

# Kaon bound states formation by Kaon beam

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Junko Yamagata (Nara Women's Univ. D1)

Hideko Nagahiro (RCNP, Osaka Univ.)

Satoru Hirenzaki (Nara Women's Univ.)

J. Yamagata, H. Nagahiro, Y. Okumura and S. Hirenzaki,  
Prog. Theor. Phys. 114, 301 (2005)

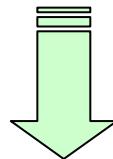
J. Yamagata, H. Nagahiro and S. Hirenzaki, Phys. Rev. C 74, 014604 (2006)

# Introduction

R. Seki, C. E. Wiegand Ann. Rev. Nucl. Part. Sci. 25(75)241.  
C. J. Batty, E. Friedman and A. Gal, Phys. Rep. 287(97)385.  
S. Hirenzaki et al., Phys. Rev. C61(00)055205.  
many others.....

- Study of Kaonic Atoms --- for long time
  - To know the kaon properties at finite density,  
K-A interaction
  - X-ray spectroscopy
    - Deeply bound state were **not be observed.**

- ★ Deeply Bound Pionic Atoms observed by ( $d$ ,  ${}^3\text{He}$ ) reactions.
- ★ New facility    J-PARC    --- Coming Soon!!



We can expect **kaonic bound states** formation  
by using the  $(K^-, p)$  reaction.  
Theoretical  $(K^-, p)$  spectra  
→ Important!! Before experiment.

# Introduction

(Kaonic Atoms +  
Kaonic Nuclei, **Both!!**)

## □ Our Studies

- Theoretical Comprehensive spectra  
→ We can also check the contributions  
from Kaonic Nuclear states in the calculated spectra.

Kishimoto Group, Iwasaki, Suzuki Group, FINUDA Group  
Akaishi, Yamazaki, Dote  
Oset, Toki

- Predict new Kaon-Nucleus bound systems  
( Deeply bound Kaonic Atoms and Kaonic Nuclei )  
formation by Kaon beam.

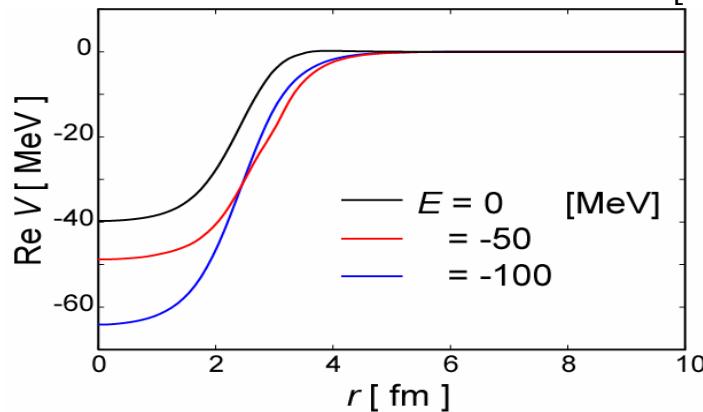
- Structure of Kaon-Nucleus bound systems (Atom + Nucleus)
  - Energy-Dependent optical potentials  
Chiral Unitary Model, Phenomenological Model
- Theoretical formation spectra in (In-Flight  $K^- p$ ) reaction

# Formulation -- Structure

## □ Klein-Gordon equation

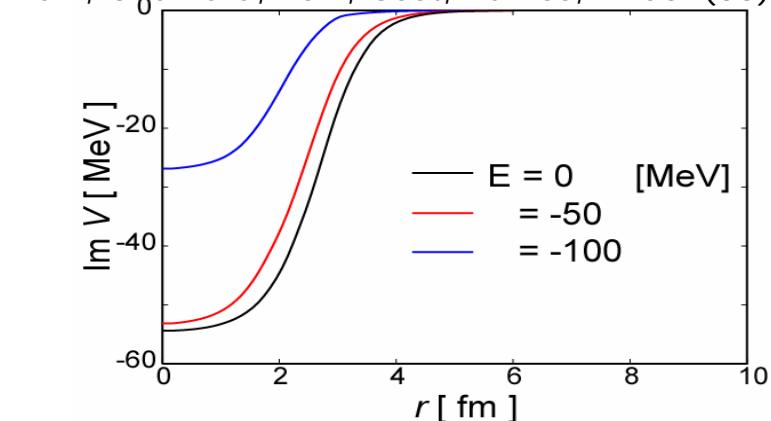
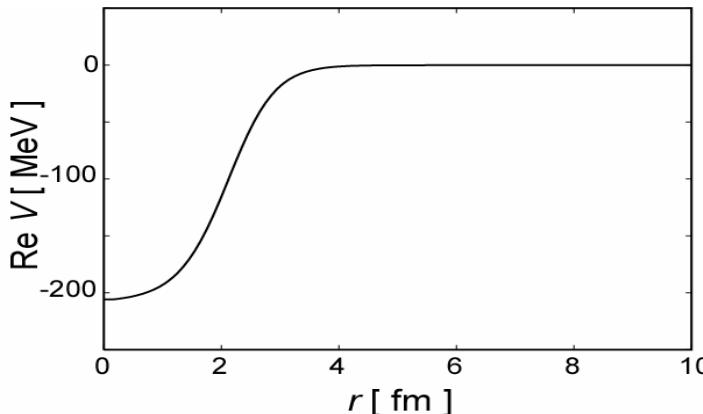
$$[-\vec{\nabla}^2 + \mu^2 + 2\mu V_{\text{opt}}(r, E)]\phi(\vec{r}) = [\omega - V_{\text{coul}}(r)]^2 \phi(\vec{r})$$

