

Mechanisms of (semi-)Exclusive DY processes

KEK Workshop on hadron physics with high momentum hadron beams at

J-PARC

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Oleg Teryaev
JINR, Dubna

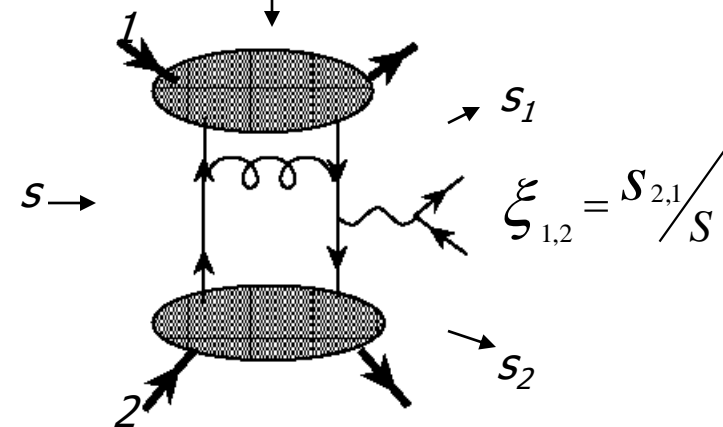
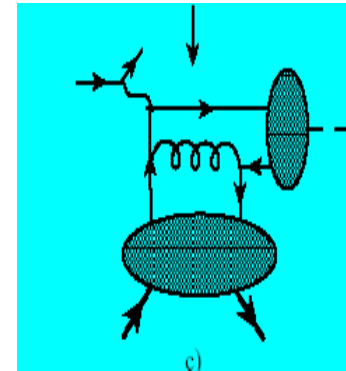
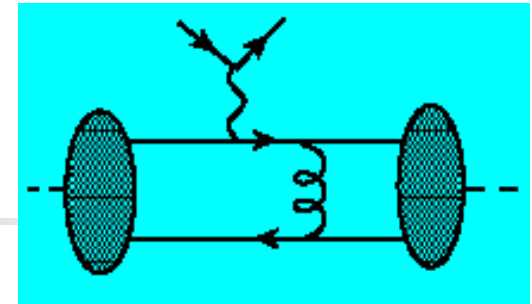


Outline

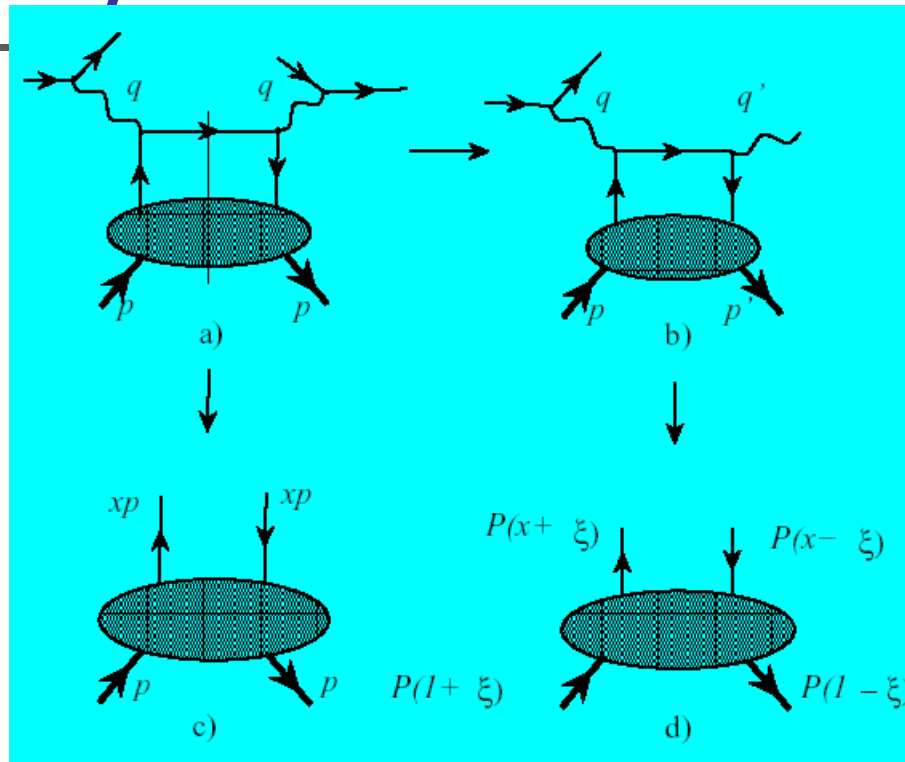
- Exclusive hard processes: analyticity and factorization
- Interference between exclusive lepton pair production mechanisms
- Transverse SSA in DY: contour gauge and factor 2
- DYW/BG-type duality in DY: SSA, Siverson function and time-like formfactors

