

# Nuclear Astrophysics

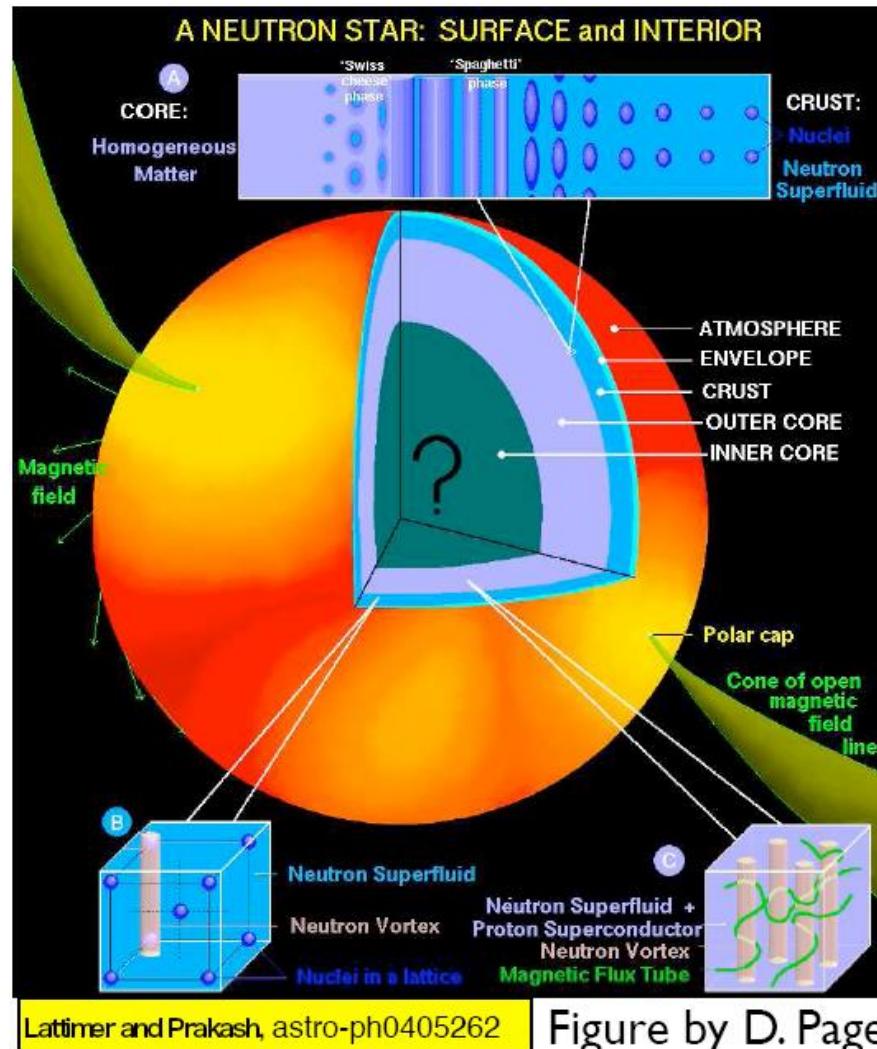
-Neutron Stars, Nuclear Matter, Symmetry Energy-

Kei Iida (Kochi University)

## Contents

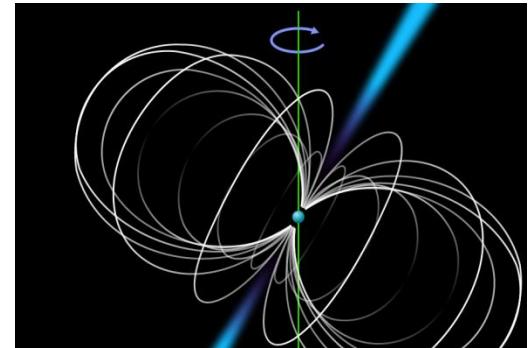
- *Neutron stars: Introduction and recent topics*
- *Nuclear matter: Introduction and recent topics*

# Neutron stars



## Discovery of pulsars and neutron star observations

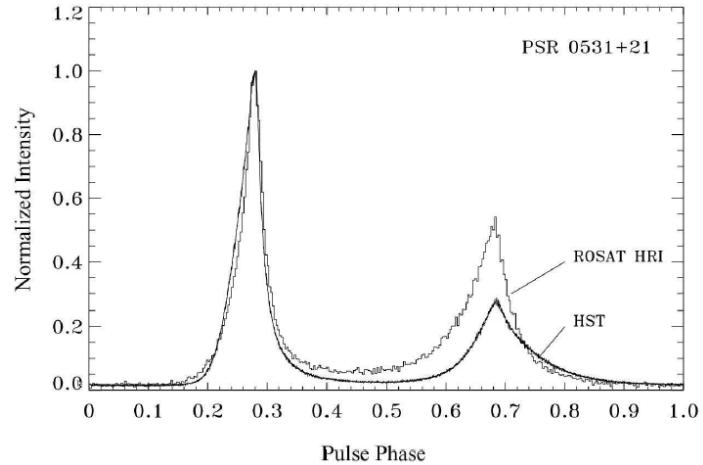
In 1967, Hewish & Bell discovered a “pulsar” emitting periodic radio pulses, PSR B1919+21 (at that time, referred to as LGM “Little Green Men”-1.)



Imaginary drawing of a pulsar (gigantic “dynamo”)



1968: A pulsar discovered in the Crab Nebula.

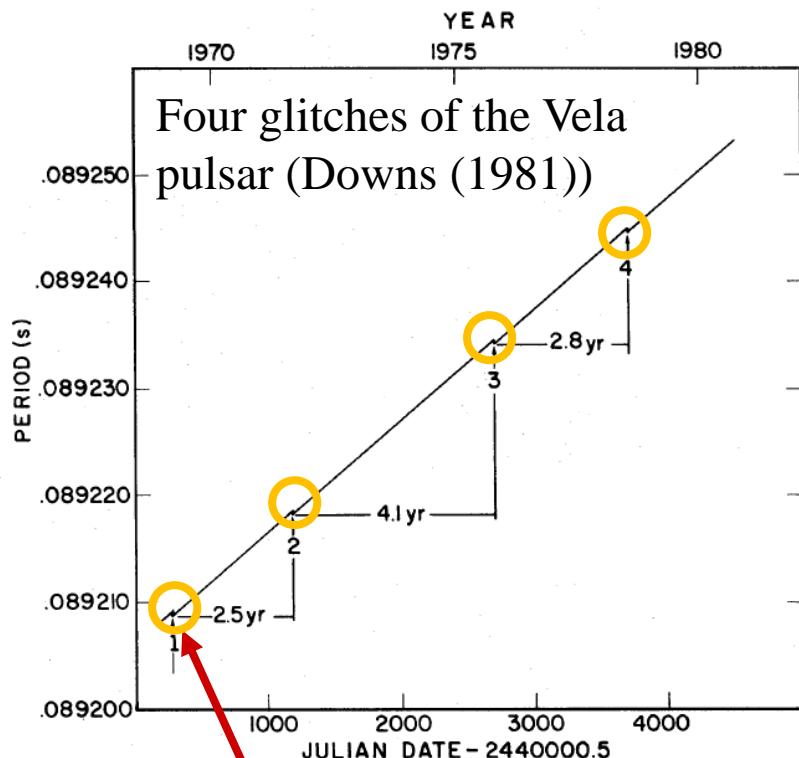


The very short (33 msec) period of the Crab pulsar helped to identify pulsars as neutron stars!

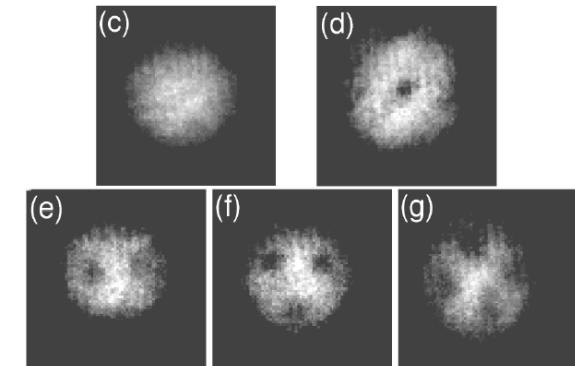
Crab Nebula (NASA/ESA)

## Pulsar glitch

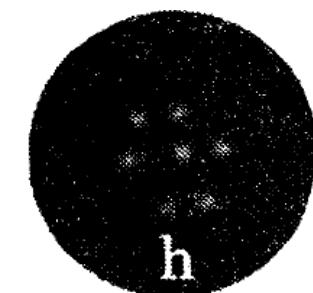
From young pulsars, glitches, sudden decrease in the pulse period, are frequently observed.



Consistent with backreaction to disappearance of outwardly moving vortices, suggesting that superfluidity should occur in a neutron star!



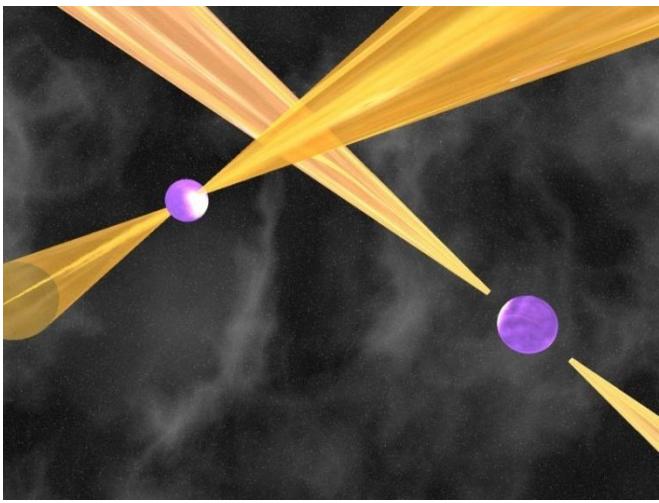
Vortices in rotating Bose condensate of Rb atoms (Madison et al.(2000))



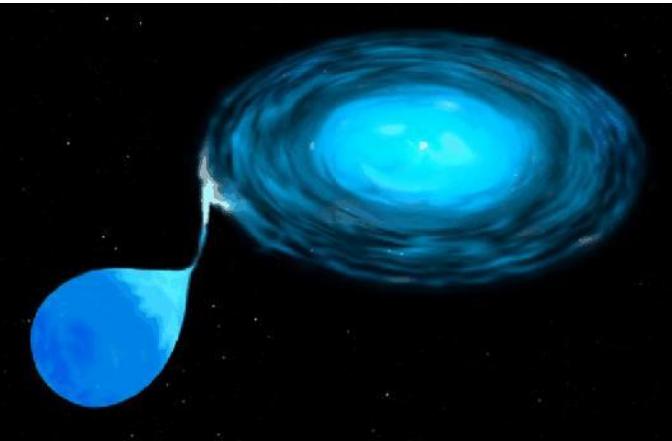
Vortices in rotating superfluid helium (Yarmchuk et al.(1979))

## Various types of pulsars

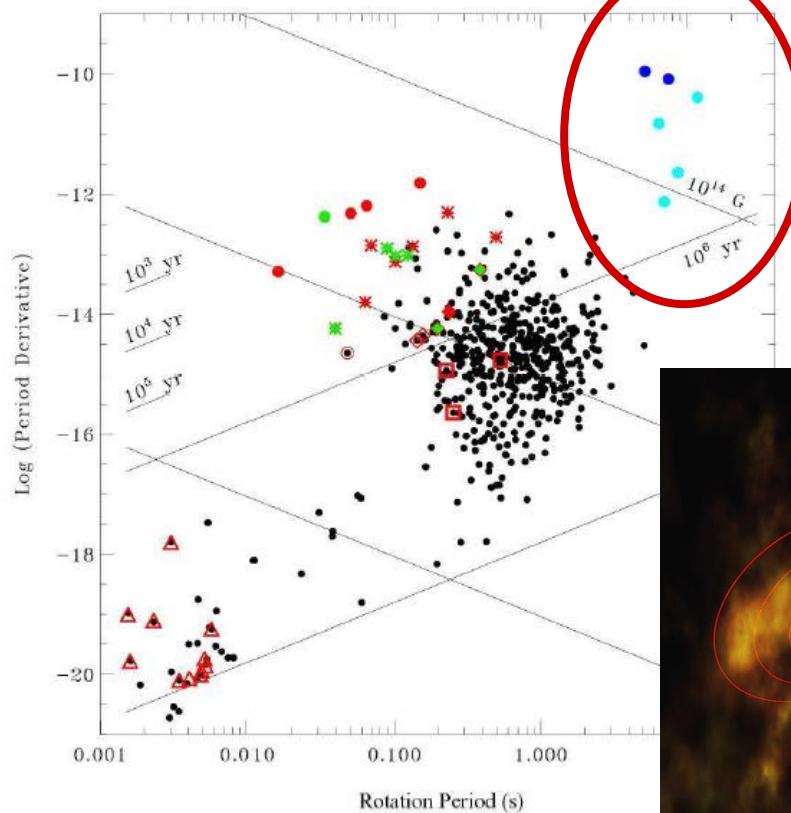
- Double pulsar (PSR J0737-3039 alone)



- X-ray pulsars  
(accretion-powered pulsars)