### Chiral Unitary Model

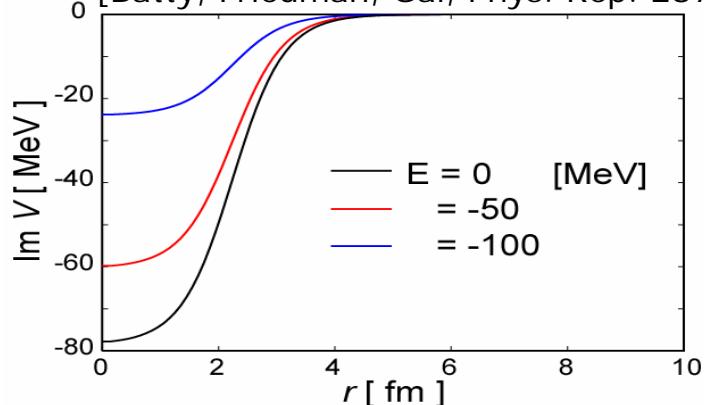


[A. Ramos, E. Oset, NPA671(00)481]  
[Hirenzaki, Okumura, Toki, Oset, Ramos, PRC61(00)055205]

### Phenomenological Model

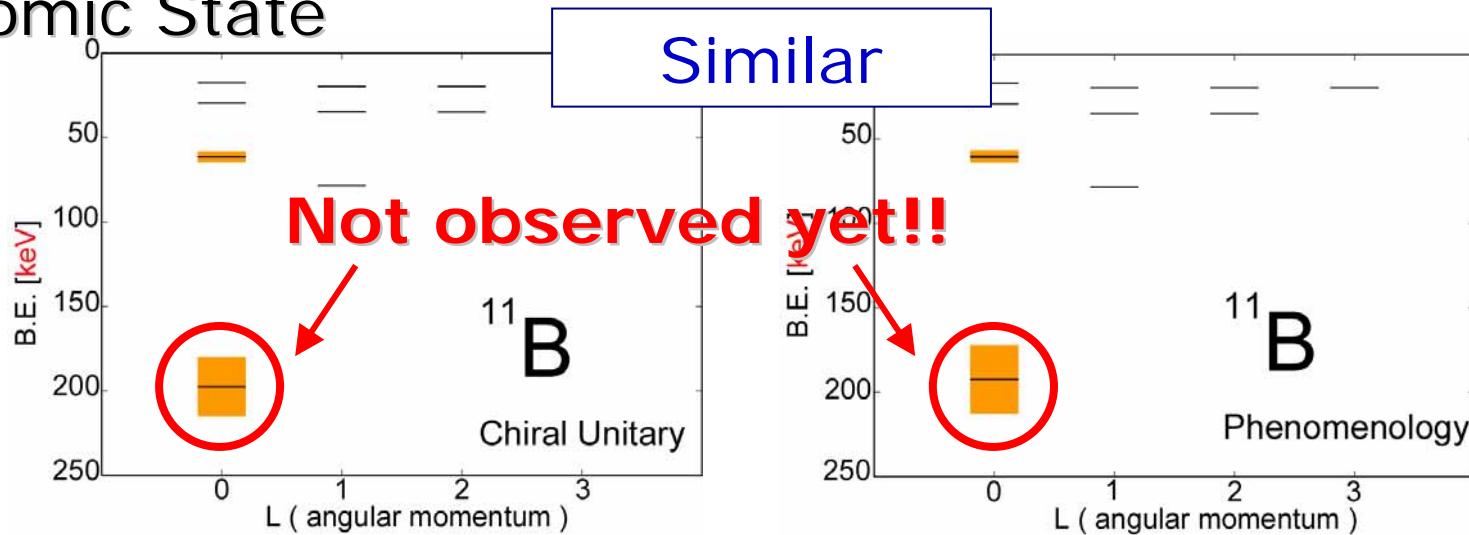


[J. Mareš, E. Friedman, A. Gal, Phys. Lett. B606(2005)295]  
[Batty, Friedman, Gal, Phys. Rep. 287(97)385]