Ways to to exclusive DY

- Simplest case - pion FF(ERBL)
- Change DA to GPD- exclusive electroproduction (Frankfurt,Strikman)
- $M_{DY} \sim M_{DVCS} F_{\pi|g|g^*}$
- Time from right to left- exclusive DY (DAXGPD)- Berger,Diehl,Pire
- Phase sign change: c.f. Sivers for SIDIS/DY
- Analytic properties \sim factorization (not completely lear yet)
- Second DA->GPD-another mechanism- OT'05 (problems with factorization -analytic continuation to be performed)



QCD Factorization for DIS and DVCS/DVMP



- Manifestly spectral

$$\mathcal{H}(x_B) = \int_{-1}^1 dx \frac{H(x)}{x - x_B + i\epsilon}$$

- Extra dependence on ξ

$$\mathcal{H}(\xi) = \int_{-1}^1 dx \frac{H(x, \xi)}{x - \xi + i\epsilon}$$



Unphysical regions

- DIS : Analytical function – if $1 \leq |X_B|$ polynomial in $1/x_B$

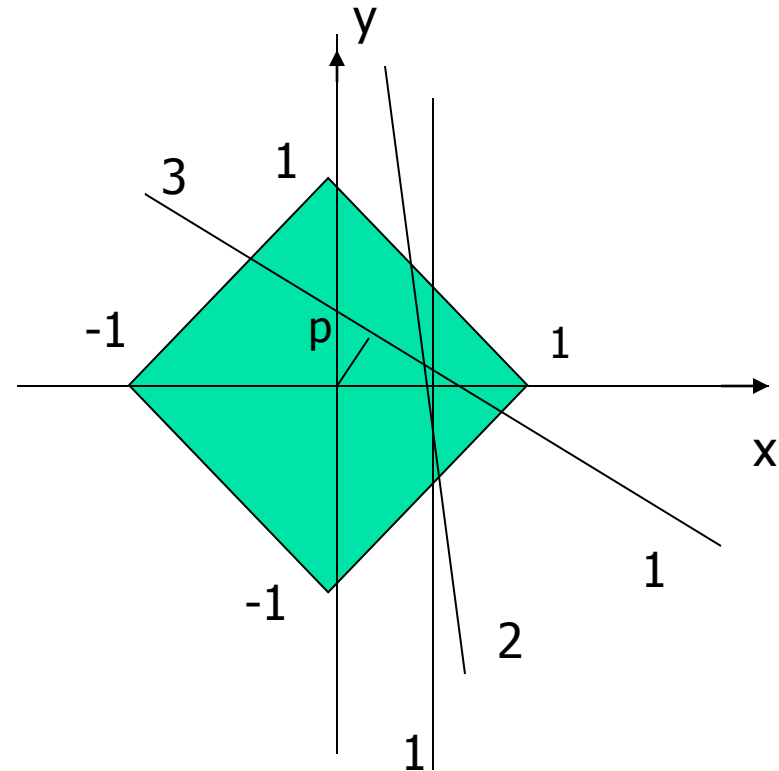
$$H(x_B) = - \int_{-1}^1 dx \sum_{n=0}^{\infty} H(x) \frac{x^n}{x_B^{n+1}}$$

- DVCS – additional problem of analytical continuation of $H(x, \xi)$
- Solved by using of Double Distributions Radon transform

$$H(z, \xi) = \int_{-1}^1 dx \int_{|x|-1}^{1-|x|} dy (F(x, y) + \xi G(x, y)) \delta(z - x - \xi y)$$

