### Study of Aoki phase in Nc=2 gauge theories with fundamental and adjoint fermions

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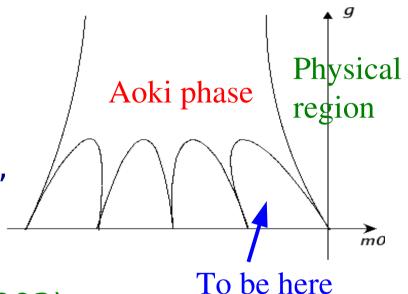
#### Study of phase structure of SU(N) gauge theories

- Fundamental and adjoint representations
- Search for conformal window: possible alternative to Standard Model Higgs sector
- At zero and finite temperature
- SU(2) theory:
  - Conformal behavior expectesd with less #flavor
- Overlap fermion
  - Exact chiral symmetry
  - Epsilon regime to explore chiral symmetry breaking
- For locality of overlap operator
  - Wilson-Dirac kernel must have gap (mobility edge)
    ⇔ Out of Aoki phase (Golterman and Shamir, 2003)
    Motivation of present work



#### Flavor-parity broken phase of Wilson-Dirac operator

- Proposed by Aoki, 1984
- Numerical evidence
- Chiral Lagrangian analysis
  (Sharpe and Singleton, 1998)
- As the kernel of overlap operator, to be in between fingers



#### Conjecture of Golterman-Shamir (2003)

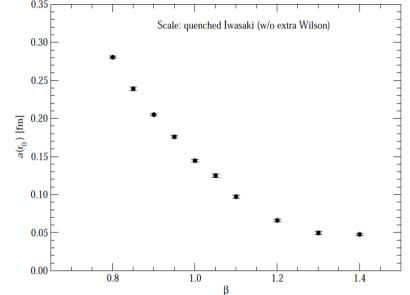
- Eigenmodes of  $H_W$  is local below "mobility edge"
- Aoki phase is characterized by vanishing mobility edge
- Locality of overlap operator is ensured if  $H_W$  is out of Aoki phase



## Lattice setup

#### Present study: quenched SU(2) with Iwasaki gauge action

- Hermitian Wilson-Dirac operator
- Fundamental and adjoint fermions
- Lattice: 8<sup>3</sup>x16 (12<sup>3</sup>x24 in progress)
- Scale: r<sub>0</sub>=0.49fm (just a guide!)
- Mainly at  $\beta = 0.80, 1.00$
- All results are preliminary



#### In progress:

- With topology fixing term (extra Wilson fermion/ghost)
- Dynamical overlap fermions (fundamental, adjoint)



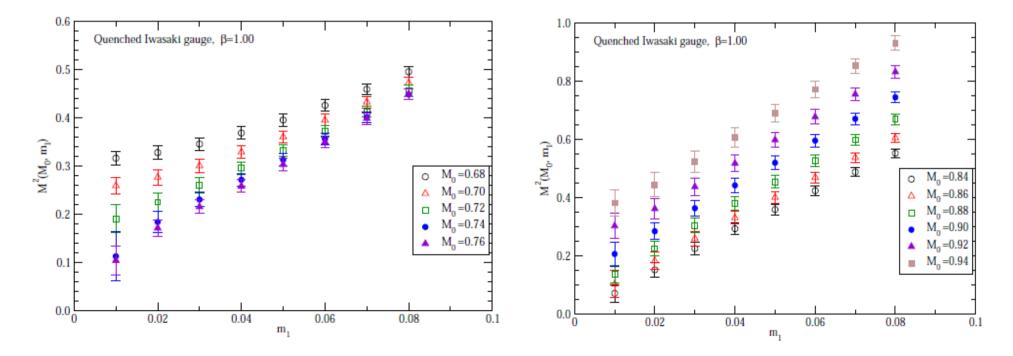
Pion correlator:

$$\Gamma(x,y) = \langle \pi_+(x)\pi_-(y) \rangle \qquad \pi_\pm(x) = i\bar{\psi}(x)\gamma_5\tau_\pm\psi(x)$$