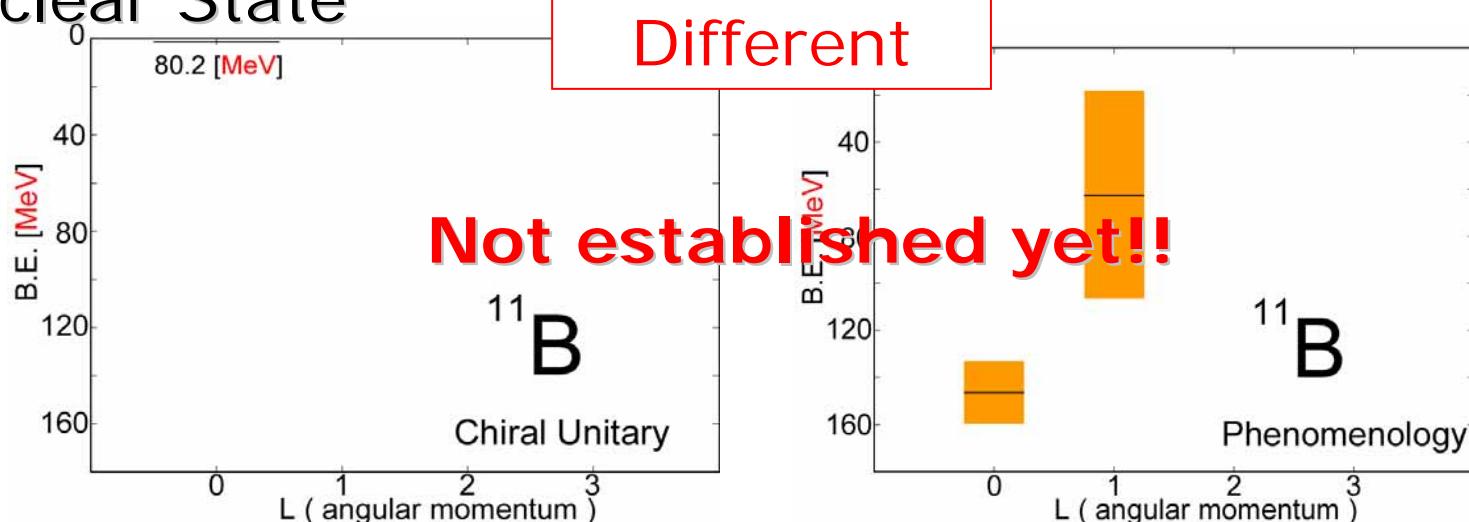


# Energy level ( Energy dep. V<sub>opt</sub> )

## Atomic State

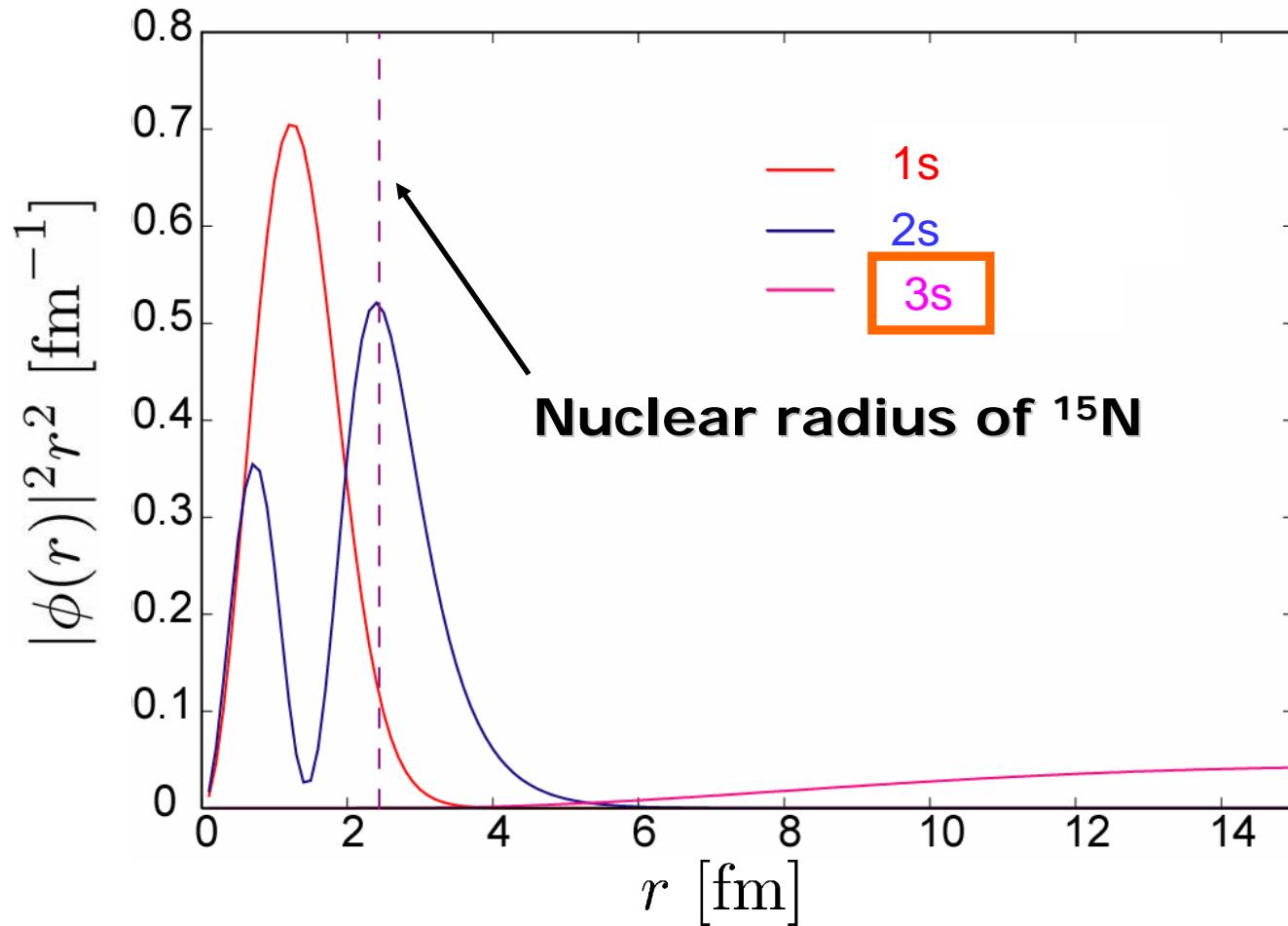


## Nuclear State



# Wave Function

## Phenomenology



# Formulation -- Reaction (In-flight $K^-$ , $p$ )

## □ Green Function Method

J. Yamagata et al., Phys. Rev. C 74 (06) 014604

O. Morimatsu, K. Yazaki NPA435(85)727, NPA483(88)493

$$\frac{d^2\sigma}{dEd\Omega} = \left( \frac{d\sigma}{d\Omega} \right)_{K^-p \rightarrow pK^-} - \frac{1}{\pi} \text{Im} \int d\vec{r} d\vec{r}' f_\alpha^*(\vec{r}') G(E; \vec{r}', \vec{r}) f_\alpha(\vec{r})$$

- $\left( \frac{d\sigma}{d\Omega} \right)_{K^-p \rightarrow pK^-}$  : Elementary cross section (Exp. data)
- $G(E; \vec{r}', \vec{r})$  : Green function for K interacting with the nucleus  