Double distributions and their integration

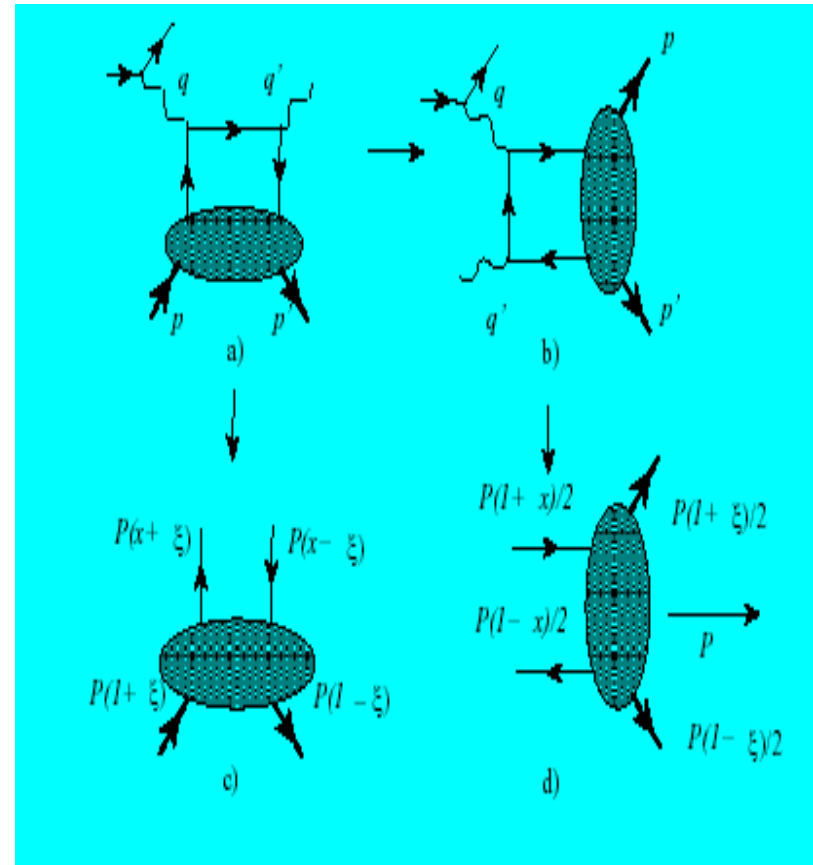
- Slope of the integration line-skewness
- Kinematics of DIS: $\xi = 0$
("forward") - vertical line (1)
- Kinematics of DVCS: $\xi < 1$
- line 2
- Line 3: $\xi > 1$ unphysical region - required to restore DD by inverse Radon transform: tomography



$$\begin{aligned}
 f(x, y) &= -\frac{1}{2\pi^2} \int_0^\infty \frac{dp}{p^2} \int_0^{2\pi} d\phi |\cos\phi| (H(p/\cos\phi + x + ytg\phi, t g\phi) - H(x + ytg\phi, t g\phi)) = \\
 &= -\frac{1}{2\pi^2} \int_{-\infty}^\infty \frac{dz}{z^2} \int_{-\infty}^\infty d\xi (H(z + x + y\xi, \xi) - H(x + y\xi, \xi))
 \end{aligned}$$

Crossing for DVCS and GPD

- DVCS \rightarrow hadron pair production in the collisions of real and virtual photons
- GPD \rightarrow Generalized Distribution Amplitudes



GDA -> back to unphysical regions for DIS and DVCS

- Recall DIS

$$H(x_B) = - \int_{-1}^1 dx \sum_{n=0}^{\infty} H(x) \frac{x^n}{x_B^{n+1}}$$

- Non-positive powers of x_B

- DVCS

$$H(\xi) = - \int_{-1}^1 dx \sum_{n=0}^{\infty} H(x, \xi) \frac{x^n}{\xi^{n+1}}$$

- Polynomiality (general property of Radon transforms): moments - integrals in x weighted with x^n - are polynomials in $1/\xi$ of power $n+1$
- As a result, analyticity is preserved: only non-positive powers of ξ appear



Holographic property (OT'05)

Factorization
Formula

->

$$\mathcal{H}(\xi) = \int_{-1}^1 dx \frac{H(x, \xi)}{x - \xi + i\epsilon}$$

- Analyticity
("dynamical") ->
Imaginary part ->
Dispersion relation:

$$\mathcal{H}(\xi) = \int_{-1}^1 dx \frac{H(x, x)}{x - \xi + i\epsilon}$$

$$\Delta\mathcal{H}(\xi) \equiv \int_{-1}^1 dx \frac{H(x, x) - H(x, \xi)}{x - \xi + i\epsilon}$$

- "Holographic" equation
(DVCS AND VM)

$$= \sum_{n=1}^{\infty} \frac{1}{n!} \frac{\partial^n}{\partial \xi^n} \int_{-1}^1 H(x, \xi) dx (x - \xi)^{n-1} = \text{const}$$