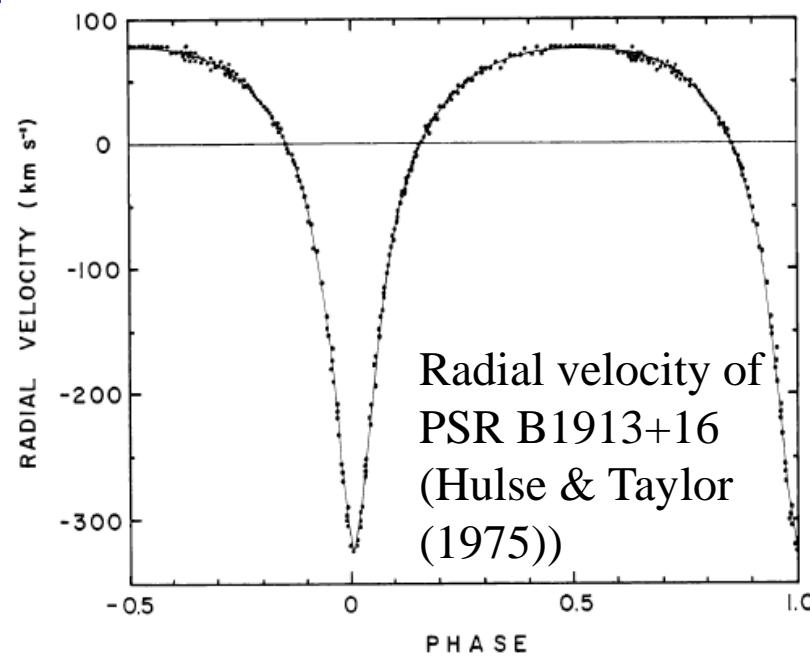
- Anomalous X-ray pulsars  
(presumably, magnetars)



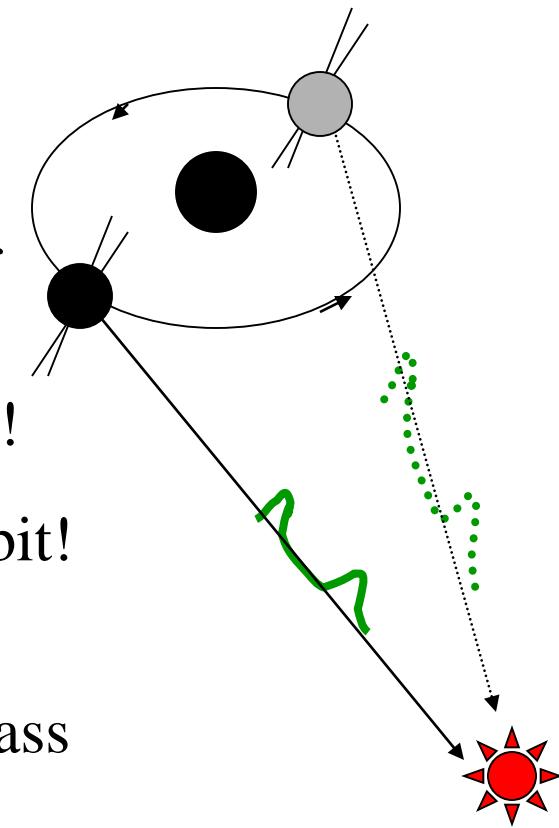
Imaginary drawing  
by NASA

# Neutron star mass determination by Hulse & Taylor

A pulsar with a binary companion:  
Observed orbital motion → mass measurement!



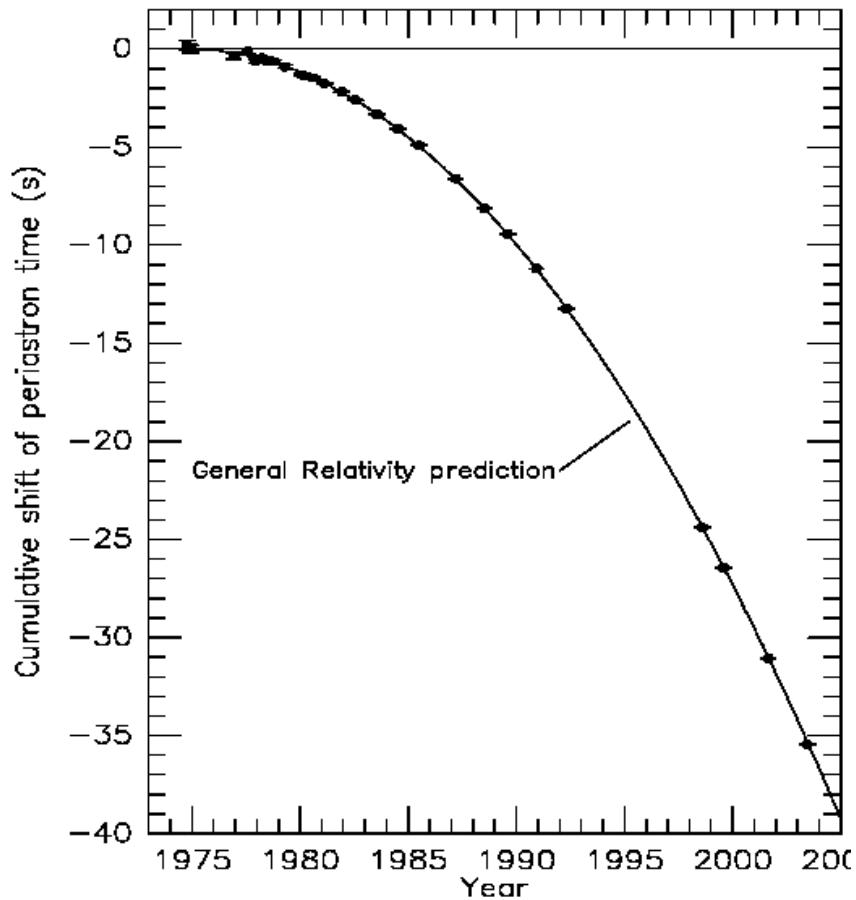
The companion of PSR B1913+16 is also a neutron star!  
Post-Keplerian orbit!  
General relativity allows accurate mass determination!



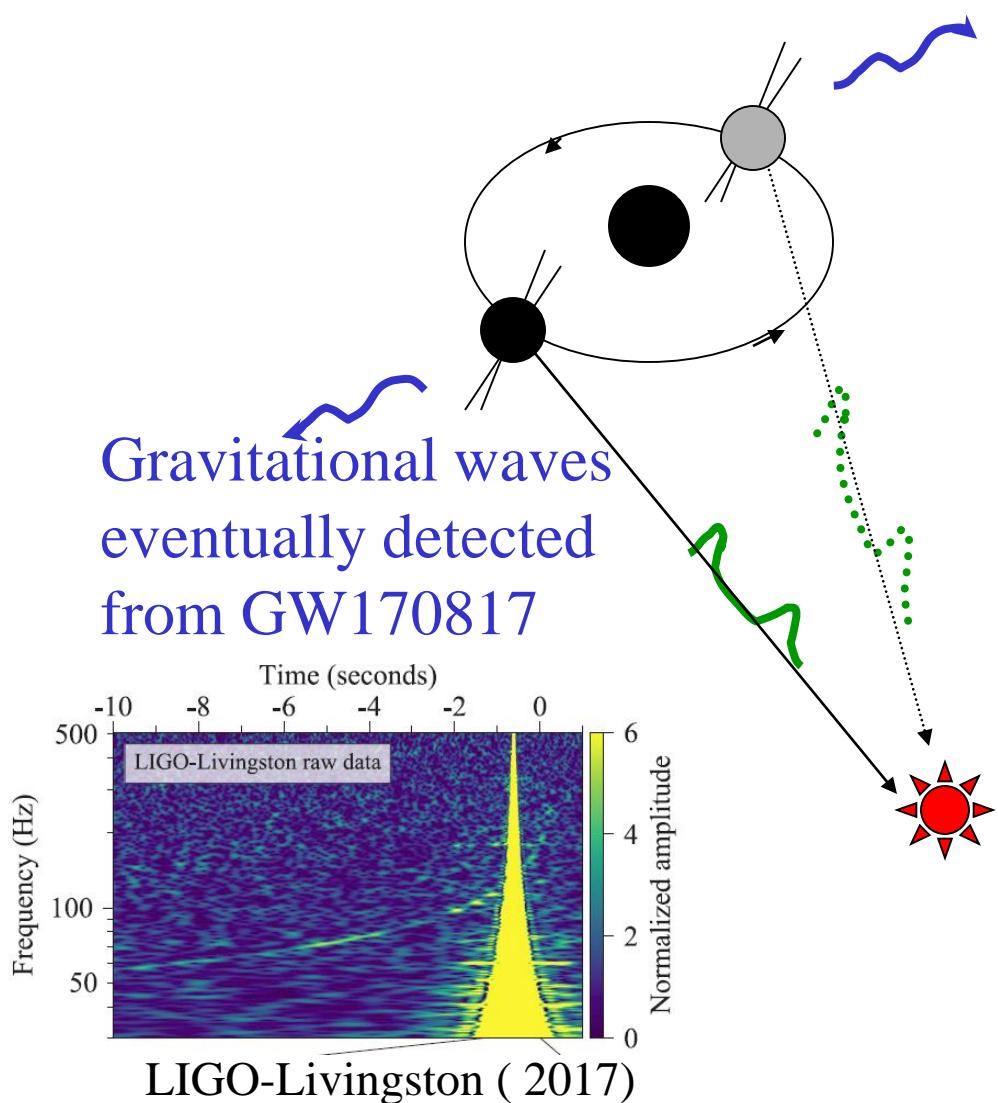
Neutron star–neutron star binaries					
1518+49	$1.56^{+0.13}_{-0.44}$	(88)	1518+49 companion	$1.05^{+0.45}_{-0.11}$	(88)
1534+12	$1.3332^{+0.0010}_{-0.0010}$	(88)	1534+12 companion	$1.3452^{+0.0010}_{-0.0010}$	(88)
1913+16	$1.4408^{+0.0003}_{-0.0003}$	(88)	1913+16 companion	$1.3873^{+0.0003}_{-0.0003}$	(88)
2127+11C	$1.349^{+0.040}_{-0.040}$	(88)	2127+11C companion	$1.363^{+0.040}_{-0.040}$	(88)
J0737-3039A	$1.337^{+0.005}_{-0.005}$	(46)	J0737-3039B	$1.250^{+0.005}_{-0.005}$	(46)
Mean = $1.34 M_{\odot}$ , weighted mean = $1.41 M_{\odot}$					
Lattimer & Prakash (2004)					

## Neutron star mass determination by Hulse & Taylor (contd.)

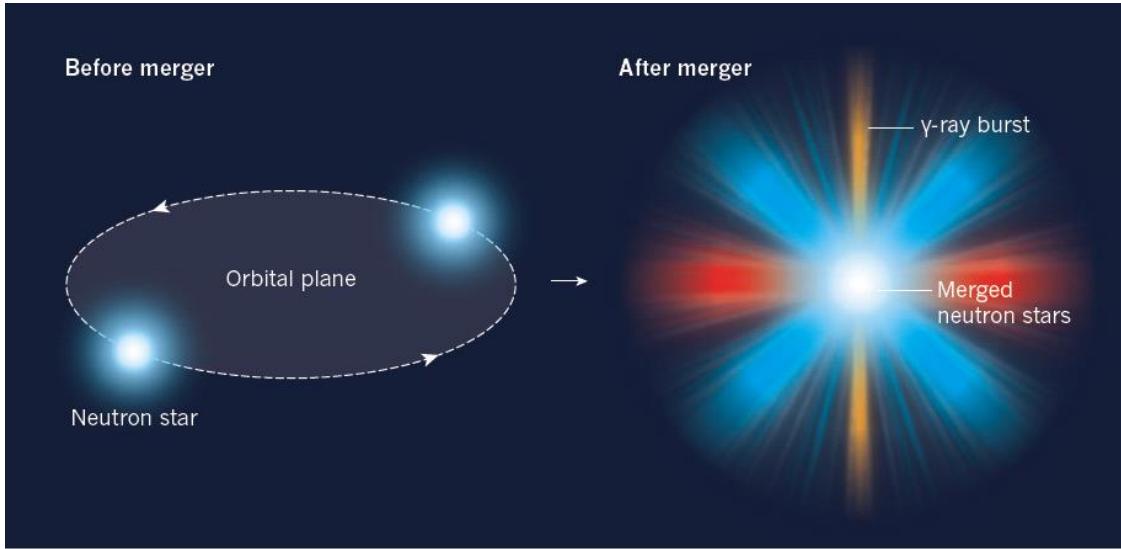
Observed decrease in the orbital period was successfully explained by emission of gravitational waves predicted by general relativity.