 $(H_{K^-} - E)G(E; \vec{r}', \vec{r}) = \delta^3(\vec{r} - \vec{r}')$
- $f_\alpha(\vec{r}) = \chi_p^*(\vec{r}) \chi_K(\vec{r}) \langle \alpha | \psi_p(\vec{r}) | i \rangle$
- Previous work: Effective Number Approach

$$\frac{d^2\sigma}{d\Omega dE} = \sum \frac{\Gamma_K}{2\pi} \frac{1}{\Delta E^2 + \Gamma_K^2/4} N_{\text{eff}} \left( \frac{d\sigma}{d\Omega} \right)_{K^-p \rightarrow pK^-} \quad (\text{J. Yamagata et. al., PTP114(05)301})$$

$$\Delta E = T_p - (T_K - S_p(j_p^{-1}) + B.E.(nl))$$

$$N_{\text{eff}} = \sum_{JMm_s} \left| \int \chi_p^*(\vec{r}) \xi_{\frac{1}{2}m_s}^*(\sigma) [\phi_{L_K}(\vec{r}) \otimes \psi_{j_p}(\vec{r}, \sigma)]_{JM} \chi_K(\vec{r}) d^3r d\sigma \right|^2$$

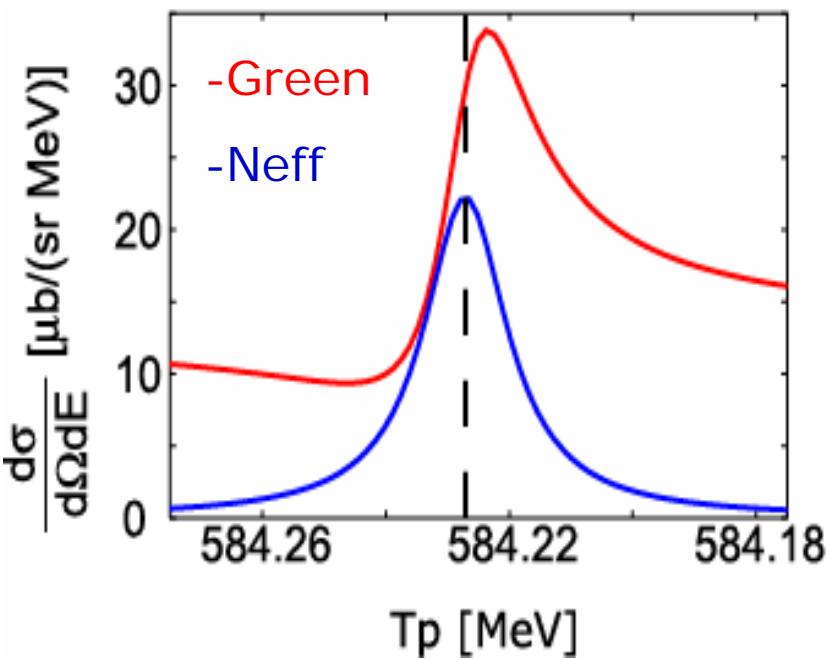
→  $^{12}\text{C}$  is interesting !