Holographic property - II

- Directly follows from double distributions

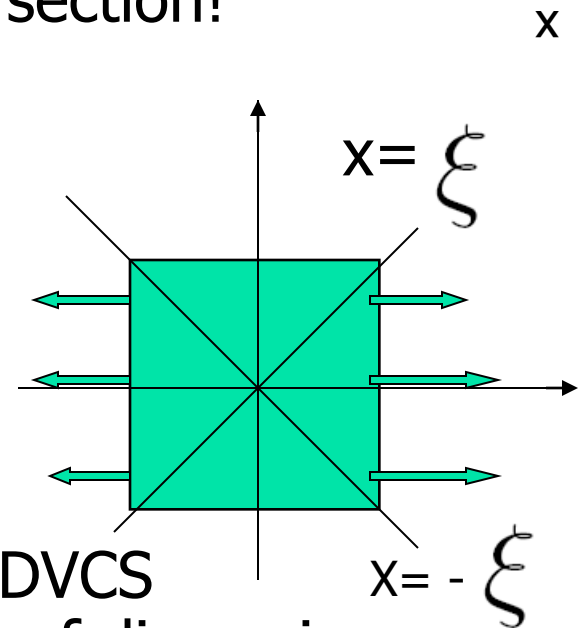
$$H(z, \xi) = \int_{-1}^1 dx \int_{|x|-1}^{1-|x|} dy (F(x, y) + \xi G(x, y)) \delta(z - x - \xi y)$$

- Constant is the SUBTRACTION one - due to the (generalized) Polyakov-Weiss term $G(x, y)$

$$\begin{aligned} \Delta \mathcal{H}(\xi) &= \int_{-1}^1 dx \int_{|x|-1}^{1-|x|} dy \frac{G(x, y)}{1-y} \\ &= \int_{-\xi}^{\xi} dx \frac{D(x/\xi)}{x - \xi + i\epsilon} = \int_{-1}^1 dz \frac{D(z)}{z - 1} = \text{const} \end{aligned}$$

Holographic property - III

- 2-dimensional space \rightarrow 1-dimensional section!
- Momentum space: any relation to holography in coordinate space ?!
- ERBL \rightarrow "GDA" region
- Strategy (now adopted) of GPD's studies: start at diagonals (through SSA due to imaginary part of DVCS amplitude) and restore by making use of dispersion relations + subtraction constants



DY?!

Time-like amplitudes and analyticity



- Extra cuts in Q^2 appear
- Scaling: $F(Q^2/s) = F(-Q^2/-s)$: cuts cancellation (cf inclusive electron-positron annihilation)
- $F(Q^2/u) = F(-Q^2/-u)$ – cuts in Q^2 has a form of cuts in u (opposite pole prescription) – diagonals on holographic plot interchanged
- Factorization proof: start in unphysical region in skewness where factorization holds (cuts cancelled but what about NLO?! – nonfactorizable corrections!?) and continue to physical region

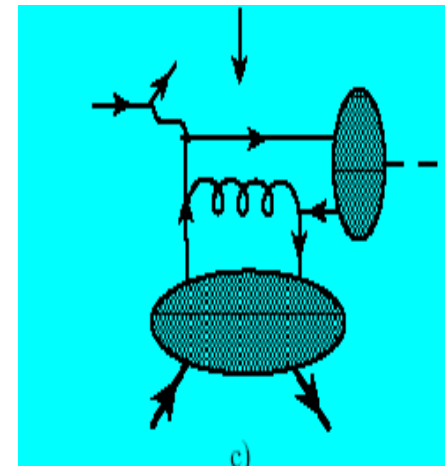
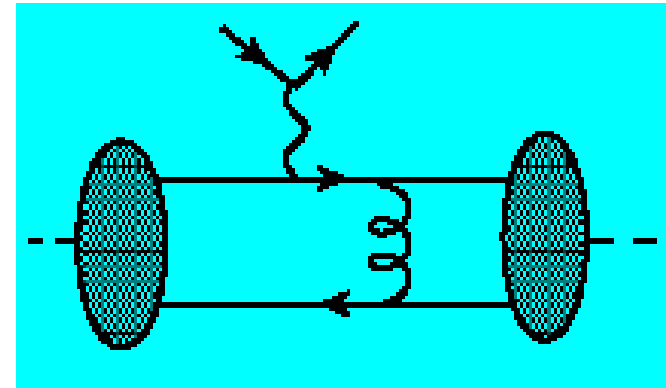
"Dispersive" factorization proof

- Starting from (Pion) form factor- 2 DA's –no cuts

$$F \square \left(\int dx \frac{\phi(x)}{1-x} \right)^2$$

- 1 DA -> GPD :Exclusive mesons production:
Factorization = DR + D-subtraction
- (DVMP/DY) - +/-

$$M \square \int dx \frac{\phi(x)}{1-x} \int dx \frac{H(x, \xi)}{x - \xi + i\varepsilon}$$