Decreasing orbital period of PSR B1913+16  
(Weisberg & Taylor (2004))



# Multimessenger observations of GW170817



By Coleman Miller  
(Nature 551, 36 (2017))

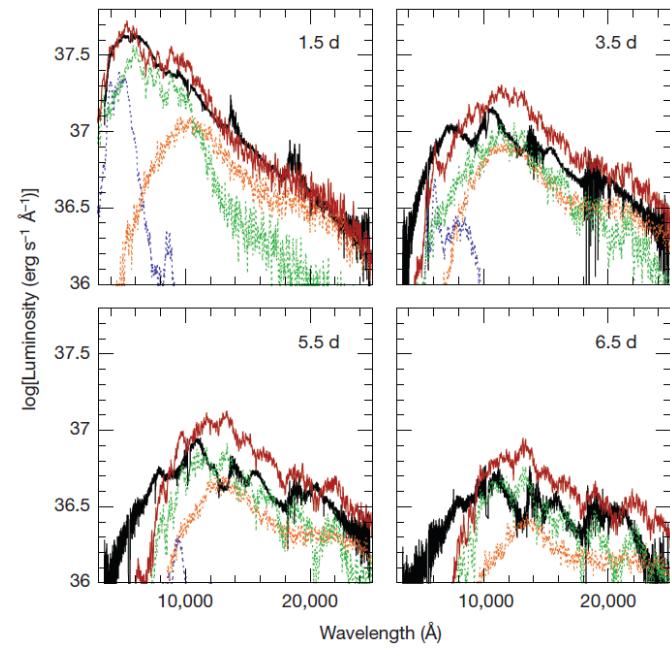
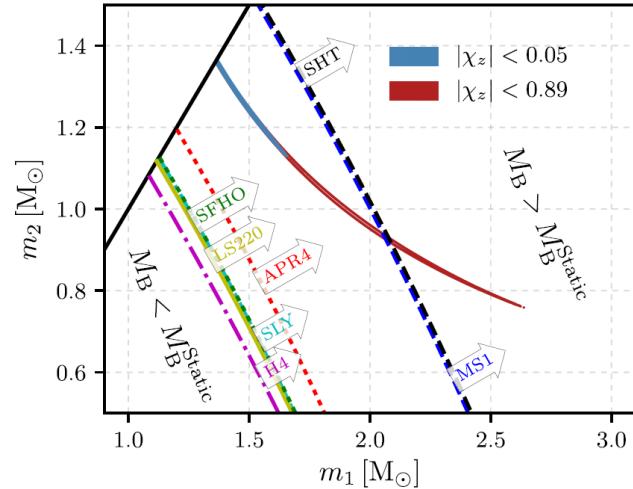
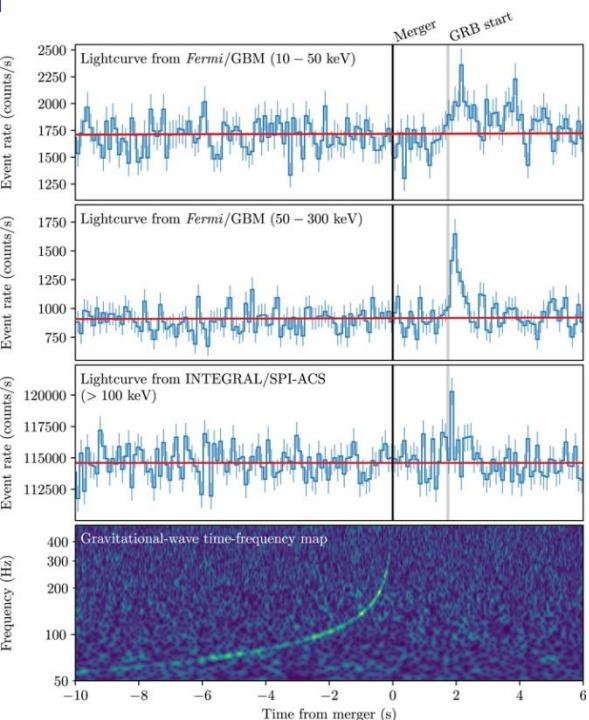
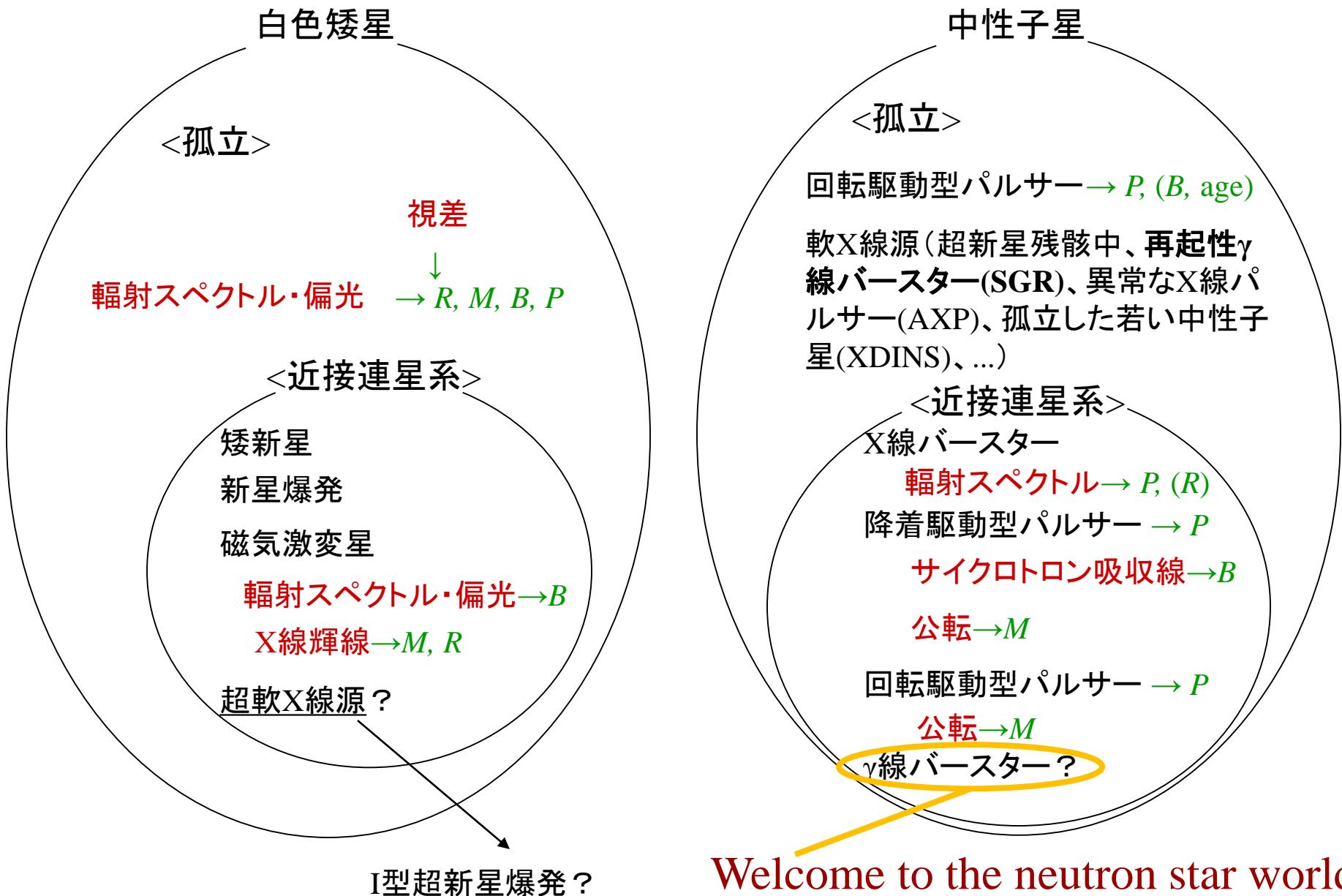


Figure 3 | Kilonova models compared with the AT 2017gfo spectra.

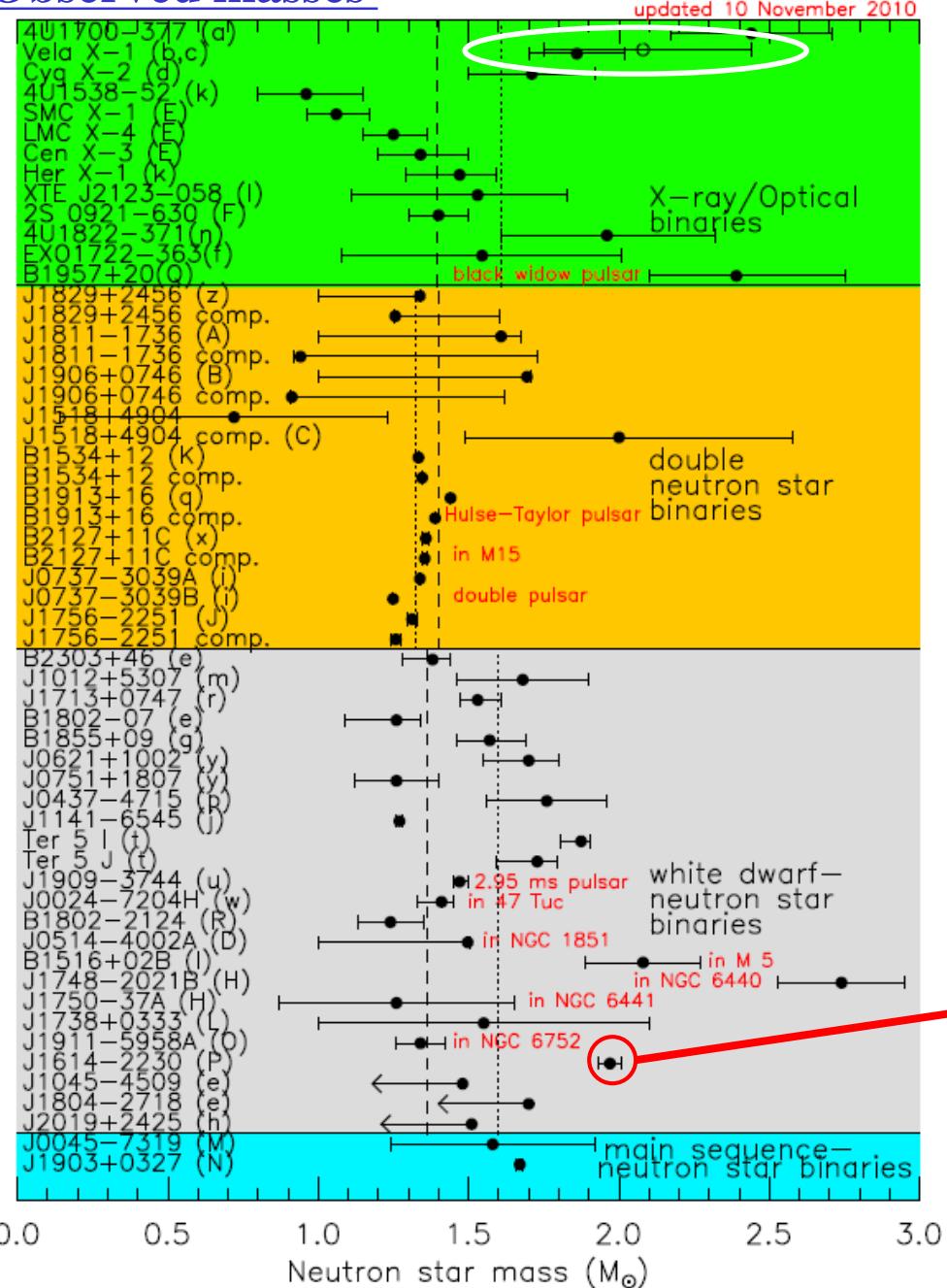
Abbott et al. ApJ 848, L13 (2017).

Pian et al. Nature 551, 67 (2017).

# 観測されている高密度縮退星

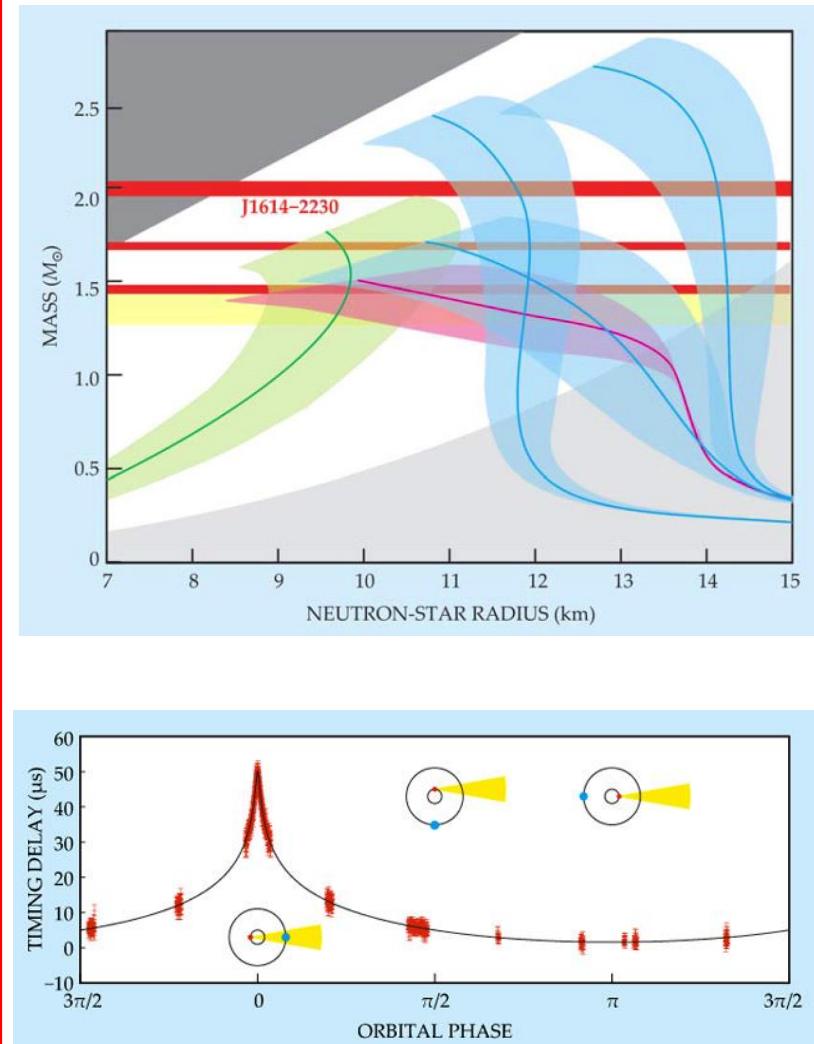


# Observed masses



Lattimer & Prakash, arXiv:1012.3208.