# Energy Spectrum (Green vs. Neff)

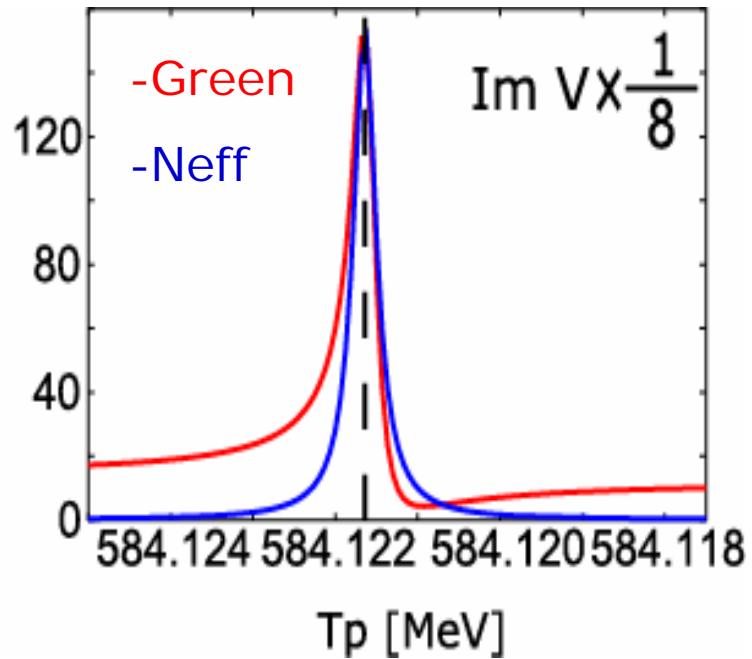
Atomic State

- $\square$   $^{12}\text{C}(\text{In-flight } K^-, p) \quad P_{K^-} = 976 \text{ MeV/c} \quad (T_{K^-} = 600 \text{ MeV})$
- $\square$   $V_{\text{opt}}$  : Chiral Unitary Model ( $E = 0$ )
- $\square$  state:  $(s, p)_{K^-} \otimes p_{3/2}^{-1}$

Atomic 1s state



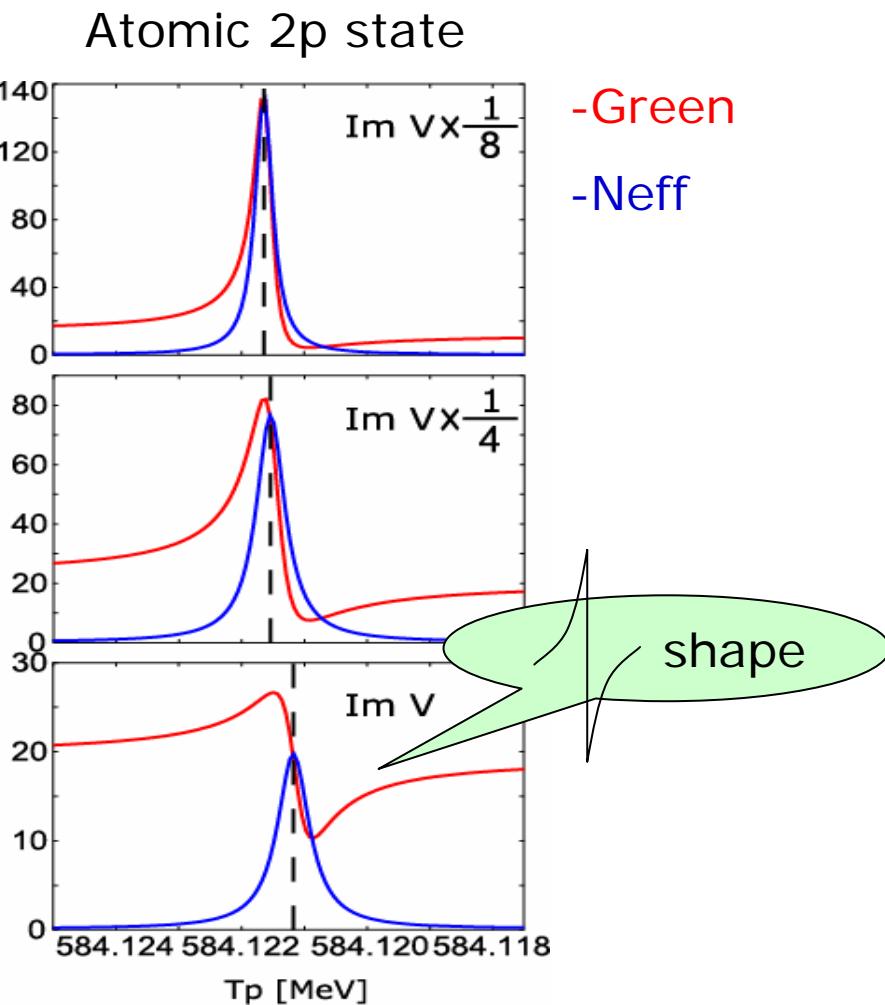
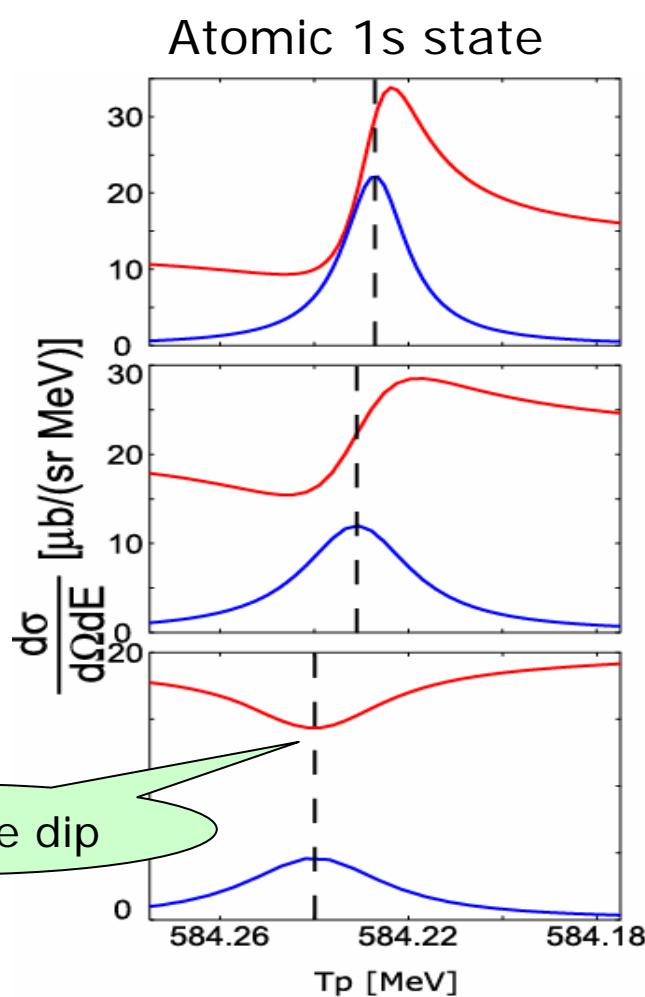
Atomic 2p state