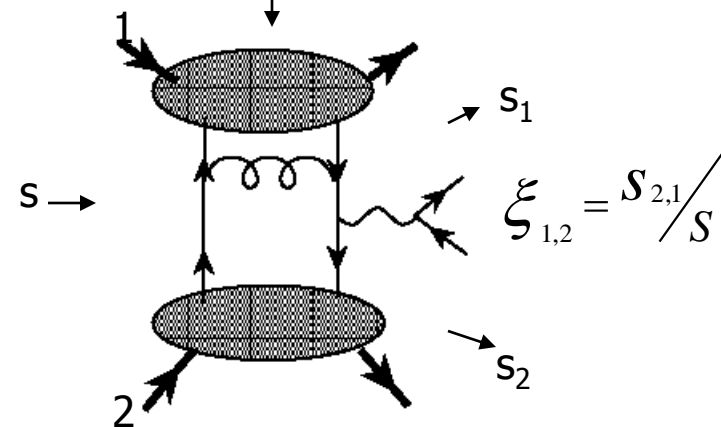
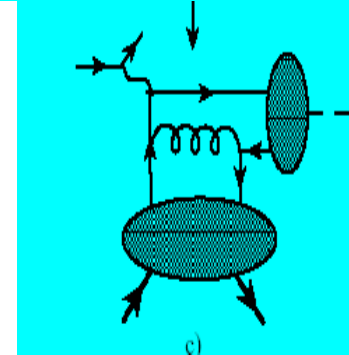
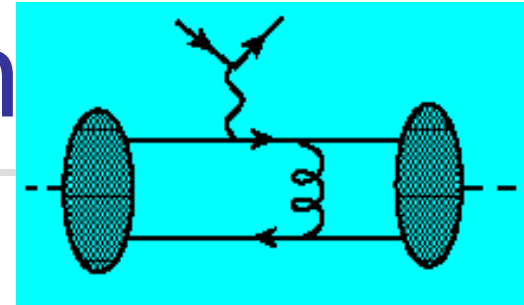
Next step: 2 DA's -> 2 GPD's- Double Diffraction

- Exclusive double diffractive DY process
- Analytic continuation:

$$M \square \int dx \frac{H(x, \xi_1)}{x - \xi_1 \pm i\epsilon} \int dy \frac{H(y, \xi_2)}{y - \xi_2 \mp i\epsilon}$$

- DIFFERS from direct calculation – NO factorization in physical region

$$M \square \iint dx dy \frac{H(x, \xi_1) H(y, \xi_2)}{(x - \xi_1)(y - \xi_2) + i\epsilon}$$





Double Diffraction: properties and problems

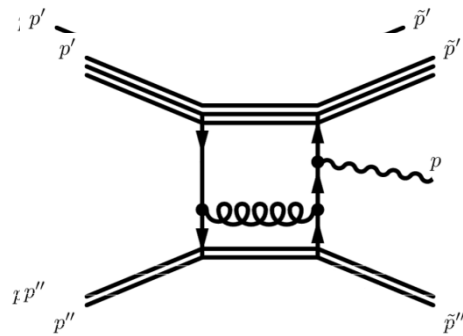
- Holographic equation: DR contains double and single (linear in D-term) dispersion integrals as well as subtraction (quadratic in D-term)
- $F(Q^2/s) \rightarrow F(s_i/s), F(s_i/s_j)$
- Analytic continuation for various cuts is still unclear. Possible cancellation of cuts – real amplitude?



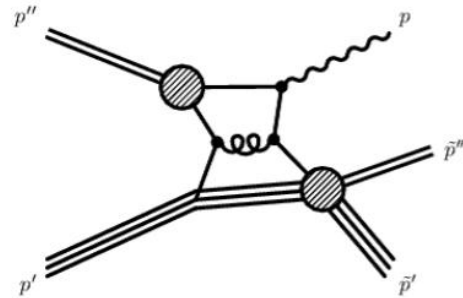
Interference effects

- Interference with pure EM (FFxFF) production of (C-even) lepton pair contains only real IR safe part of the amplitude and gives rise to charge asymmetry (Pivovarov,OT, work in progress)
- The way to extract GPDxGPD in central region from inclusive DY

Interference with DGP(TDA) mechanism



(16 diagrams)



(8 diagrams)



Interference in exclusive DY

- In the forward region interference with BDP-like mechanism with TDA (Pivovarov, OT'14)