## Pulsar twice as heavy as the Sun



# The Best Measured Neutron Star Radii

Name	$R_\infty$ (km/D)	D (kpc)	$kT_{\text{eff},\infty}$ (eV)	$N_H$ ( $10^{20} \text{ cm}^{-2}$ )	Ref.
omega Cen (Chandra)	$13.5 \pm 2.1$	$5.36 \pm 6\%$	$66^{+4}_{-5}$	(9)	Rutledge et al (2002)
omega Cen** (XMM)	$13.6 \pm 0.3$	$5.36 \pm 6\%$	$67 \pm 2$	$9 \pm 2.5$	Gendre et al (2002)
M13** (XMM)	$12.6 \pm 0.4$	$7.80 \pm 2\%$	$76 \pm 3$	(1.1)	Gendre et al (2002)
47 Tuc X7 (Chandra)	$34_{-13}^{+22}$	$5.13 \pm 4\%$	$84^{+13}_{-12}$	$0.13^{+0.06}_{-0.04}$	Heinke et al (2006)
M28** (Chandra)	$14.5_{-3.8}^{+6.9}$	$5.5 \pm 10\%$	$90_{-10}^{+30}$	$26 \pm 4$	Becker et al (2003)
M30 (Chandra)	$16.9_{-4.3}^{+5.4}$	--	$94_{-12}^{+17}$	$2.9^{+1.7}_{-1.2}$	Lugger et al (2006)
NGC 2808 (XMM)	??	9.6 (?)	$103_{-33}^{+18}$	$18^{+11}_{-7}$	Webb et al (2007)

$$R_\infty < 5\%$$

Caveats:

- All IDd by X-ray spectrum (47 Tuc, Omega Cen now have optical counterparts)
- calibration uncertainties

Distances:

Carretta et al (2000),  
Thompson et al (2001)

Quiescent low-mass X-ray  
binaries in globular clusters

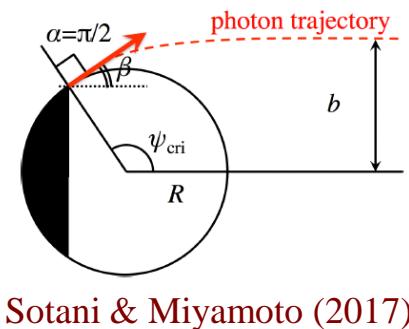


Apparent radius :

$$R_\infty = \frac{R}{\sqrt{1 - 2GM/Rc^2}}$$

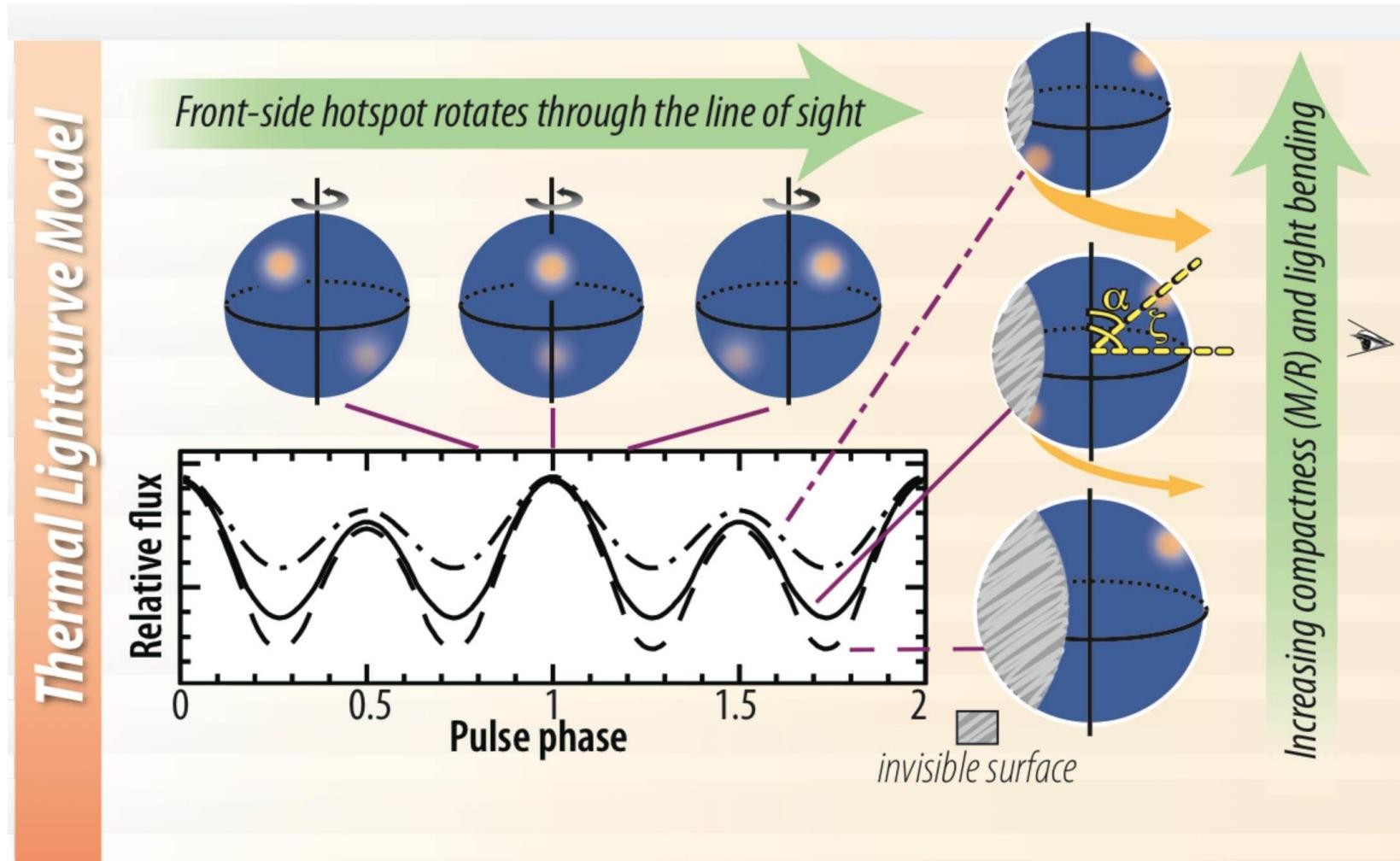
Distance to the  
globular cluster

# NICER (Neutron star Interior Composition ExploreR)

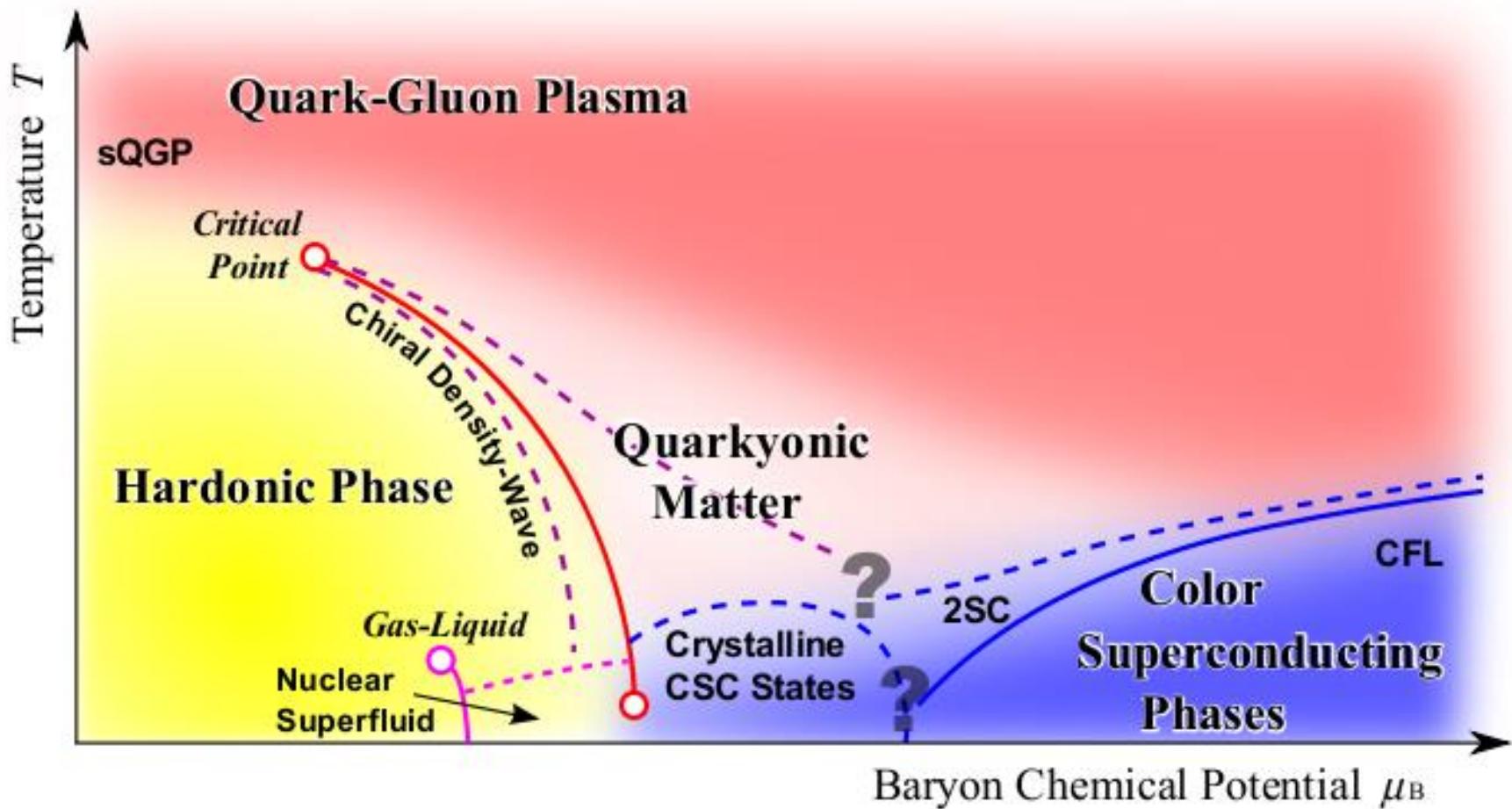


Deducing  $M/R$  from light curves of msec pulsars

Sotani & Miyamoto (2017)



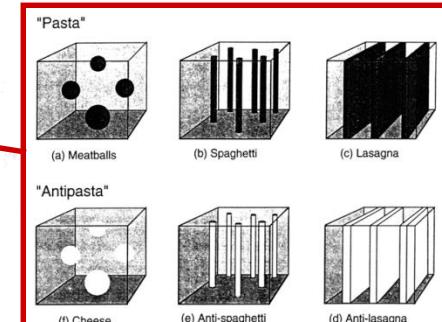
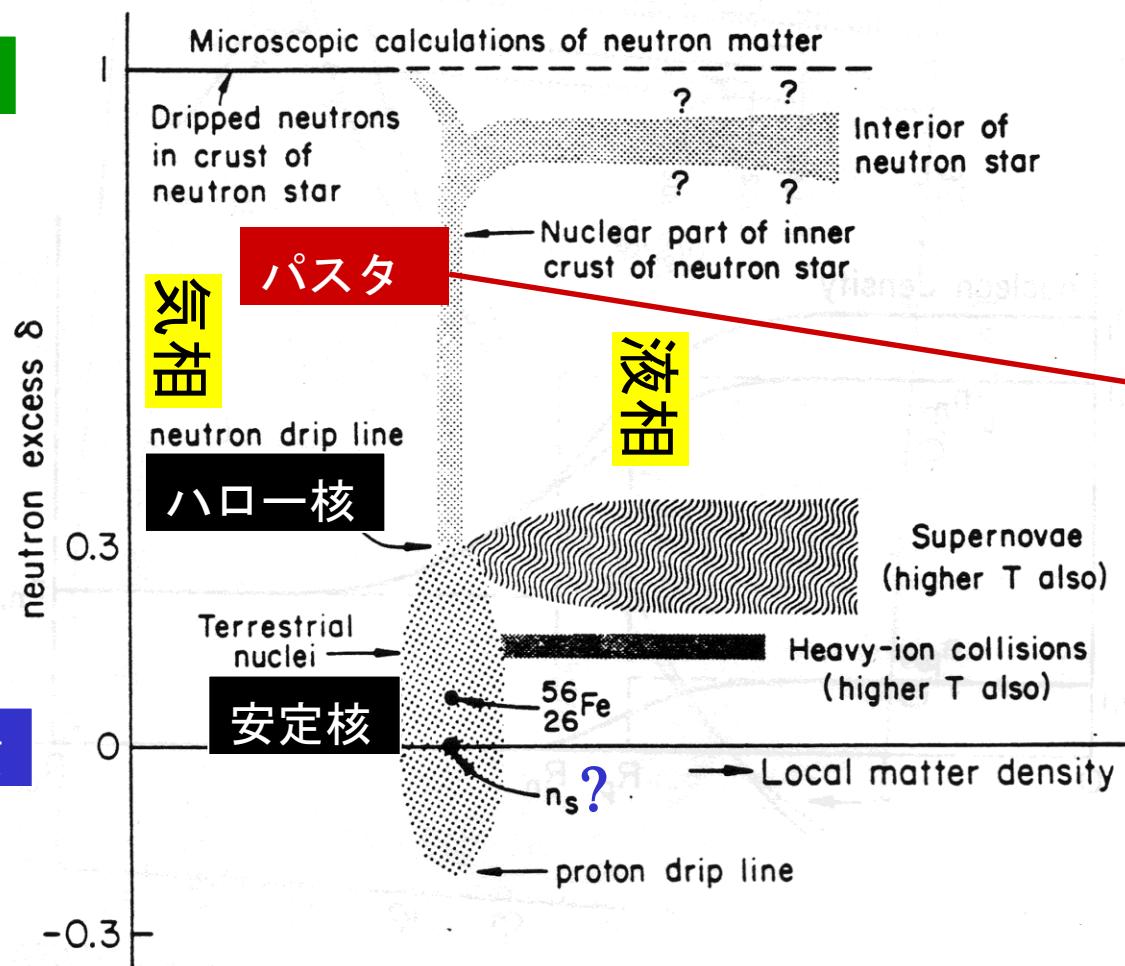
# Nuclear matter



