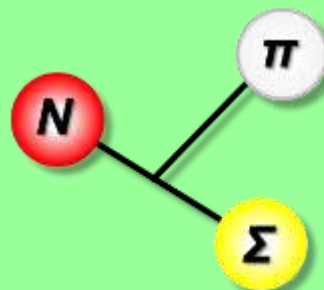
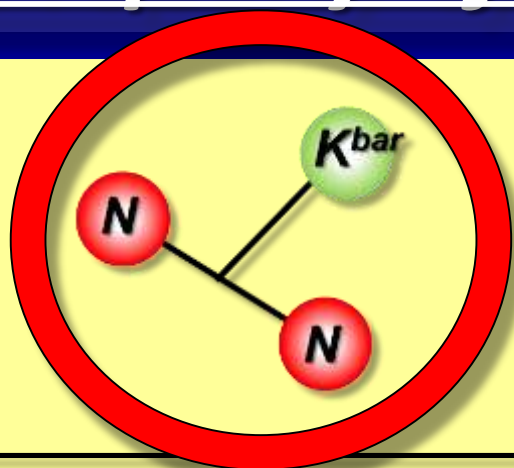
$$G_a^{(X)}(\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) = N_a^{(X)} \exp \left[-(\mathbf{x}_1^{(3)}, \mathbf{x}_2^{(3)}) A_a^{(X)} \begin{pmatrix} \mathbf{x}_1^{(3)} \\ \mathbf{x}_2^{(3)} \end{pmatrix} \right]$$

Complex eigenvalue distribution

NN: Av18 pot.
 $K^{\text{bar}}N-\pi Y$: Akaishi-Yamazaki pot.
 (Phe... lep.)



Property of the “ K^-pp ” pole



Norm $1.004 - i 0.286$

$-0.002 + i 0.276$

$-0.002 + i 0.010$

$K^- N$

$\pi \Sigma$

$\pi \Lambda$

$(l=0) \quad 0.726 - i 0.213$

$(l=0) \quad -0.009 + i 0.261$

$(l=0) \quad ---$

$(l=1) \quad 0.278 - i 0.073$

$(l=1) \quad 0.007 + i 0.015$

$(l=1) \quad -0.002 + i 0.010$

BB distance [fm]

$1.86 + i 0.14$

$1.50 + i 0.48$

$1.10 + i 0.23$

MB distance [fm]

$(l=0) \quad 1.40 - i 0.01$

$(l=0) \quad 0.52 + i 1.31$

$(l=0) \quad ---$

$(l=1) \quad 1.95 + i 0.14$

$(l=1) \quad 0.80 + i 1.22$

$(l=1) \quad 0.74 + i 0.74$

5. Summary, future plans and remarks

5. Summary

A prototype of K^{bar} nuclei, “K-pp” = Resonance state of K^{bar} NN- π YN coupled system

“K-pp” is theoretically investigated in various ways:

Chiral SU(3)-based potential (E-dep.)	→ Shallow binding ... $B(K\text{-pp}) = 10\sim 25$ MeV
Phenomenological potential (E-indep.)	→ Deep binding ... $B(K\text{-pp}) = 50\sim 90$ MeV

All theoretical studies predict $B(K\text{-pp}) < 100$ MeV.

K-pp studied with “coupled-channel Complex Scaling Method + Feshbach projection”

- A chiral SU(3)-based K^{bar} N potential constrained with the latest K^{bar} N scattering length data
 $K\text{-pp} (J^{\pi}=0, T=1/2) \dots (B, \Gamma/2) = (15\sim 22, 10\sim 25)$ MeV (SIDDHARTA constraint)
- A candidate of self-consistent solution is found. ... Deeper binding and larger decay width
 $K\text{-pp} (J^{\pi}=0, T=1/2) \dots (B, \Gamma/2) = (60\sim 80, 75\sim 105)$ MeV (Martin constraint, Particle pict.)

“K-pp” has a double-pole structure similarly to $\Lambda(1405)$?

- The signal observed in J-PARC E27 corresponds to the lower pole of “K-pp”??
J-PARC E15 may pick up the higher pole of “K-pp”???
- NN mean distance of “K-pp” system = 2.1 fm (Chiral pot.), 1.9 fm (AY pot.)
→ **If K^{bar} N potential is so attractive as AY potential,**
kaonic nuclei could be a gateway to dense matter.

5. Future plans and remarks

Future plans:

- **Fully coupled-channel calculation of K^-pp (on-going)**
... E -dep. Chiral $SU(3)$ pot. case, Detail study for the double pole structure, etc
- Application to resonances of other hadronic systems

Remaining issues:

1. Spectrum calculations with reaction mechanism, for the comparison with experimental result

Earlier works on $^3\text{He}(\text{in-flight } K^-, n)$ reaction: -->> T. Sekihara, E. Oset and A. Ramos, arXiv: 1607.02058
T. Koike and T. Harada, PRC80, 055208 (2009) (PTEP in press)
J. Yamagata-Sekihara, D. Jido, H. Nagahiro and S. Hirenzaki, Phys. Rev. C 80, 045204 (2009)

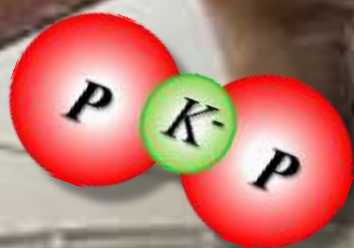
Poles obtained in theoretical study = on the **complex** energy plane
Observables measured in experiments = on the **real** energy axis

2. Non-mesic decay of “ K^-pp ” (two nucleon absorption, “ K^-pp ” --> YN)?

Most of theoretical calculations of the “ K^-pp ” pole position consider only mesic-decay mode, not non-mesic decay mode. Need to be careful when comparing with experimental results.

3. Nature of $\Lambda(1405)$ and $K^{\text{bar}}N$ interaction

How strongly attractive is the $K^{\text{bar}}N$ interaction? “ $\Lambda(1405)$ vs $\Lambda(1420)$ ”



Thank you for your attention!

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NPA 912, 66 (2013)
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3. A. D., T. Inoue, T. Myo,
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4. A. D., T. Inoue, T. Myo,
JPS Conf. Proc. (Proc. of HYP2015)
(to be published)

Cats in KEK