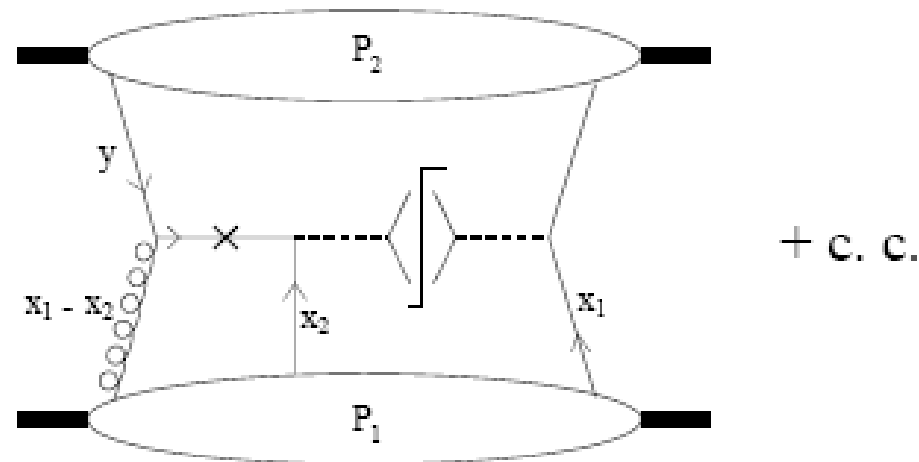
$$\frac{d\sigma}{d^3\tilde{p}'d^3\tilde{p}''} = \frac{\alpha_{(em)}\alpha_{(s)}^2}{2^6 N_c^4 \pi^2 \tilde{\epsilon}'\tilde{\epsilon}''} \cdot \frac{1}{(p', p'')^2} \cdot \left[\frac{8s^2}{s_1 s_2} |I_1|^2 + \frac{8s}{s_1 + s_2 - s} |I_2|^2 + 4s \left(\frac{1}{s_2} + \frac{s}{s_1(s_1 + s_2 - s)} \right) (I_1^* I_2 + I_2^* I_1) \right] \cdot \delta(q^2 - m_\gamma^2)$$

SSA in DY

- TM integrated DY with one transverse polarized beam – unique SSA – gluonic pole (Hammon, Schaefer, OT) – “factor 2” problem

$$A = g \frac{\sin 2\theta \cos \phi \left[T(x, x) - x \frac{dT(x, x)}{dx} \right]}{M [1 + \cos^2 \theta] q(x)}$$

- Twist 3 – energy should not be too large (J-PARC)



Contour gauge in DY

(Anikin,OT, PLB690 (2010) 519; Direct photons - arXiv: 1501.05900)

- Motivation of contour gauge – $[-\infty^-, 0^-] = 1$
elimination of link

- Field'

$$[-\infty^-, 0^-] = P \exp \left\{ -ig \int_{-\infty}^0 dz^- A^+(0, z^-, \vec{0}_T) \right\}$$

$$A^\mu(z) = \int_{-\infty}^{\infty} d\omega^- \theta(z^- - \omega^-) G^{+\mu}(\omega^-) + A^\mu(-\infty)$$

- Gluonic pole appearance

$$B^V(x_1, x_2) = \frac{T(x_1, x_2)}{x_1 - x_2 + i\epsilon}$$

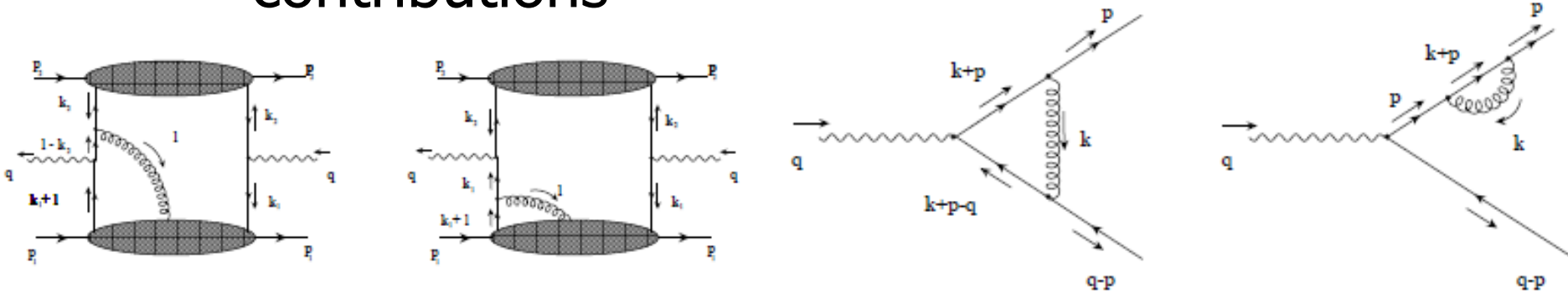
- cf naïve expectation

$$B^V(x_1, x_2) = \frac{\mathcal{P}}{x_1 - x_2} T(x_1, x_2)$$

- Source of "Hidden" phase

New phases and (EM) gauge invariance

- EM GI (experience from $g_2, DVCS$) – 2 contributions



- Cf PT – only one of two diagrams contribute to SSA and required for GI
- NP tw3 analog - GI only if GP absent