By Fukushima

# Systems composed of nuclear matter

中性子物質



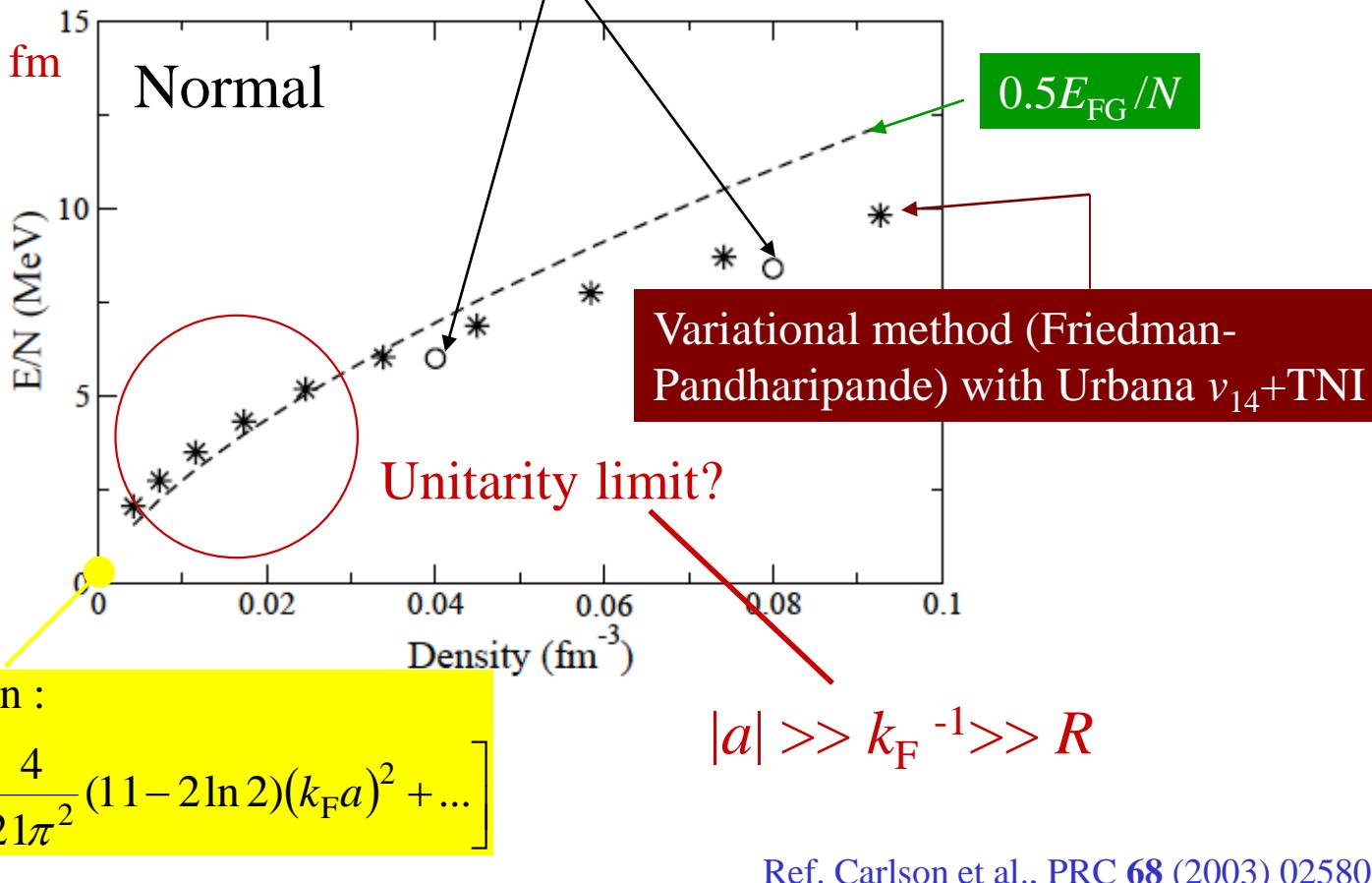
対称核物質

## Microscopic EOS calculations

### Pure neutron matter

Green's function Monte-Carlo (GFMC)  
with Argonne  $v_8'$

Scattering length  $a \approx -18$  fm  
Effective range  $\approx 2$  fm

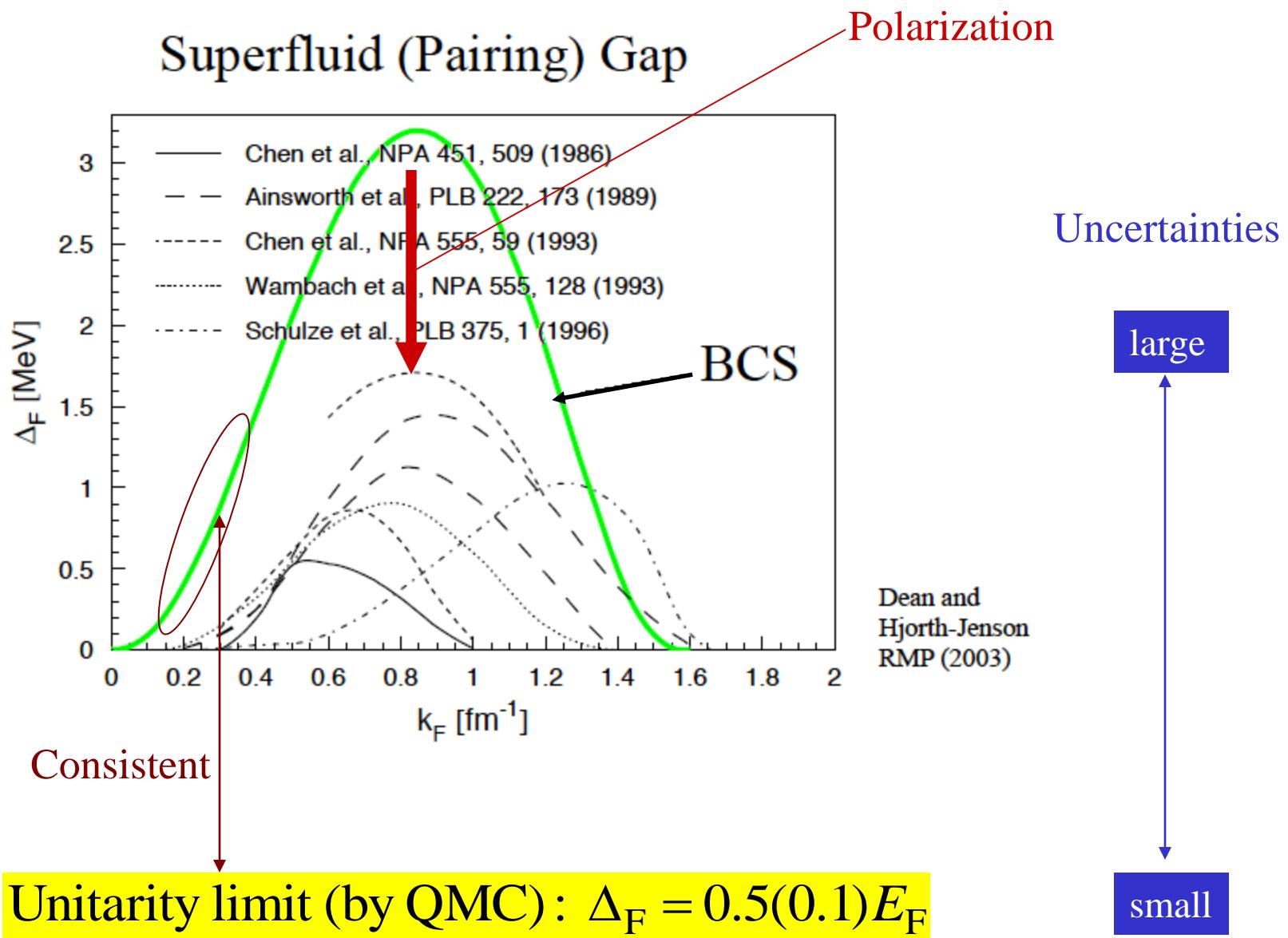


### Symmetric nuclear matter

Variational method: Overbinding without phenomenological three-nucleon forces

## Microscopic EOS calculations (contd.)

### Pure neutron matter



## Phenomenological EOS parameters

Energy per nucleon of bulk nuclear matter near the saturation point  
(nucleon density  $n$ , neutron excess  $\alpha = (n_n - n_p)/n$ ):

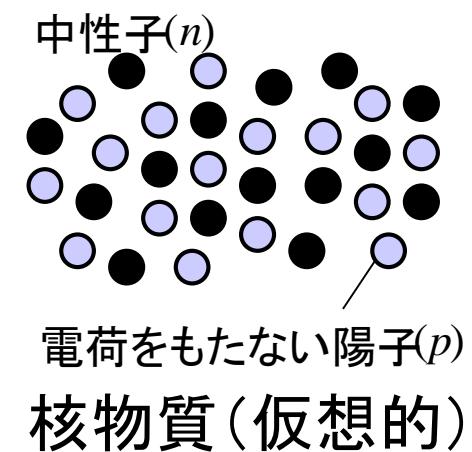
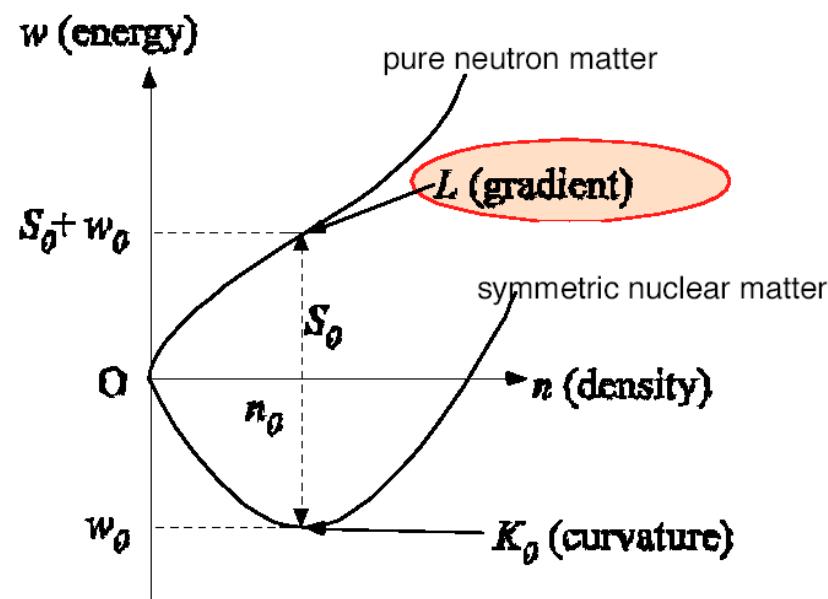
$$w = w_0 + \frac{K_0}{18n_0^2} (n - n_0)^2 + \left[ S_0 + \frac{L}{3n_0} (n - n_0) \right] \alpha^2$$