# Energy Spectrum (Green vs. Neff)

Atomic State

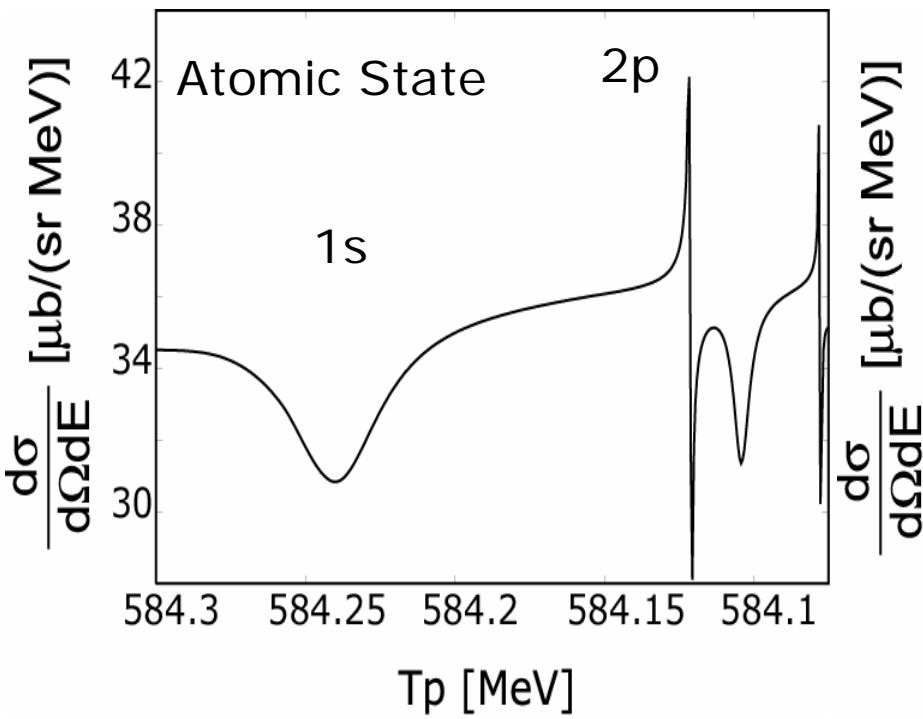
- $^{12}\text{C}(\text{In-flight } K^-, p) \quad P_{K^-} = 976 \text{ MeV/c} \quad (T_{K^-} = 600 \text{ MeV})$
- state:  $(s, p)_{K^-} \otimes p_{3/2}^{-1}$