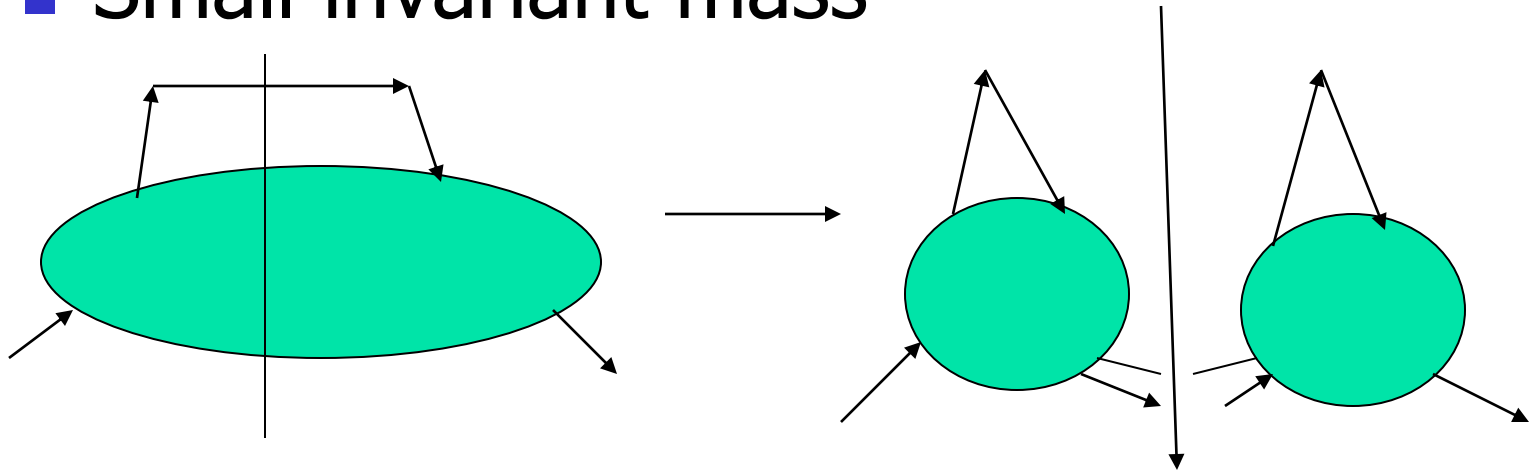


Hidden phase

- Analogous to Beliitsky, Ji, Yuan finding for gauge link?! (GP/Sivers relation – Boer, Mulders, Pijlman; Ji, Qiu, Vogelsang, Yuan)
- Plasma physics: phase of naively real poles - Landau damping
- GP – “Hidden phases” – experimental tests@J-PARC?!

Exclusive limit : DIS and space-like (transitional and elastic) FFs

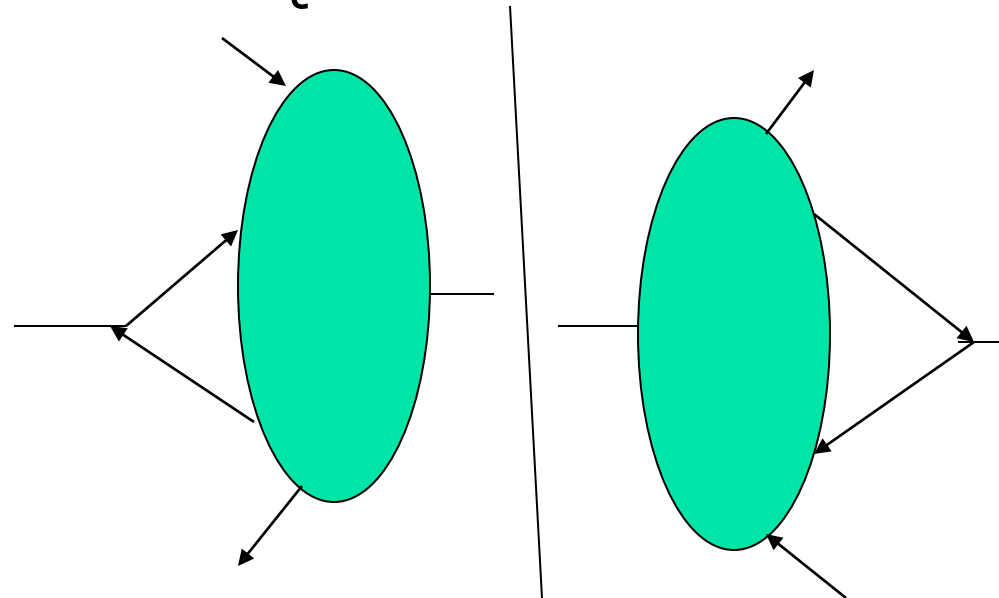
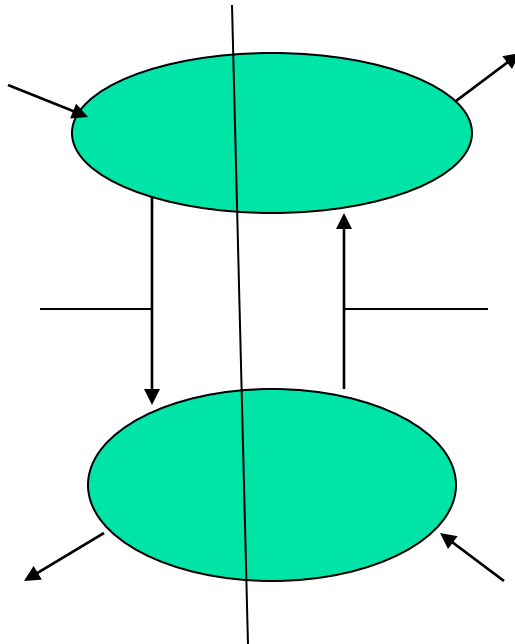
- Small invariant mass