$n_0, w_0$  saturation density & energy of symmetric nuclear matter

$S_0$  symmetry energy coefficient

$K_0$  incompressibility

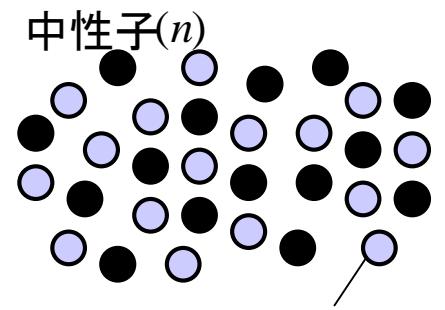
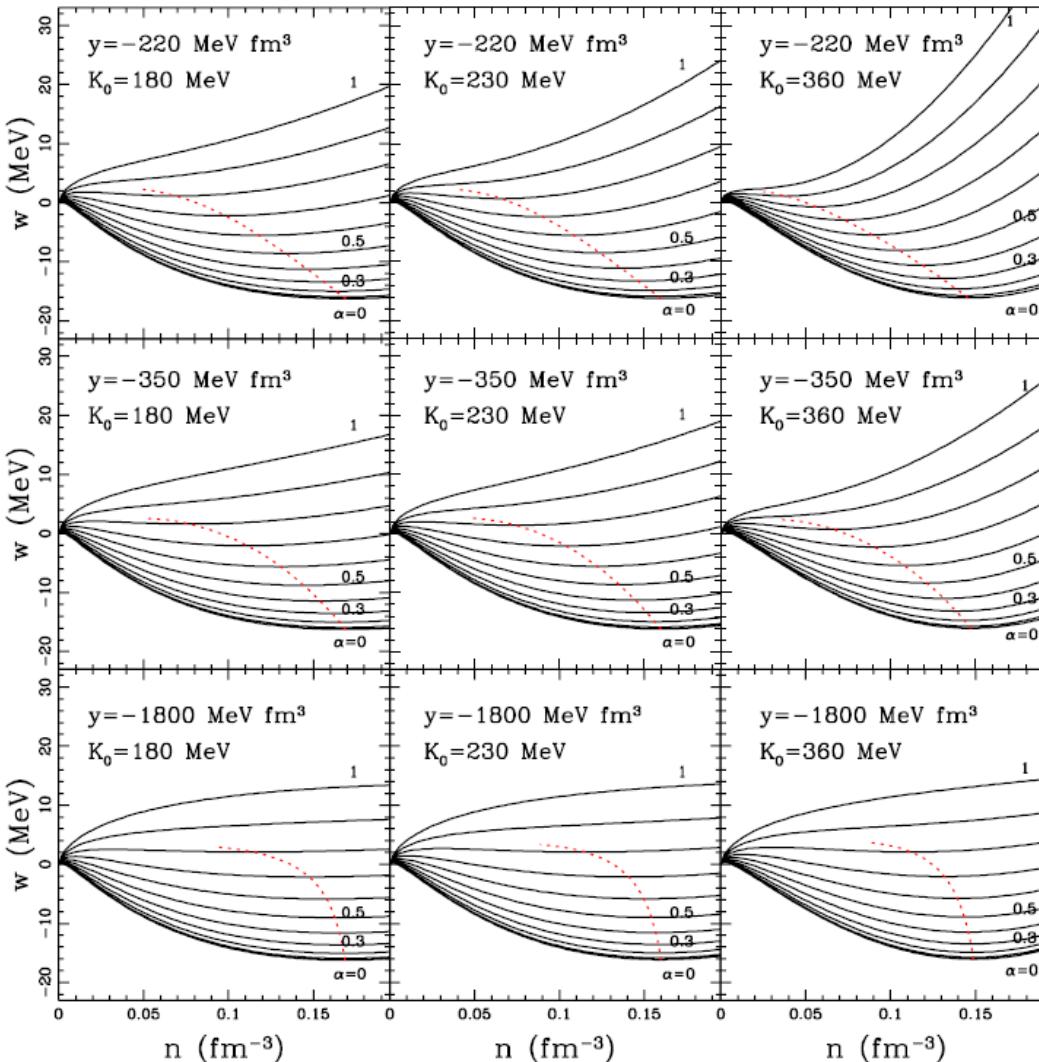
$L$  density symmetry coefficient



# ゼロ温度での核物質の状態方程式

非圧縮率

対称エネルギーの密度勾配



電荷をもたない陽子( $p$ )  
核物質(仮想的)

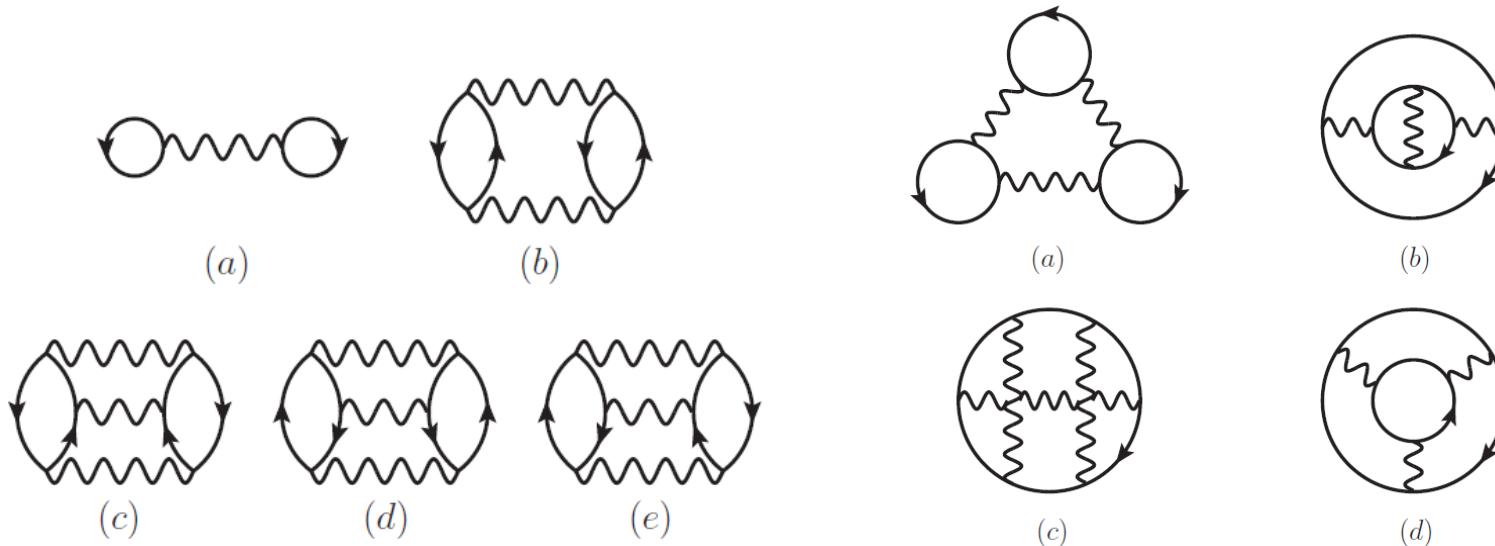
## 9つの極端な例

- ・安定核の半径・質量データは同様に再現
- ・将来の不安定核データで峻別可能？

Ref. Oyamatsu & Iida, PTP  
**109** (2003) 631 ; Kohama, Iida,  
& Oyamatsu PRC **72** (2005)  
024602.

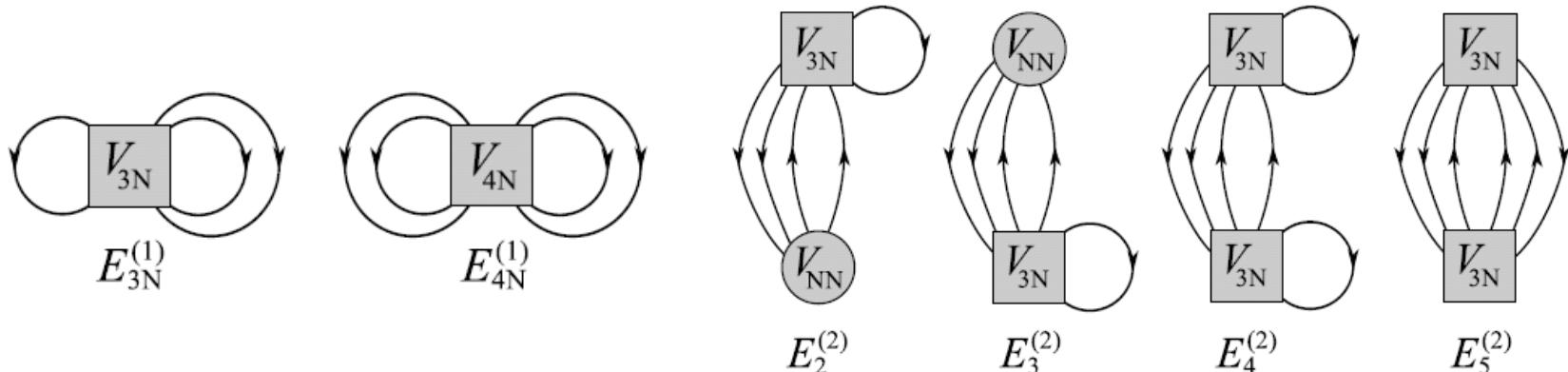
# Many-body perturbation calculations with chiral 2N, 3N, 4N interactions

1<sup>st</sup>, 2<sup>nd</sup>, 3<sup>rd</sup> order pp and 3<sup>rd</sup> ph contributions due to 2N interactions:



Ref. Holt & Kaiser, PRC **95** (2017) 034326.

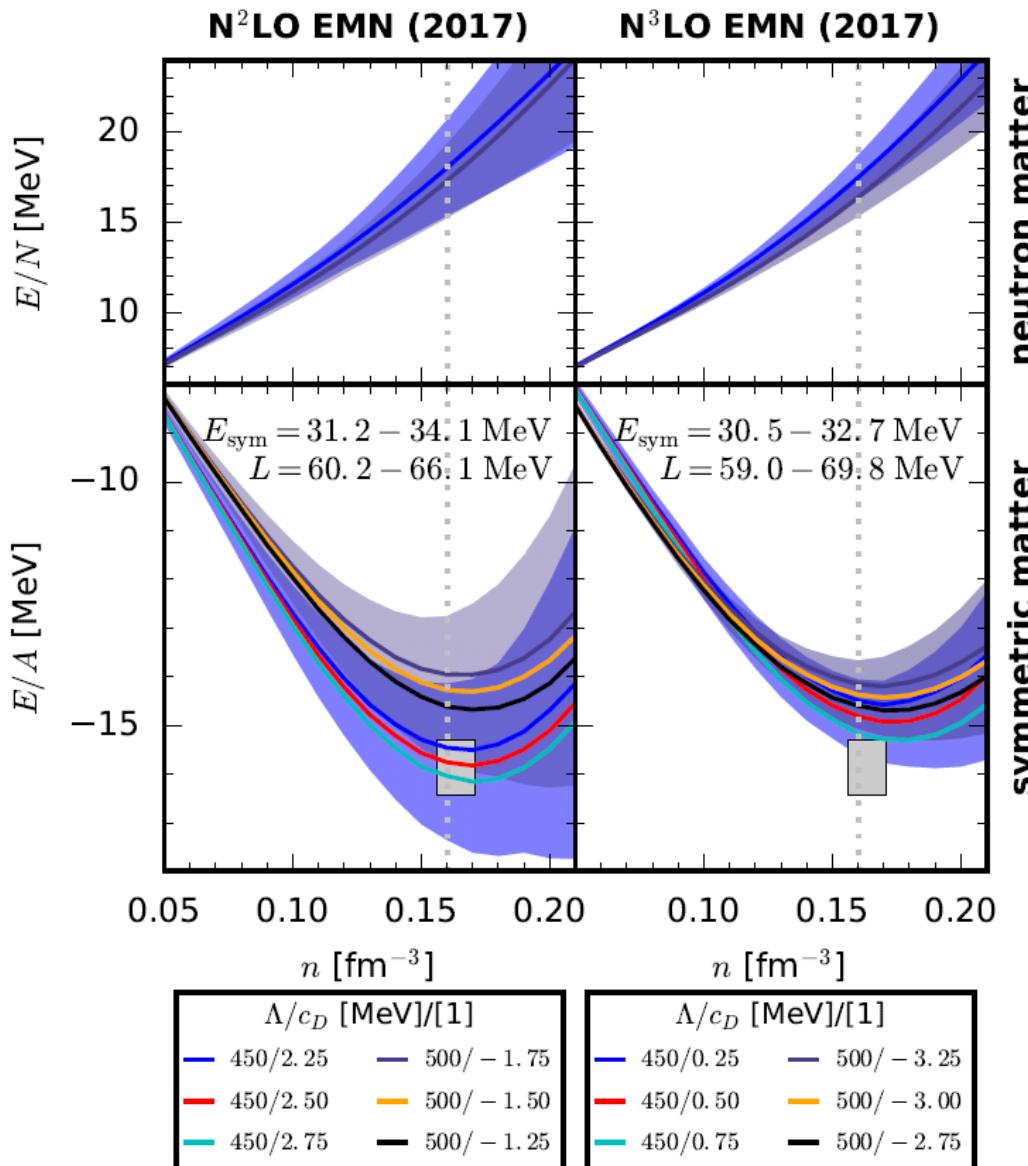
1<sup>st</sup>, 2<sup>nd</sup> order pp contributions due to 3N and 4N interactions:



Ref. Krüger, Tews, Hebeler, & Schwenk, PRC **88** (2013) 025802.