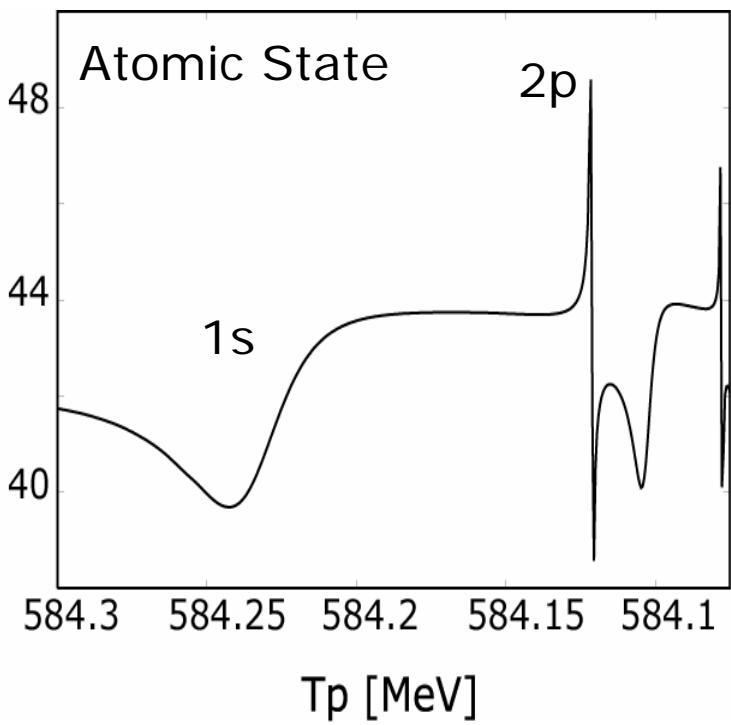
# Energy Spectrum

- $^{12}\text{C}(\text{In-flight } K^-, p) \quad P_{K^-} = 976 \text{ MeV/c} \quad (T_{K^-} = 600 \text{ MeV})$
- $V_{\text{opt}}$  : Energy Dependence

Chiral Unitary Model



Phenomenology

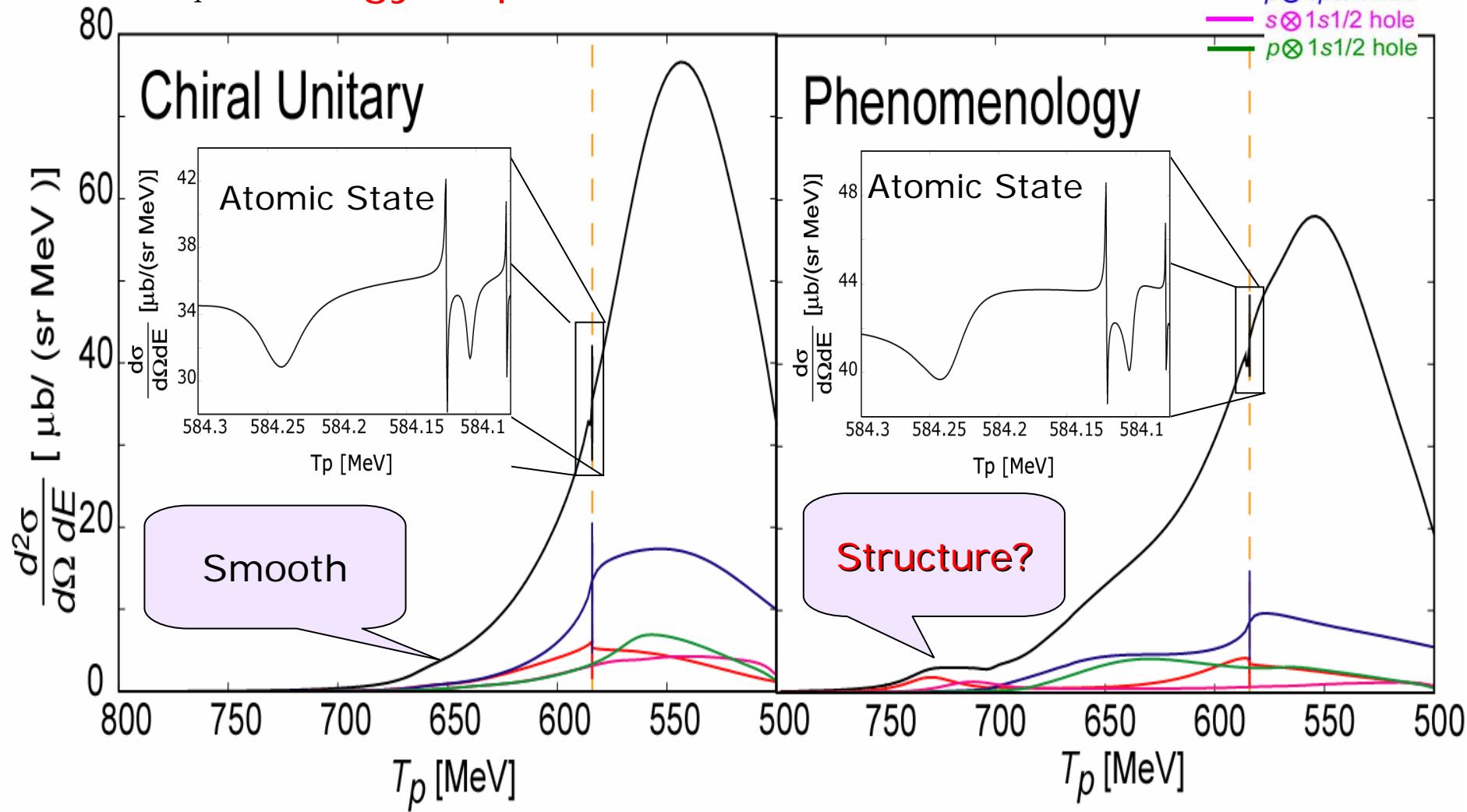


# Energy Spectrum

□  $^{12}\text{C}(\text{In-flight } K^-, p)$      $P_{K^-} = 976 \text{ MeV}/c$    ( $T_{K^-} = 600 \text{ MeV}$ )

□  $V_{\text{opt}}$  : Energy Dependence

$s \otimes 1p3/2$  hole  
 $p \otimes 1p3/2$  hole  
 $s \otimes 1s1/2$  hole  
 $p \otimes 1s1/2$  hole