from propagators with twisted mass

$$S_q = [D_W - im_1\tau_3\gamma_5]^{-1}$$

Meson mass extracted from exponential fit

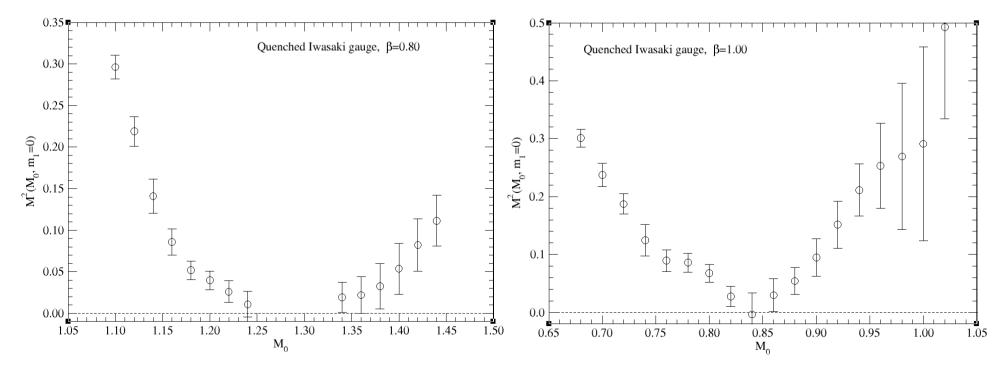




## Meson correlator (fundamental)

Linearly extrapolated to  $m_1=0$  with smallest 3 points

- Vanishing pion mass = Aoki phase
  Result:
  - Data at  $\beta$ =0.80 and 1.0 indicate existence of Aoki phase
  - Width of Aoki phase decreased as  $\beta$  increases
  - More careful analysis of extrapolation in  $m_1$  is necessary

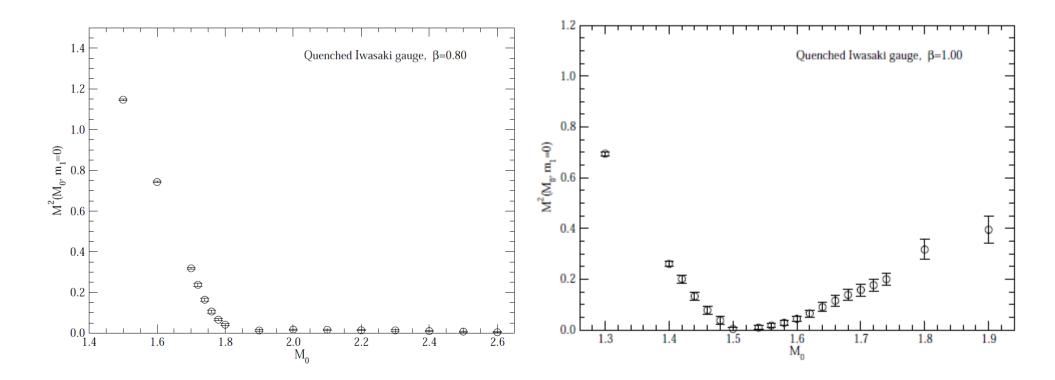




• Same analysis as fundamental fermion

#### **Results:**

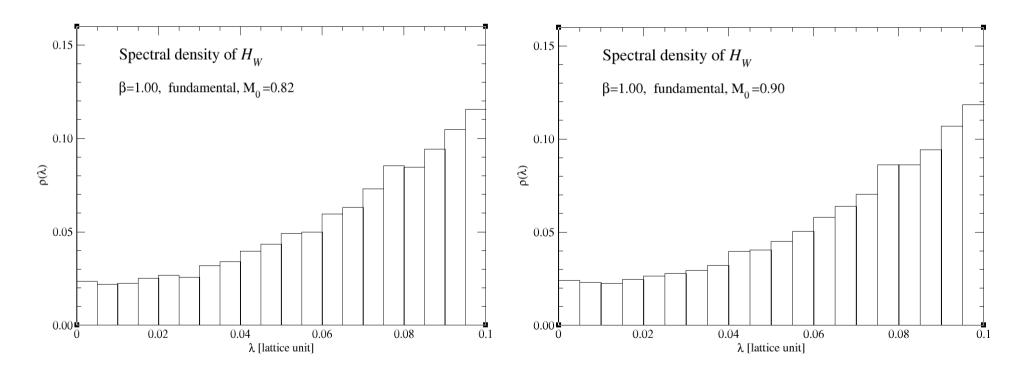
- At  $\beta$ =0.80, Aoki phase extends to large M<sub>0</sub> values
- Critical values of  $M_0$  are different from fundamental case