# Many-body perturbation calculations with chiral 2N, 3N, 4N interactions

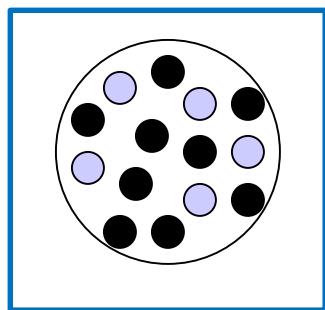
Up to 4<sup>th</sup> order:



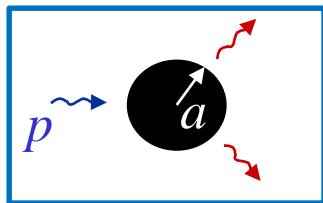
3N interaction parameters  
fitted to the empirical  
saturation region and triton  
binding energy

# これまでの核物質研究のまとめ

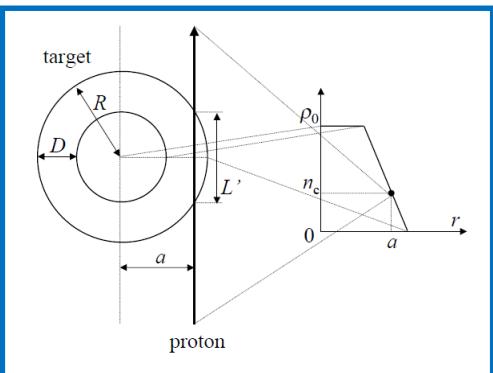
## 中性子過剰核の半径・質量



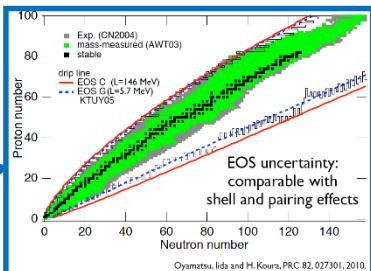
## 原子核のくろたま模型



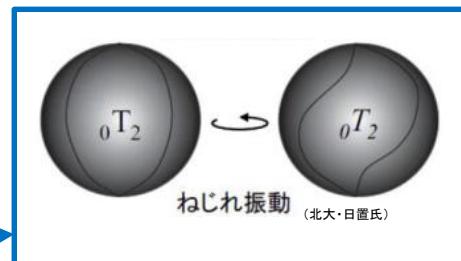
## 原子核反応断面積公式



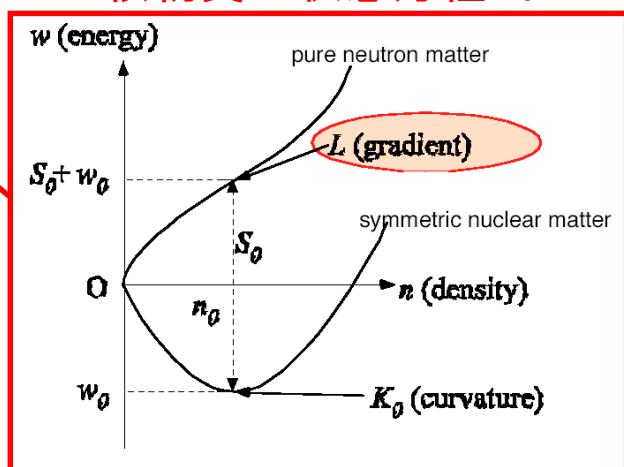
## 中性子ドリップ線



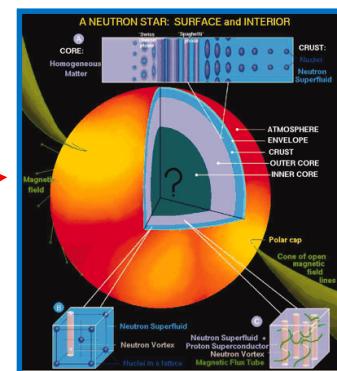
## 中性子星クラストのずりモード



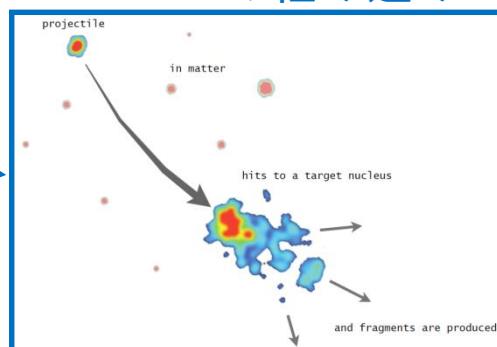
## 核物質の状態方程式



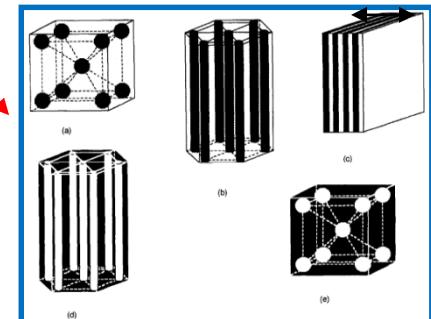
## 軽い中性子星の質量・半径

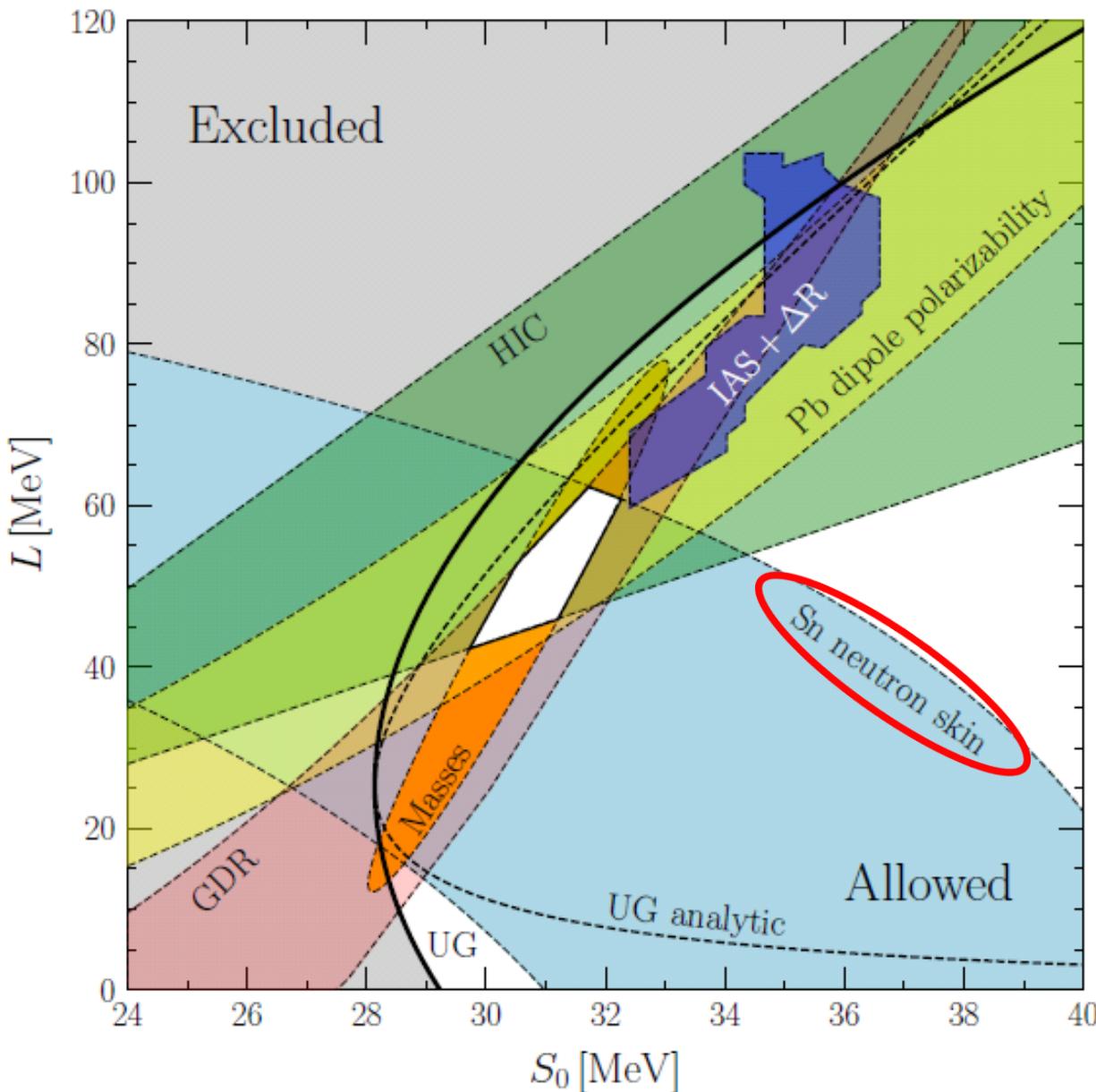


## PHITSへの組み込み



## 中性子星クラスト中のパスタ原子核の存在領域





Ref. Tews, Lattimer, Ohnishi, & Kolomeitsev, arXiv:1611.07133.

# Compressible liquid-drop model

Ref. Iida & Oyamatsu, PRC **69** (2004) 037301.

**Semi-empirical mass formula:**  $-E_B = E_{\text{vol}} + E_{\text{sur}} + E_{\text{Coul}}$

For a spherical nucleus ( $R_p \approx R_n$ ),

$$E_{\text{vol}} = Aw(n_{\text{in}}, \delta_{\text{in}})$$

$$w(n, \delta) \xrightarrow{\delta \approx 0, n \approx n_0} w_0 + \frac{K_0}{18n_0^2}(n - n_0)^2 + \left[ S_0 + \frac{L}{3n_0}(n - n_0) \right] \delta^2$$

$n_0$ ,  $w_0 \approx 0.14\text{-}0.17 \text{ fm}^{-3}, -16 \text{ MeV}$  saturation point of symmetric nuclear matter

$S_0 \approx 25\text{-}40 \text{ MeV}$  symmetry energy coefficient

$K_0 \approx 180\text{-}360 \text{ MeV}$  incompressibility

$L \approx 0\text{-}200 \text{ MeV}$  density symmetry coefficient

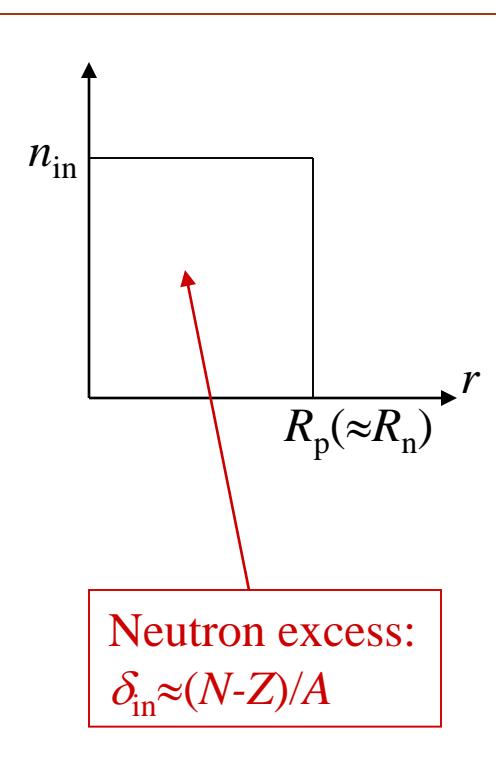
$$E_{\text{sur}} = 4\pi\sigma(n_{\text{in}}, \delta_{\text{in}})R_p^2$$

$$\sigma(n, \delta) \xrightarrow{\delta \approx 0, n \approx n_0} \sigma_0 \left[ 1 - C_{\text{sym}} \delta^2 + \chi \left( \frac{n - n_0}{n_0} \right) \right]$$

$\sigma_0 \approx 1 \text{ MeV fm}^{-2}$  surface tension at  $\delta = 0$  and  $n = n_0$

$C_{\text{sym}} \approx 1.5\text{-}2.5$  surface symmetry energy coefficient

$$E_{\text{Coul}} = \frac{3Z^2 e^2}{5R_p}$$



$\chi=0$  Myers & Swiatecki (1969)  
 $\chi \approx 1/2$  Yamada (1964)  
 $\chi=4/3$  Fermi-gas model

**Pressure equilibrium:**  $\delta E_B|_{A,Z} = 0$ , i.e.,  $P_{\text{vol}} + P_{\text{sur}} + P_{\text{Coul}} = 0$

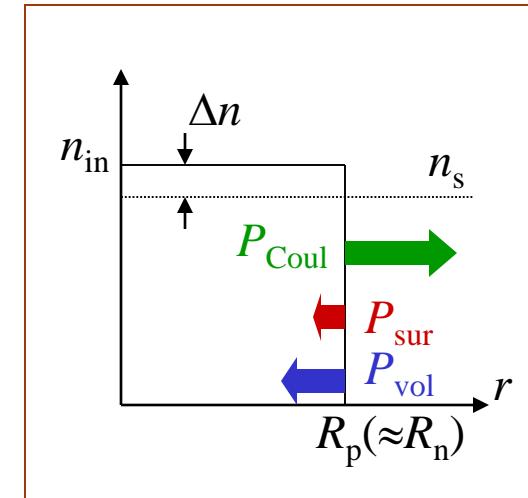
$$P_{\text{vol}} \approx \frac{K_0}{9}(n_{\text{in}} - n_0) + \frac{L}{3}n_0\delta_{\text{in}}^2 \equiv \frac{K_0}{9}(n_{\text{in}} - n_s)$$

$$w(n, \delta) \xrightarrow{\delta \approx 0, n \approx n_0} w_0 + \frac{K_0}{18n_0^2}(n - n_0)^2 + \left[ S_0 + \frac{L}{3n_0}(n - n_0) \right] \delta^2$$

$$P_{\text{sur}} \approx -\frac{2\sigma_0}{R_p} \left( 1 - \frac{3}{2}\chi \right) = 0 \quad \text{at } \chi = 2/3 !$$

$$\sigma(n, \delta) \xrightarrow{\delta \approx 0, n \approx n_0} \sigma_0 \left[ 1 - C_{\text{sym}}\delta^2 + \chi \left( \frac{n - n_0}{n_0} \right) \right]$$

$$P_{\text{Coul}} = \frac{Z^2 e^2}{5V R_p}, \quad V = A n_{\text{in}}^{-1}$$



Saturation density of uniform matter at neutron excess  $\delta_{\text{in}}$ :

$$n_s = n_0 - \frac{3n_0 L}{K_0} \delta_{\text{in}}^2 \quad (\leftarrow P_{\text{vol}} = 0)$$