# Energy Spectrum

$^{16}\text{O}(\text{In-flight K},\text{n}) \quad P_K = 930 \text{ MeV}/c$

Please ask  
Kishimoto-san Group



Comparison with  
Kishimoto group's data

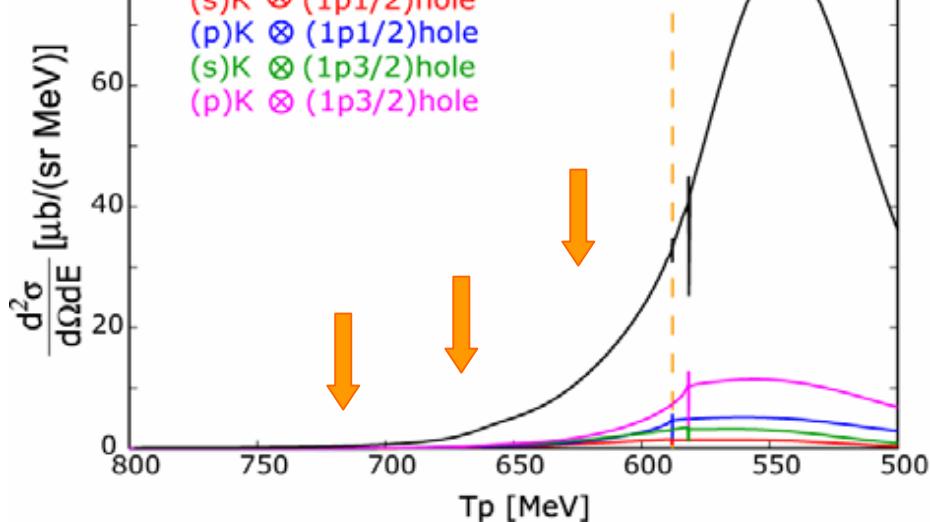
[ T.Kishimoto et al., Prog. Theor. Phys. Suppl. 149 (2003)264 ]

[ Fig. taken from the seminar slide @NWU by Dr. Hayakawa ]

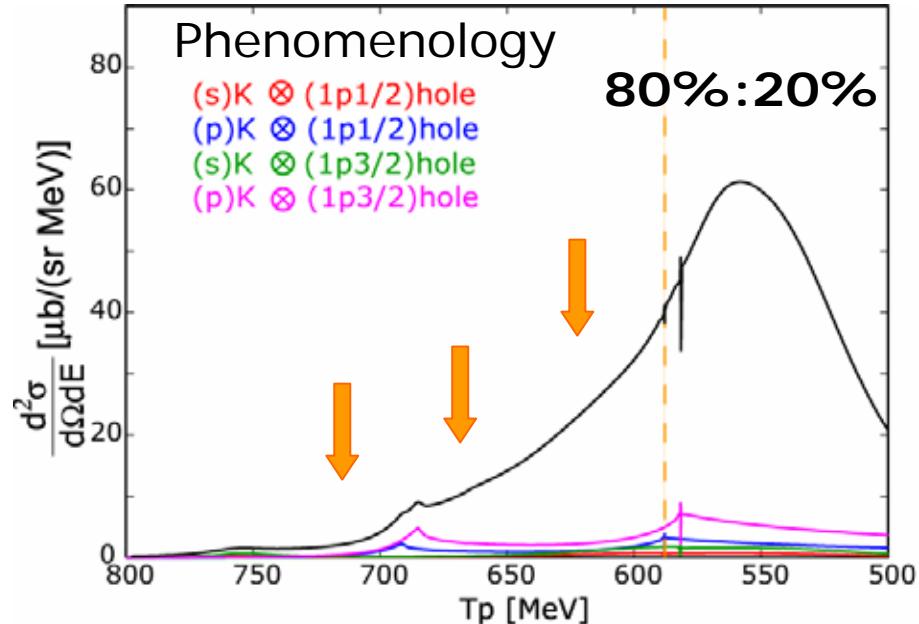
★ Energy dependent  $V_{\text{opt}}$

$^{16}\text{O}(\text{In-flight } K^-, p) \quad P_{K^-} = 976 \text{ MeV}/c$

Chiral Unitary



Phenomenology



# Summary

## □ Study of Kaonic Atoms

- To know the kaon properties at finite density.
- Deeply bound atomic states have **not been observed yet.**

## □ Our Study

### Kaonic Atoms

“Resonance Dip”

Structure -- **New deeply bound Atomic States are expected.**

Reaction -- Not simple peak structure, But dips, shapes etc.

We can expect to obtain new information !!

### Kaonic Nuclei

Structure -- Always exist in our calculation.

Reaction -- It seems very hard to observe signals.

Experimental info. of 2-body absorption  $\bar{K}NN \rightarrow YN$  preferable.  
(Old atomic data -> low  $\rho$ , FINUDA data -> higher  $\rho$  (?) )

# Future Plan

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- Deeply Atomic States formation – Systematic Study  
to find most interesting cases
- Effects of possible nuclear structure change  
due to K
- Evaluation of 2 body absorption,  $\bar{K}NN \rightarrow YN$