Low-lying eigenvalue density of  $H_W$ 

- If gap is open, no chance of Aoki phase
- With vanishing gap, Aoki phase appear if near-zero modes are extended (mobility edge is zero)



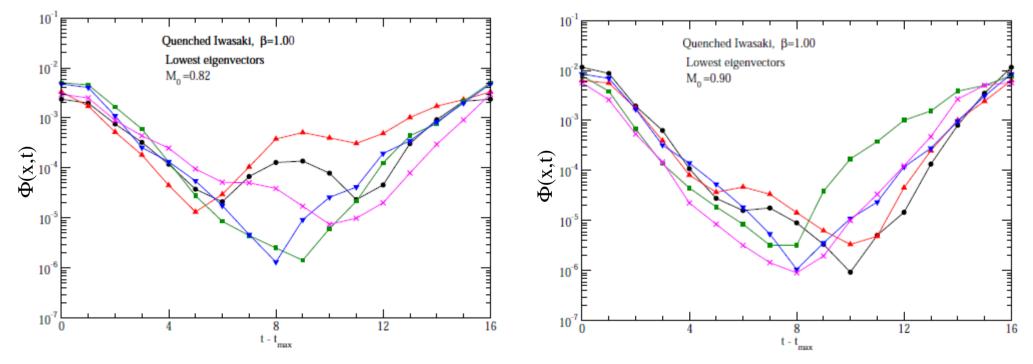
# Content of the second state of the second s

Density of the lowest eigenvector  $\Phi(x) = \sum_{a,j} |\phi_{\lambda}^{a,j}(x)|^2$ 

- Exponentially local out of Aoki phase
- Extended in Aoki phase

#### Numerical results:

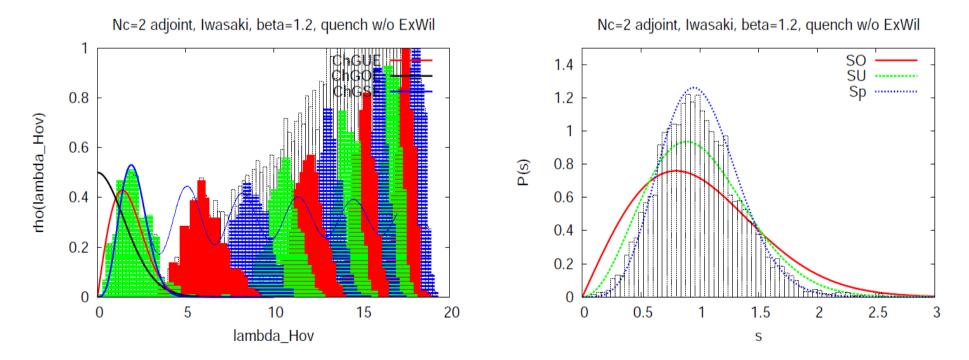
- Present results are not manifest, need refined analysis
- Same analysis is in progress for adjoint fermion



## Spectrum of overlap operator

Unfolded low-lying eigenvalues of overlap operator

- Comparison with Chiral Random Matrix Theory
  - Orthogonal (SU(2) fundamental)
  - Unitary (SU(N), N>2)
  - Symplectic (adjoint)
- To judge whether the chiral symmetry is broken





We are exploring phase structure of Wilson-Dirac operator in SU(2) gauge theories

- Location of Aoki phase
- Spectral property of Wilson-Dirac operator
- Spectral property of overlap operator
- Preparation for dynamical overlap simulation

#### Investigation being extended to

- Topology fixing term (avoiding near-zero modes of  $H_W$ )
- Dynamical overlap fermions
- Phase structure in Nf for fundamental/adjoint fermions