Density difference:

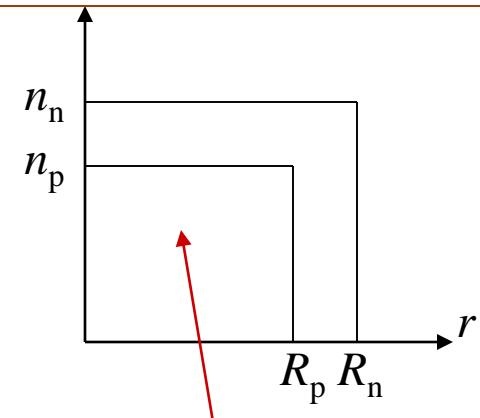
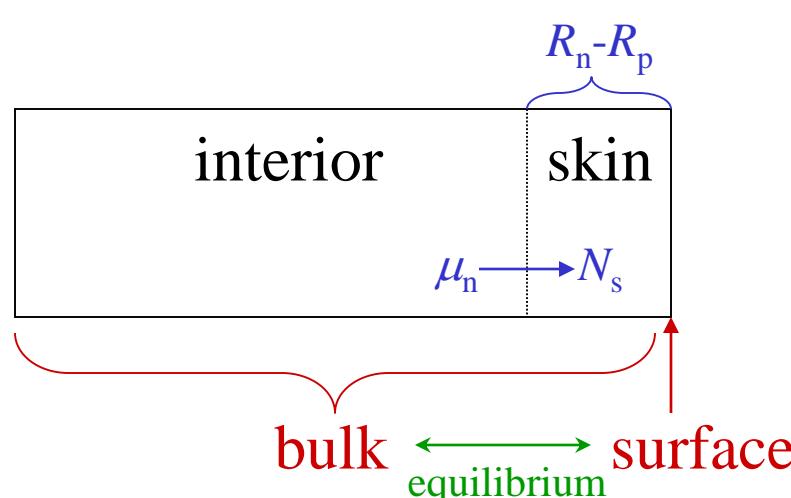
$$\Delta n \equiv n_{\text{in}} - n_s \approx -\frac{9}{K_0} (P_{\text{sur}} + P_{\text{Coul}}) \sim 0.1n_0 \quad \text{for } \chi = 0$$

$$\sim -0.1n_0 \quad \text{for } \chi = 4/3$$

— a quantity useful for deduction of the value of  $\chi$

## *Thermodynamic description of the nuclear surface*

Ref. Pethick & Ravenhall, NPA **606**(1996)173.



Neutron excess:  

$$\delta_{in} = (n_n - n_p)/(n_n + n_p)$$
  

$$\approx (N-Z)/A - 3(R_n - R_p)/2R_p$$

Small change in  $\delta_{in}$  →

$$\Delta\Omega = -N_s \Delta\mu_n$$

Surface tension:  
 $s = (\Omega_{tot} - \Omega_{bulk}) / (\text{area of the surface})$

Neutron skin:  
adsorbed neutrons at the surface

In the absence of  
Coulomb energy,

$$R_n - R_p \approx C \frac{N - Z}{A} \left( 1 + \frac{3C}{2R_p} \right)^{-1}, \quad C \equiv \frac{2\sigma_0}{S_0 n_0} \left( C_{\text{sym}} + \frac{3L\chi}{K_0} \right)$$

**Coulomb effects** Ref. Myers & Swiatecki, NPA **336**(1980)267.

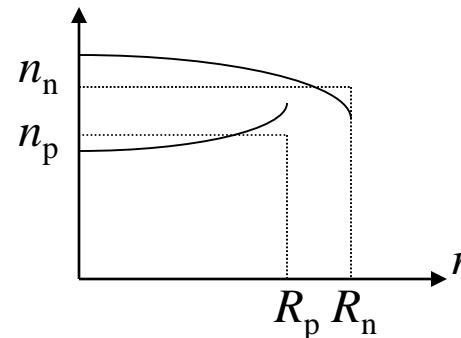
- Reduction of the neutron-skin driving force

$$R_n - R_p \propto \frac{N - Z}{A} \Rightarrow R_n - R_p \propto \frac{N - Z}{A} - \frac{Ze^2}{20R_p S_0}$$

↑  
proton skin at  $N=Z$

- Polarization of the nuclear interior

$$R_n - R_p \Rightarrow R_n - R_p - \frac{Ze^2}{70S_0}$$



Eventually,

$$R_n - R_p \approx C \left( \frac{N - Z}{A} - \frac{Ze^2}{20R_p S_0} \right) \left( 1 + \frac{3C}{2R_p} \right)^{-1} - \frac{Ze^2}{70S_0}, \quad C \equiv \frac{2\sigma_0}{S_0 n_0} \left( C_{\text{sym}} + \frac{3L\chi}{K_0} \right)$$

Cf. The diffuseness correction is ignored.

Poorly known

# Diffuseness correction to neutron skin thickness

$$\Delta r_{np}^{\text{surf}} \simeq \sqrt{\frac{3}{5}} \frac{5}{2R} (b_n^2 - b_p^2)$$

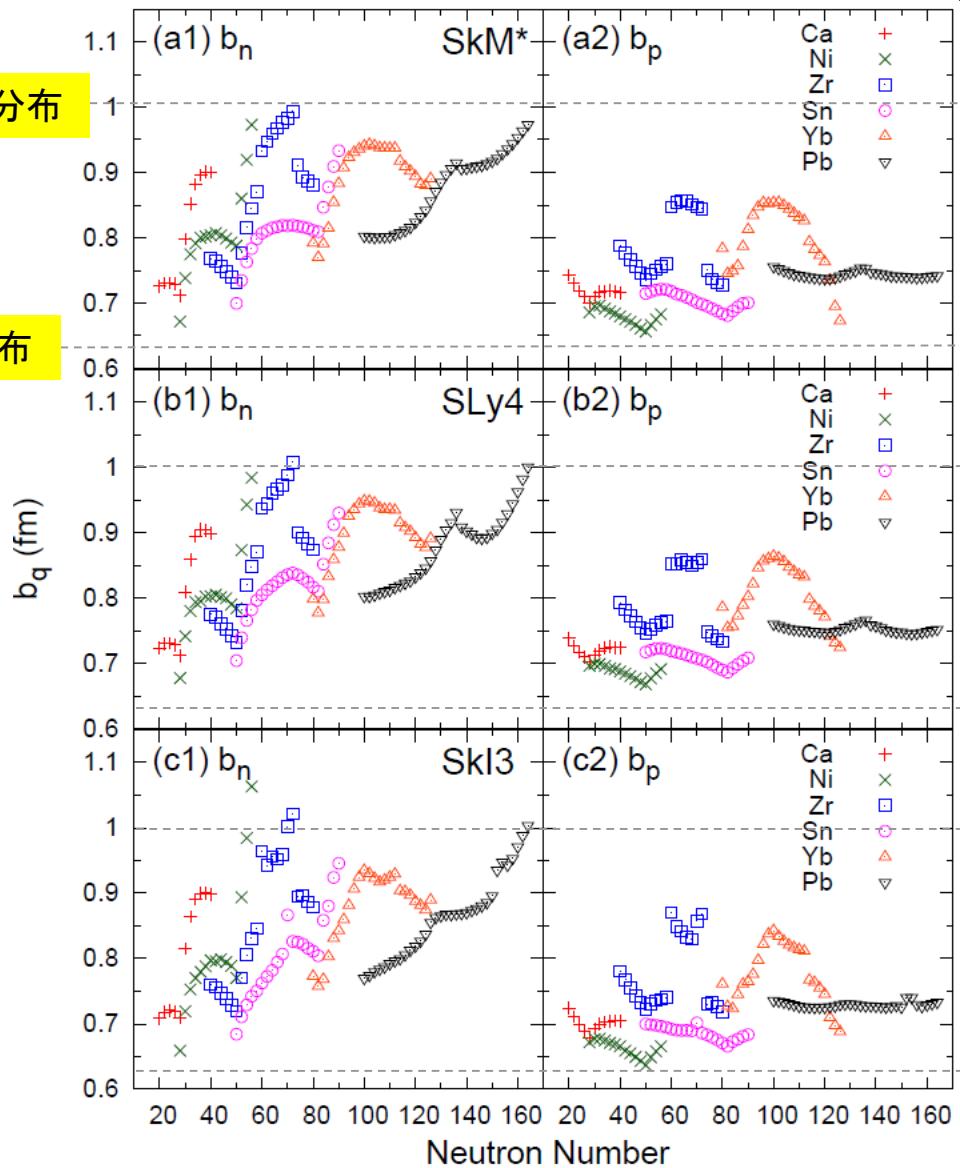
with

$$b_q^2 = \frac{2 \int_{c_q}^{\infty} (r - c_q)^2 [(r - c_q)^2 + c_q^2] \rho'_q(r) dr}{\int_0^{\infty} r^2 \rho'_q(r) dr}$$

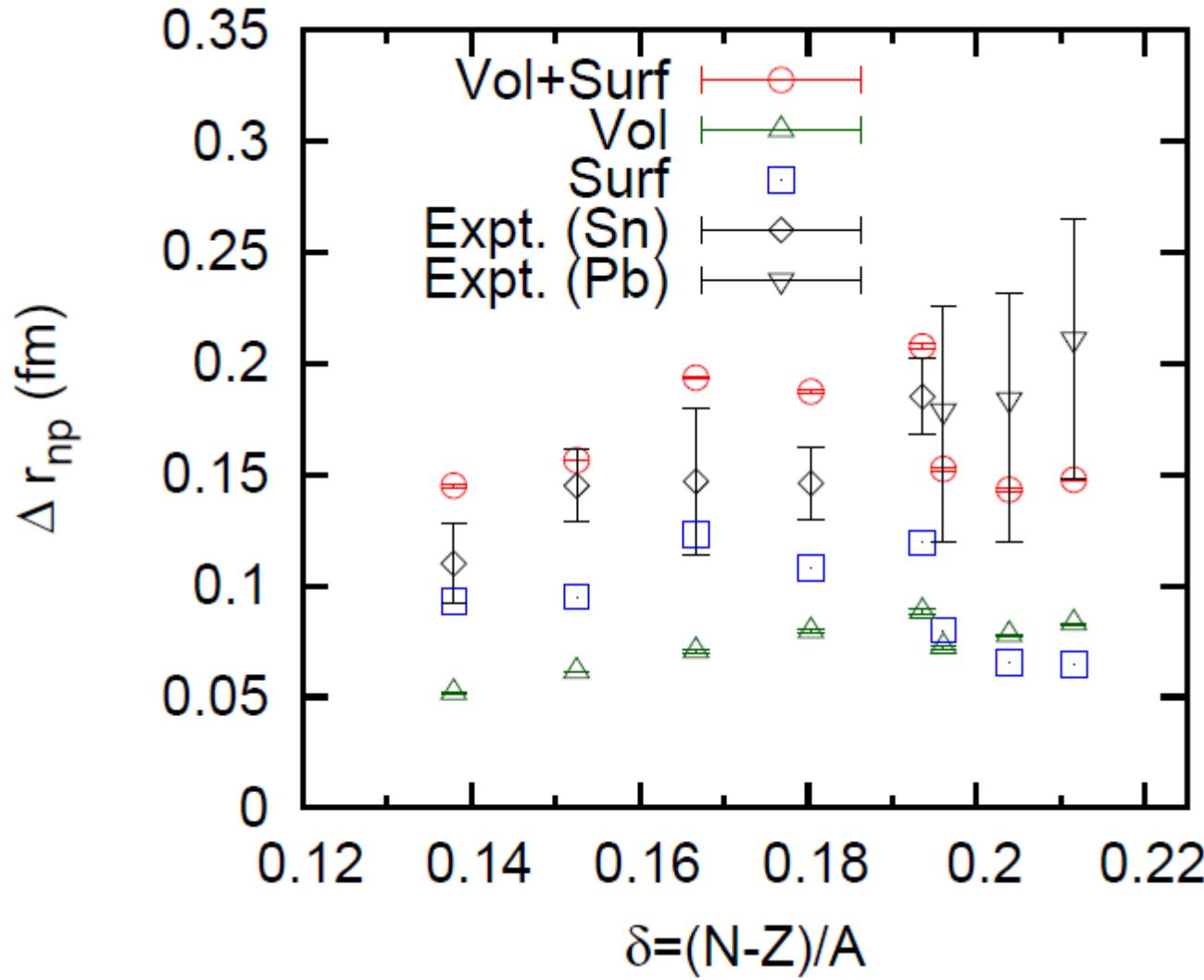
$$c_q = \frac{4\pi \int_0^{\infty} r^3 \rho'_q(r) dr}{4\pi \int_0^{\infty} r^2 \rho'_q(r) dr}$$

フェルミ分布

台形分布



## Why the EOS dependence of neutron skin thickness is so elusive?



Only  $C$  is empirically determined as  $\sim 1.06$ .

The diffuseness correction is of the order of the liquid-drop contribution.

# Conclusion

Neutron star  
observations

Laboratory  
nuclei

Properties of nuclear matter  
e.g., the symmetry energy