- May be related to unitarity analyticity and DR (OT'05)
- Relation between $x \rightarrow 1$ and large Q^2
- pdf $\sim (FF)^2$

Exclusive limit of DY and time-like FFs (OT'14)

- (Proton-antiproton) DY at small $s - Q^2$



$(pdf)^2 \sim (\text{Dirac}) (FF)^2$

- Other beams – baryon number conservation – time-like transition FFs

Comparing space-like and time-like FFs

- “Duality intervals” - from mass to x-space
- DIS: $(P+q)^2 = (P_f + \delta P_{DIS})^2 = (M + \mu_{DIS})^2$ $\mu_{DIS} \sim$ pion related scale
- Deviation of $x_B (\equiv 1 - \delta_{DIS})$ from 1
$$\delta_{DIS} \sim 2M\mu_{DIS}/Q^2.$$
- DY: $(P_1 + P_2)^2 = (q + \delta P_{DY})^2$
- Deviation of $\tau = Q^2/s (\equiv 1 - \delta_{DY})$ from 1
$$\delta_{DY} \sim 2\mu_{DY}/Q$$



DR: FFs from duality intervals

- DIS: $F_{SL}^2 \sim \int_0^{\delta_{DIS}} d\bar{x} f(\bar{x}) \quad x = 1 - \bar{x}$

- DY: $F_{TL}^2 \sim \int_0^{\delta_{DY}} d\bar{x}_1 d\bar{x}_2 f(\bar{x}_1) f(\bar{x}_2) \delta(\delta_{DY} - \bar{x}_1 - \bar{x}_2)$

- Proton-antiproton DY –same parton distributions $f(\bar{x}) = C\bar{x}^a$

$$F_{SL}^2(Q^2) \sim \frac{C}{a+1} \left(\frac{2M\mu_{DIS}}{Q^2} \right)^{a+1} ; F_{TL}^2(Q^2) \sim \frac{C^2}{2(a+1)} \left(\frac{4\mu_{DY}^2}{Q^2} \right)^{a+1}$$

- Pion: $a=1$ supported !?



SL vs TL

- Same Q-dependence
- Normalization –defined by distribution scale (~ 5) and duality intervals
- Asymptotically coincide – scales close to QCDSR pion duality interval (rather than pion mass) similar (equal?!) for DIS and DY) !?
- Experimental tests at J-PARC – like BG tests in DIS@Jlab – lower energy pion beams

Sivers function and formfactors



- Relation between Sivers function and AMM known on the level of matrix elements (Brodsky, Schmidt, Burkardt)
- Phase?
- Duality for observables?

BG/DYW type duality for DY SSA in exclusive limit

- Proton-antiproton DY – valence annihilation – analyticity - cross section is described by Dirac FF squared
- The SSA (analyticity?!) similar to twist 3 one- due to interference of Dirac and Pauli FF's with a phase shift (Rekalo, Brodsky)
- Exclusive large energy limit; $x \rightarrow 1$:
 $T(x,x)/q(x) \rightarrow \text{Im } F2/F1(Q^2 \sim M^2(1-x))$
- Both directions – estimate of Sivers at large x and explanation of phases in FF's



CONCLUSIONS/OUTLOOK

- Analyticity - natural way of factorization proof. DY – holds due to cuts cancellation, but possible problems at NLO
- Interference and QCD induced charge asymmetry is possible for lepton pairs production
- SSA@DY factor 2 (“Landau damping”) – can it be tested at J-PARC?
- BG/DYW for FF’s – J-PARC at lower energy?